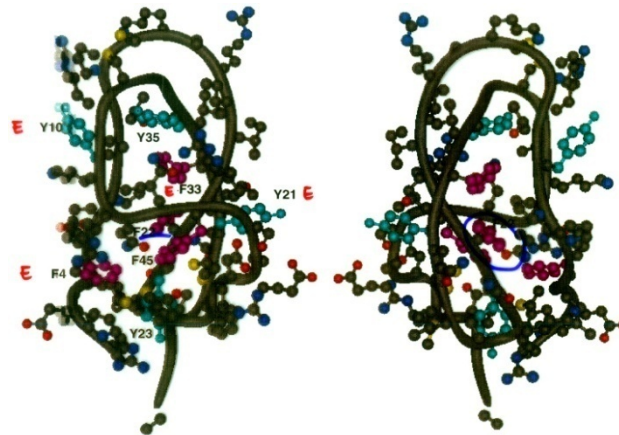


# Protein Dynamics

10/1/14 and 10/3/14



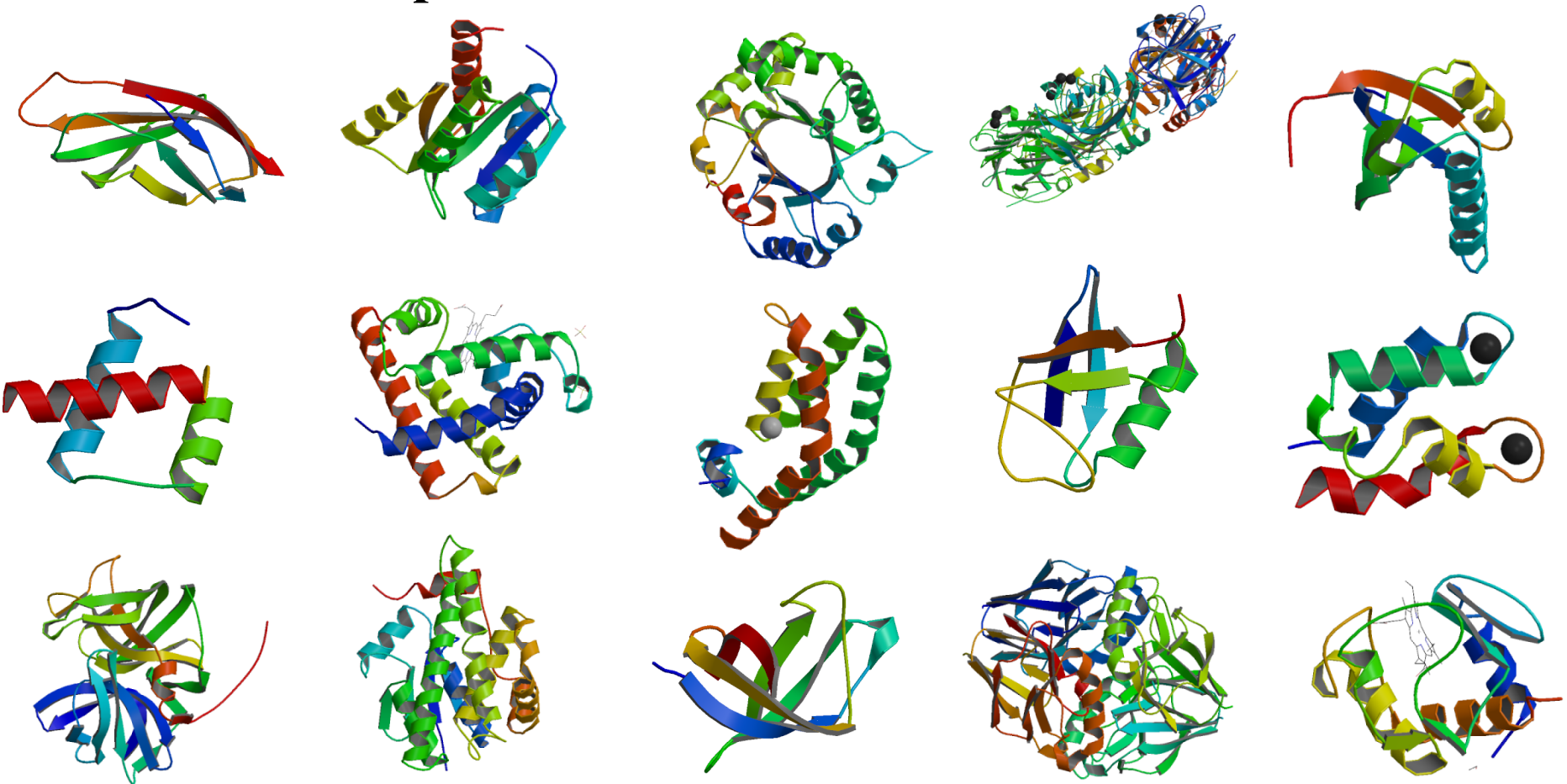
Valerie Daggett

[daggett@u.washington.edu](mailto:daggett@u.washington.edu)

# Proteins

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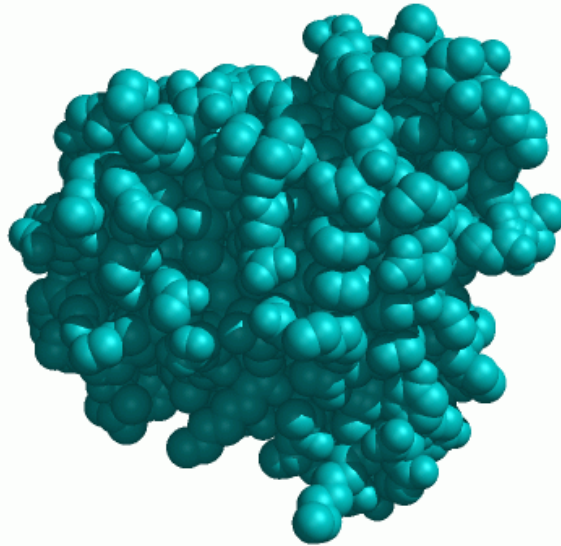
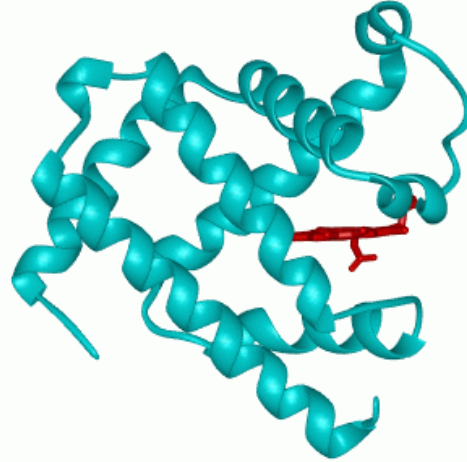
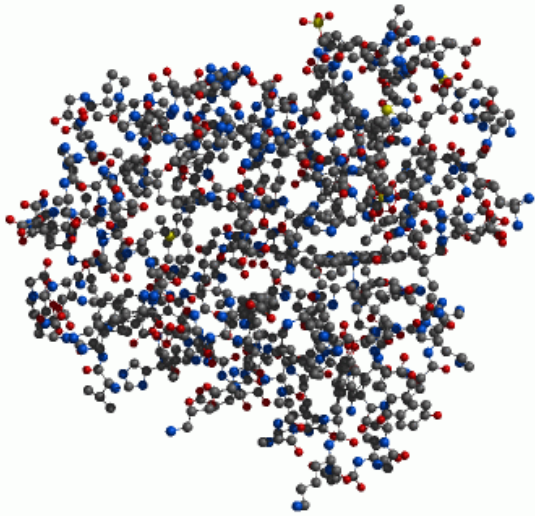
**Many shapes, many sizes, >100,000 in PDB → 807 unique autonomous protein folds**



# Protein Structure

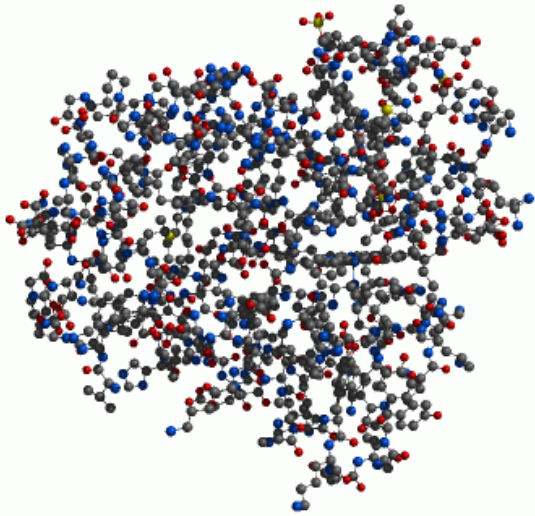
- First protein crystal structure solved in the 1950s
- Myoglobin
- Nobel prize to Perutz and Kendrew

# Myoglobin

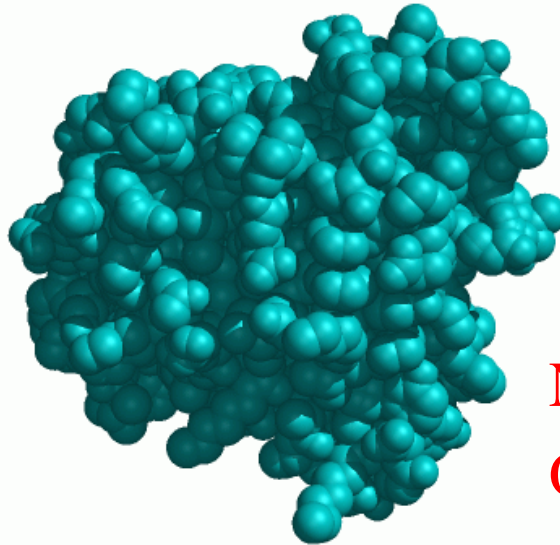




# Myoglobin



Tightly packed!



No pathway for  
 $O_2 \rightarrow$  heme!

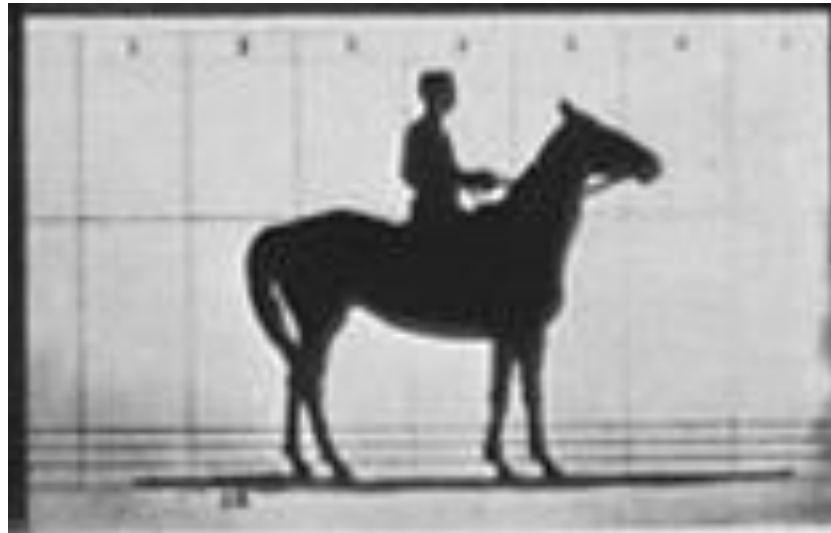
# Protein Dynamics

- Proteins are not static
- Motion is an incontrovertible consequence of existing @ room temperature (or any  $T > 0$  K)
- Kinetic energy per atom is  $\sim 1$  kcal/mole @ 298K (25°C)  
 $\Rightarrow$  several Å/ps
- Motion recognized to be important since first crystal structure solved

...everything that living things do  
can be understood in terms of  
the jigglings and wiggings of  
atoms.

Richard Feynman

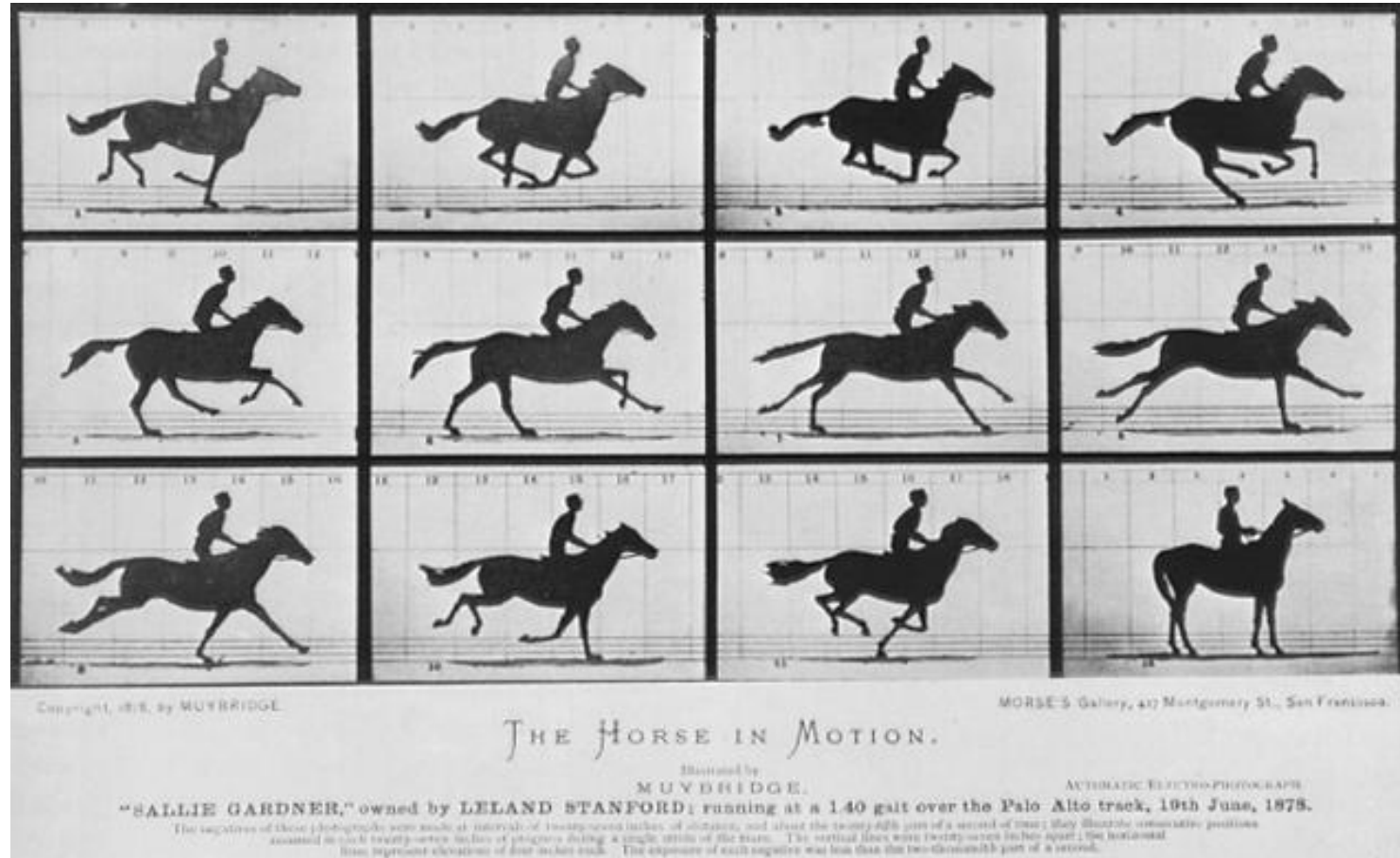
# Function from Static Structure



# Dynamics necessary for function



# Dynamics Necessary for Function

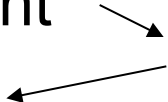


# Outline of Lecture

- Prevalent Protein Motions

- Experiment

- Theory



Problems w/extracting detailed structural information regarding dynamics from expt

- Biological Relevance

- » Is motion just a result of thermal energy and weak interactions, or is such motion functionally important and designed into a protein?



# Prevalent Protein Motions

<u>Type of Motion</u>	<u>Extent of Motion (Å)</u>	<u>Time Scale</u>	
Bond Vibration	0.01-0.1	0.01-0.1 ps	
Side Chain Rotation	5-10 <b>E</b> 5 <b>B</b>	10-100 ps <b>E</b> 10 <sup>8</sup> -10 <sup>12</sup> ps <b>B</b> (0.1-10 <sup>3</sup> ms)	<b>1</b>
Breathing	0.5-2	10 ps-1 ns	<b>2</b>
Relative Motion - hinge bending - allosteric tran.	1-15	10 ps-1 s	<b>3</b>
Local Denaturation	5-10	< ms, μs, ns <b>deadtime</b>	

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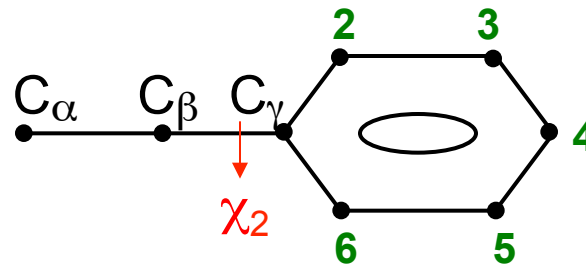
10<sup>12</sup> ps/s

10<sup>9</sup> ns/s

# 1

## Side Chain Rotations

- Ring flips
- $^1\text{H}$  NMR
  - Rotational freedom of Tyr and Phe



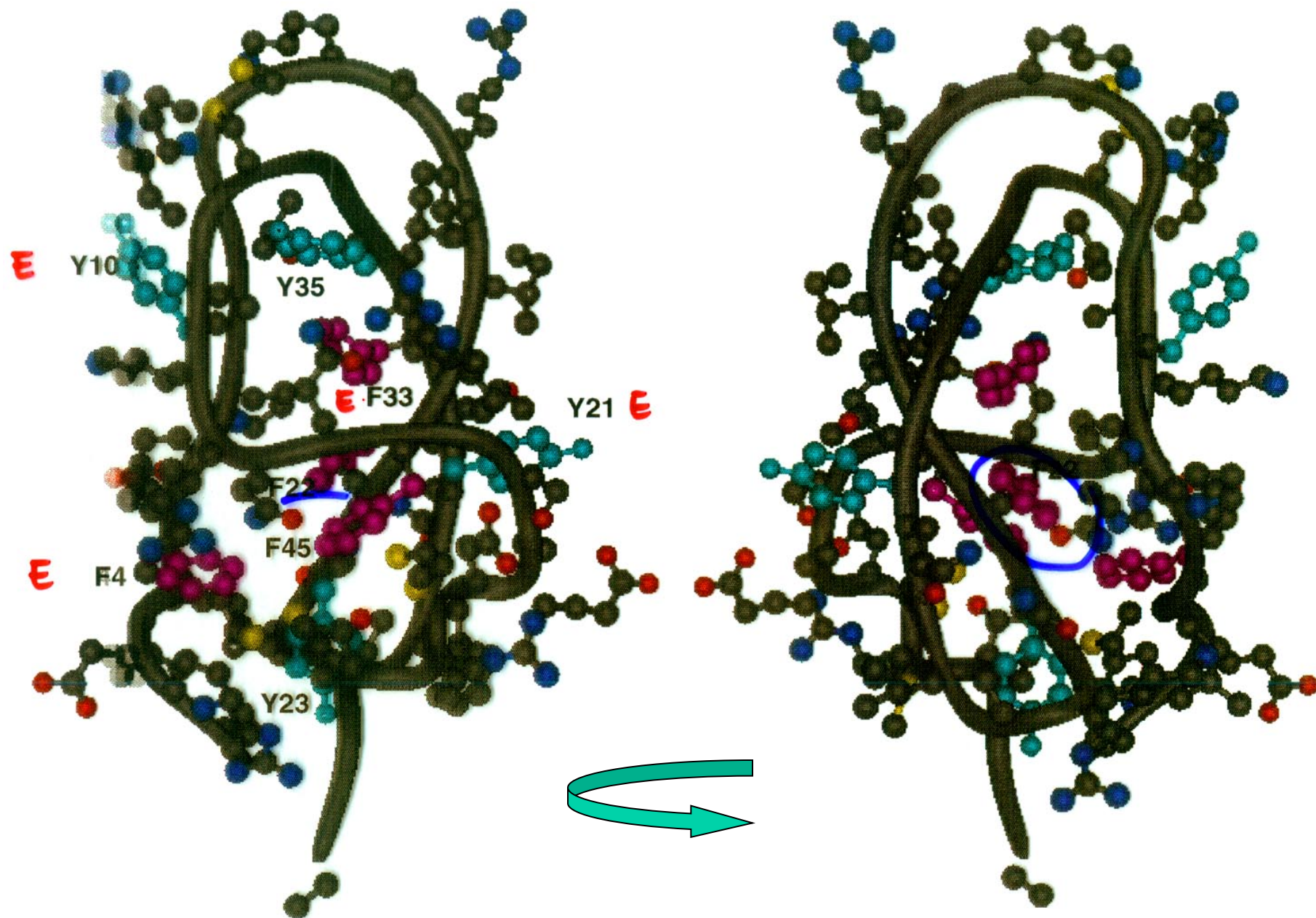
- Isotropic - Rapid rotation on NMR time scale
  - 2 pairs of closely spaced doublets  $2=6$   
 $3=5$   
 $10^4\text{-}10^5/\text{s}$
- Anisotropic - Slow rotation
  - 4 separate resonances  
 $1\text{-}10/\text{s}$

Table 7.6 Rotation of Aromatic Rings in BPTI

Residue	Frequency of 180° Rotations (s <sup>-1</sup> ) at Temperature of			Activation Parameters		
	4°C	40°C	80°C	Enthalpy $\Delta H^\ddagger$ (kcal/mol)	Entropy $\Delta S^\ddagger$ [cal/(mol · °C)]	Volume $\Delta V^\ddagger$ (Å <sup>3</sup> )
E-Tyr 10	Rotating rapidly at all temperatures					
E-Tyr 21	Rotating rapidly at all temperatures					
Tyr 23	<5	$3 \times 10^2$	$5 \times 10^4$	26	35	
Tyr 35	<1	50	$5 \times 10^4$	37	68	60
E-Phe 4	Rotating rapidly at all temperatures					
Phe 22	Rotating rapidly at all temperatures					
Phe 33	Rotating rapidly at all temperatures					
Phe 45	30	$1.7 \times 10^3$	$5 \times 10^4$	17	11	50

From G. Wagner et al., *Biophys. Struct. Mech.* 2:139–159 (1976); *J. Mol. Biol.* 196:227–231 (1987).

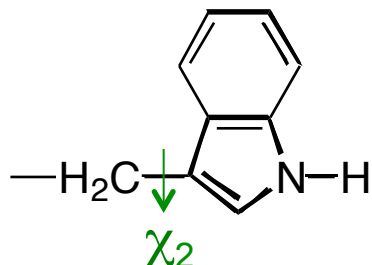
P↑ Flips ↓



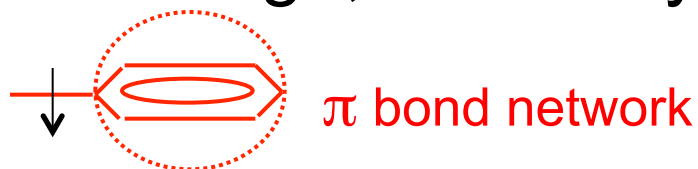
BPTI---Aromatic Groups displayed. Phe in magenta. Tyr in cyan.

# Side Chain Rotations (cont)

- w/ NMR
  - Jumps of 180° flips - not continuous rotation
- Trp usually is immobile - bulky hard to flip



- Y & F - on edge, almost cylindrical shape



- Methyl groups usually have equivalent protons - spinning rapidly

# Side Chain Rotations (cont)

- X-ray crystallography
  - *Smith et al. (1986) Biochem 25:5018*  
4 high resolution Xtal structures
  - Found that 6-13% of the side chains have multiple discrete conformations
    - » Usually on surface
    - » Some inside
  - Preference for discrete substates rather than giving an unresolved continuous smear of electron density but some lack unique conformation

# Side Chain Rotations (cont)

- So, multiple conformational substates sampled @ RT
- Slightly different conformations can perform the same function but @ different rates
- *Frauenfelder et al. Nature 280:559 (1979)*
- *Hong et al. Biophys J. 58:429 (1990)*



## 2 Breathing

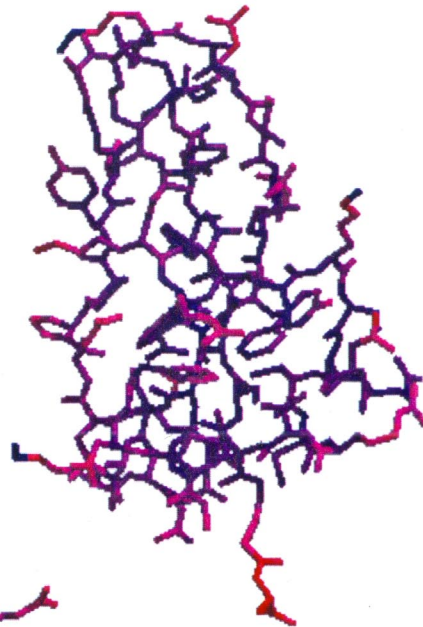
- Crystallography - not just static information
- In addition to position from e<sup>-</sup> density, the spread of the density reflects the mobility of the atoms
- B-factor, B-value, Debye-Waller isotropic temperature factor, temperature factor

$$\langle \Delta x^2 \rangle^{1/2} = (3B/8\pi^2)^{1/2}$$

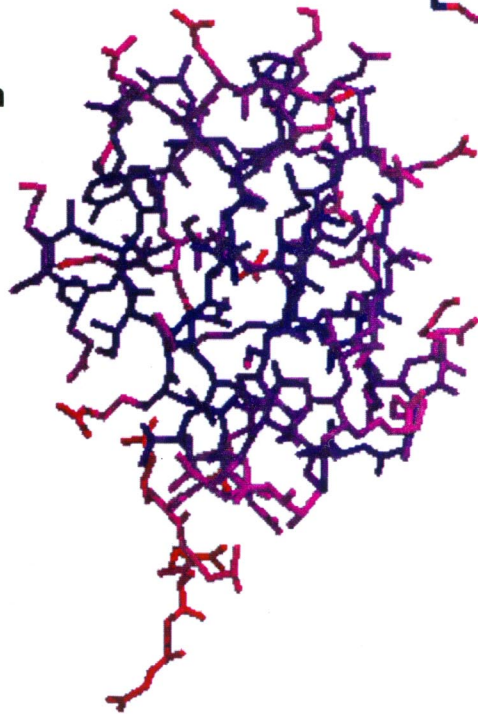
↑ displacement      ↑ B-factor Å<sup>2</sup>      when atoms move they occupy space → spread ↑

- B factors distributed differently along the sequence
  - Lower in core
  - Higher at surface
- Typical values
  - 0.5-0.7 Å for mainchain
  - 0.5-7.0 Å for side chains

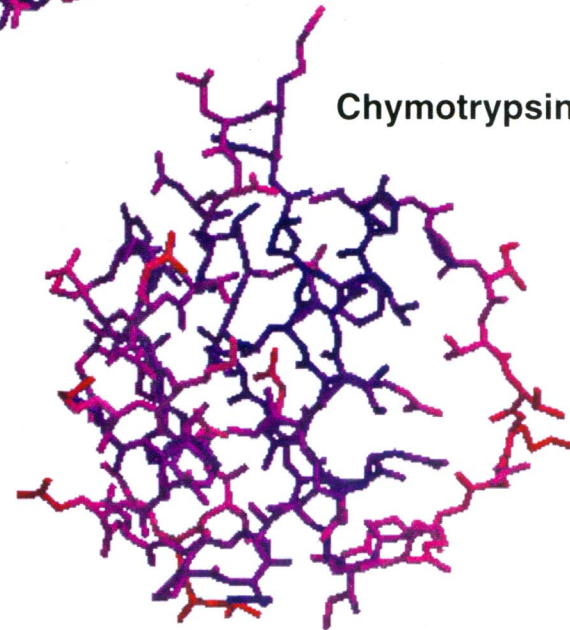
Bovine Pancreatic  
Trypsin Inhibitor



Ubiquitin

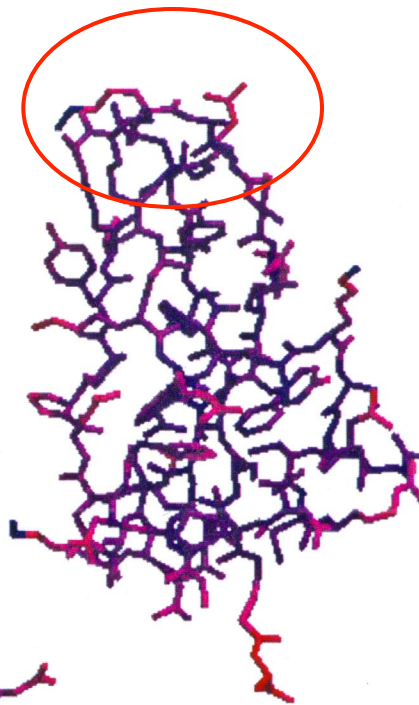


Chymotrypsin Inhibitor 2

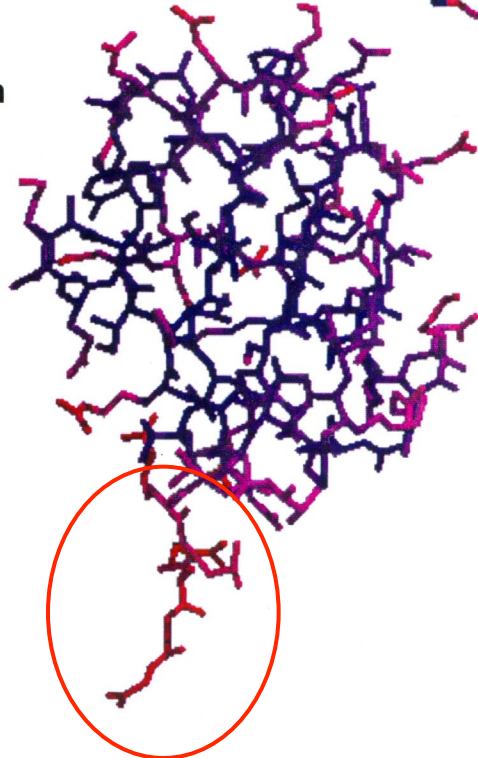


Colored according to B-factors: blue, least mobile, – red, most mobile.

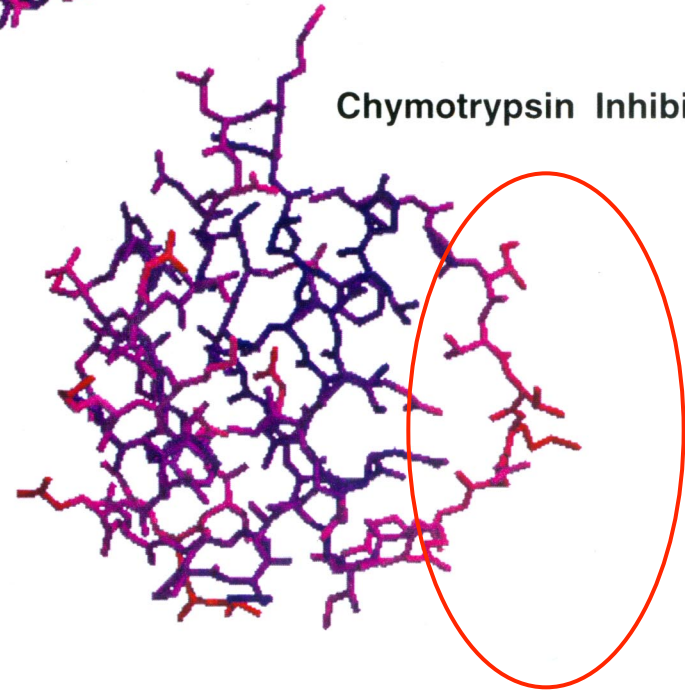
Bovine Pancreatic  
Trypsin Inhibitor



Ubiquitin



Chymotrypsin Inhibitor 2



Colored according to B-factors: blue, least mobile, – red, most mobile.

# CI-2 Free vs. Bound to Subtilisin

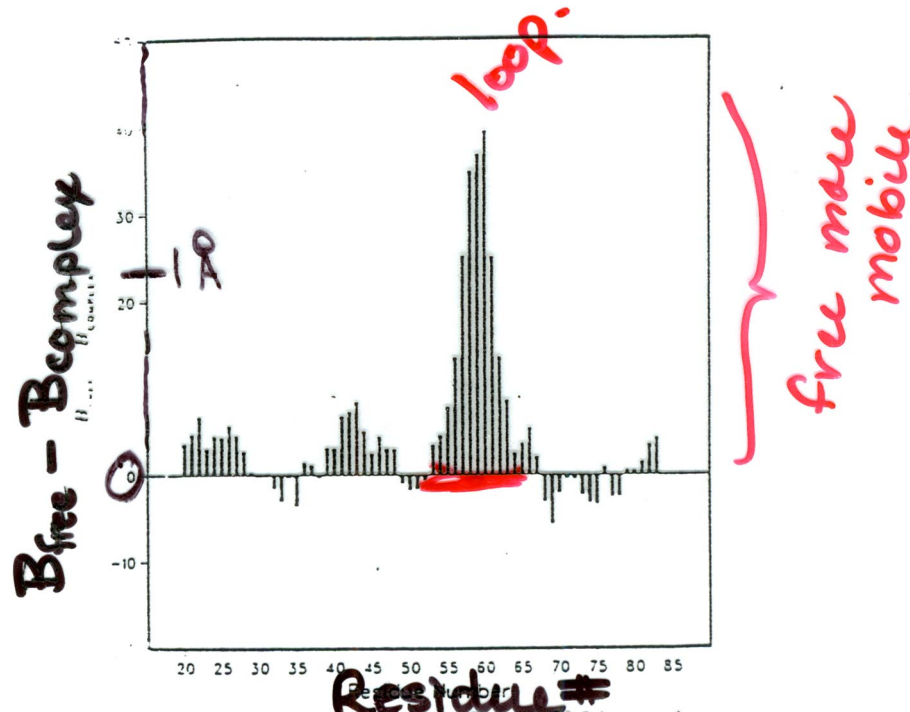


FIGURE 9: Difference  $B$  factor plot, free CI-2 vs. CI-2 in complex. The mean  $B$  factor of the main-chain atoms was calculated for each residue in free CI-2 and CI-2 from the complex with subtilisin Novo. The difference in mean  $B$  factor is plotted vs. residue number. No value is given for Asn-191; no density is seen for this residue in the CI-2 structure from the complex.



# Another Complication

- B-factor
  - Static Xtal Disorder Phase ambiguities, etc. 1
  - Internal Molecular Motion 2

- 1 Should be T independent
- 2 T dependent

- Ribonuclease A      124 aa.
  - Determine B-factors as a function of T  
(98 - 320K)  
(-175° - 47°C)



# of Atoms

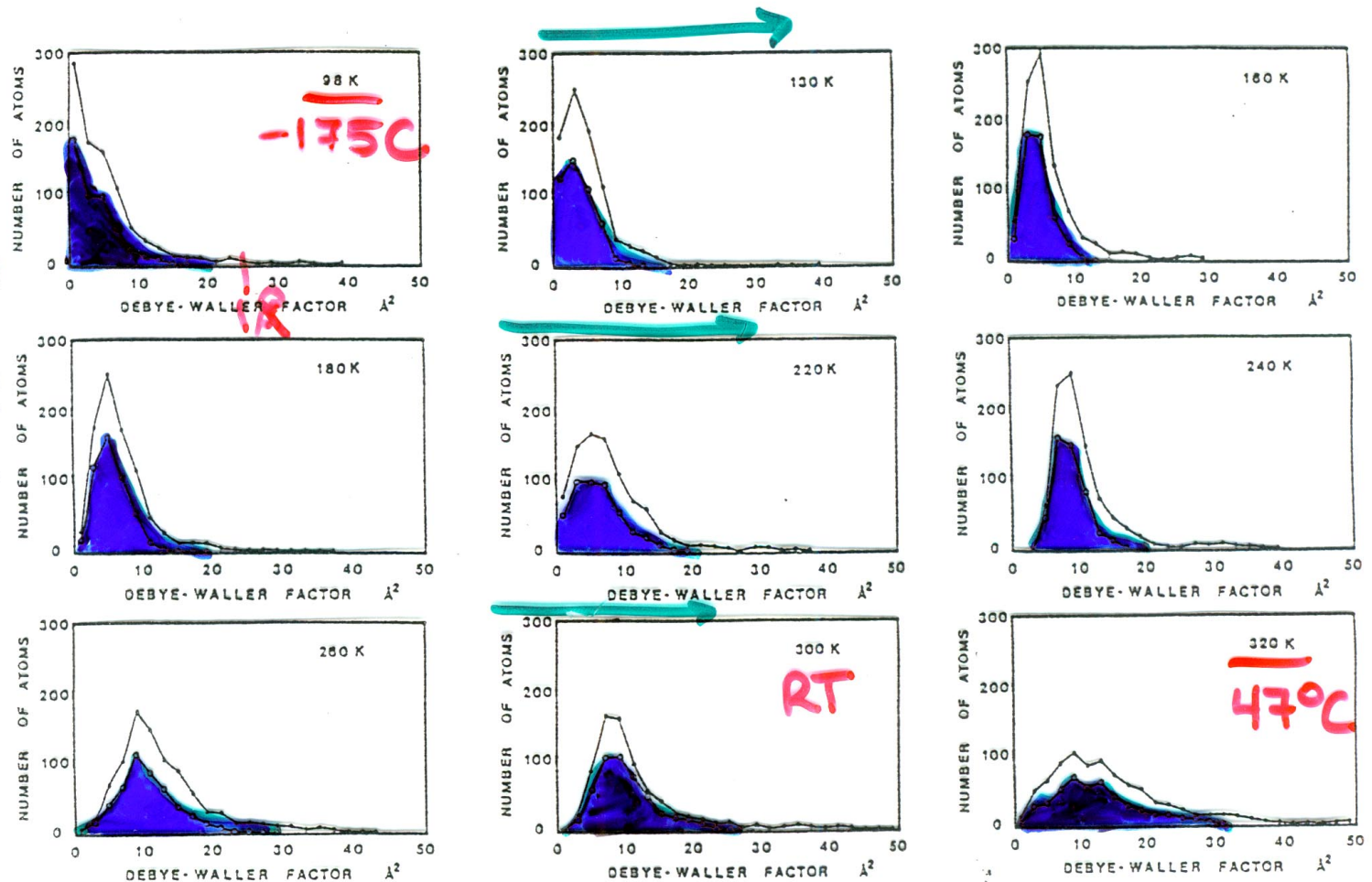


FIGURE 8: Histograms of protein atomic Debye-Waller factors for all atoms (●) and for main-chain atoms (○) at each of the nine temperatures.

**B - Factor ( $\text{\AA}^2$ )**

Tilton, Dewan & Petsko (1992) *Biochem* 31:2469

- Distribution narrow @ low T - harmonic vibration
- Shifts and broadens @ higher T - anharmonic

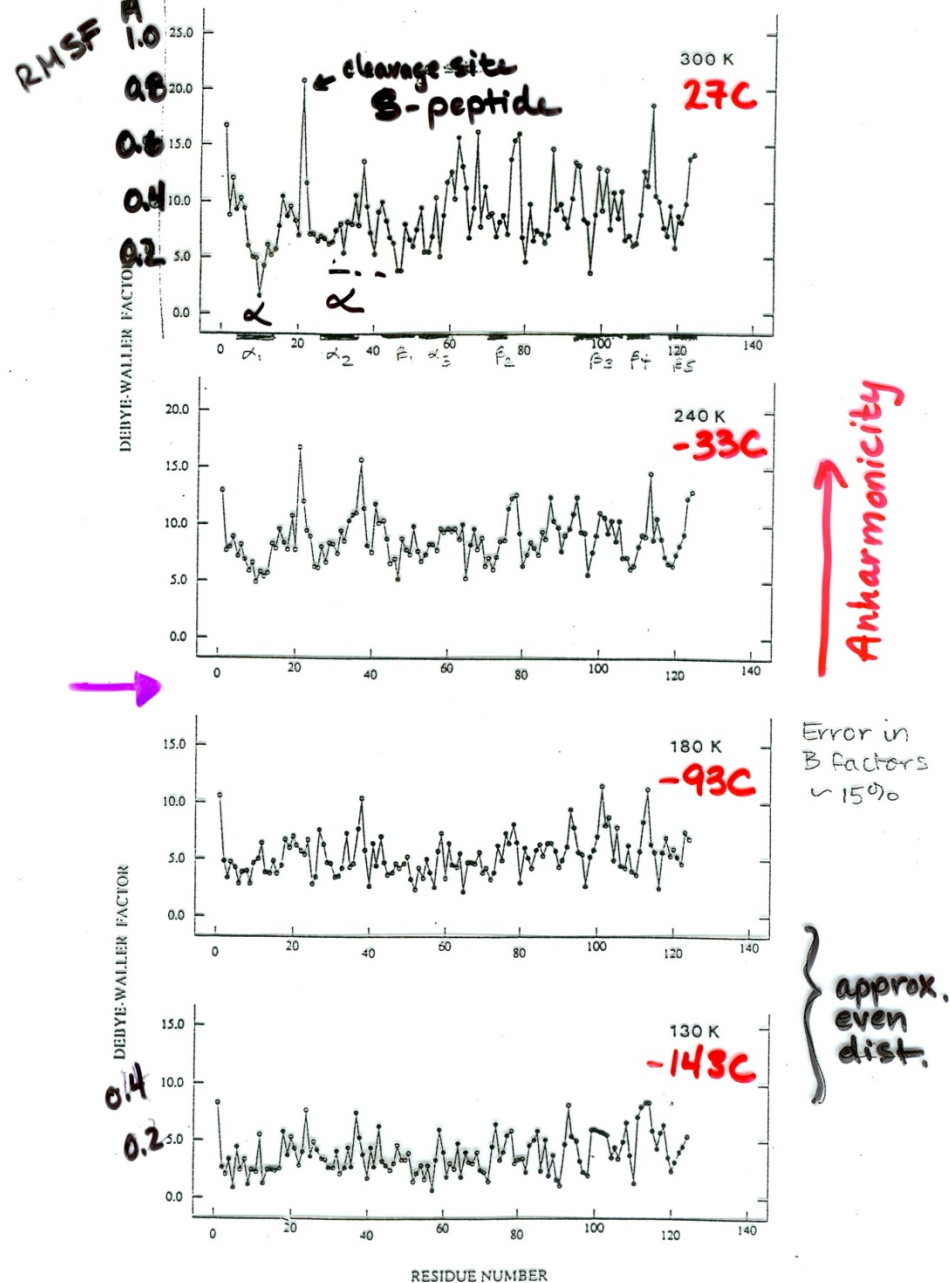
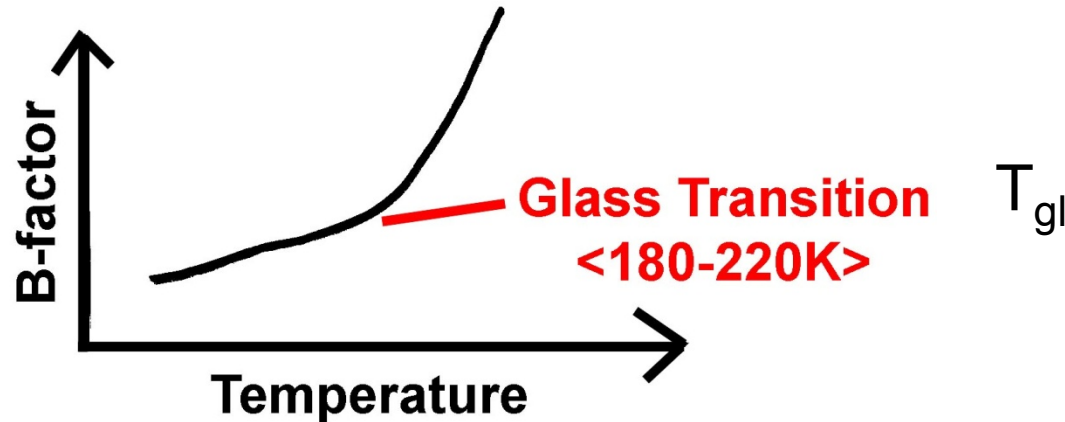


FIGURE 9: Average main-chain (C $\alpha$ , C, N) Debye-Waller factors as a function of residue number for temperatures of 130, 180, 240, and 300 K. An overall increase as well as a greater range in the Debye-Waller factor profile is observed. Residue 21, the site of proteolytic cleavage in the production of ribonuclease-S, has the largest absolute Debye-Waller factor at elevated temperatures and exhibits the greatest temperature sensitivity.

Tilton et al (1992).



# Biphasic Behavior of B w/ T



- Individual amino acids display different behavior w/ T ↑
  - Independent of T
  - Linear change w/ T
  - Different biphasic behavior w/ T (Most)
- Even when protein @ 80K, some atoms retain some ability to move.

# Other findings:

- The smaller the B-factor, the smaller the effective volume
  - » Low B, higher local atomic packing density
- $V_{\text{prot}} \uparrow$  linearly w/  $T \uparrow$
- Greatest motion in turns and loops
  - Correlates with ligand-induced conformational changes
    - »  $\alpha$ -helix and loops
    - » not  $\beta$ -structure

# Link to Function?

- RNase

@ 212K does not bind substrate nor inhibitor (-61°C, below  $T_{gl}$ )

@ 228K - reversible binding (-45°C, above  $T_{gl}$ )

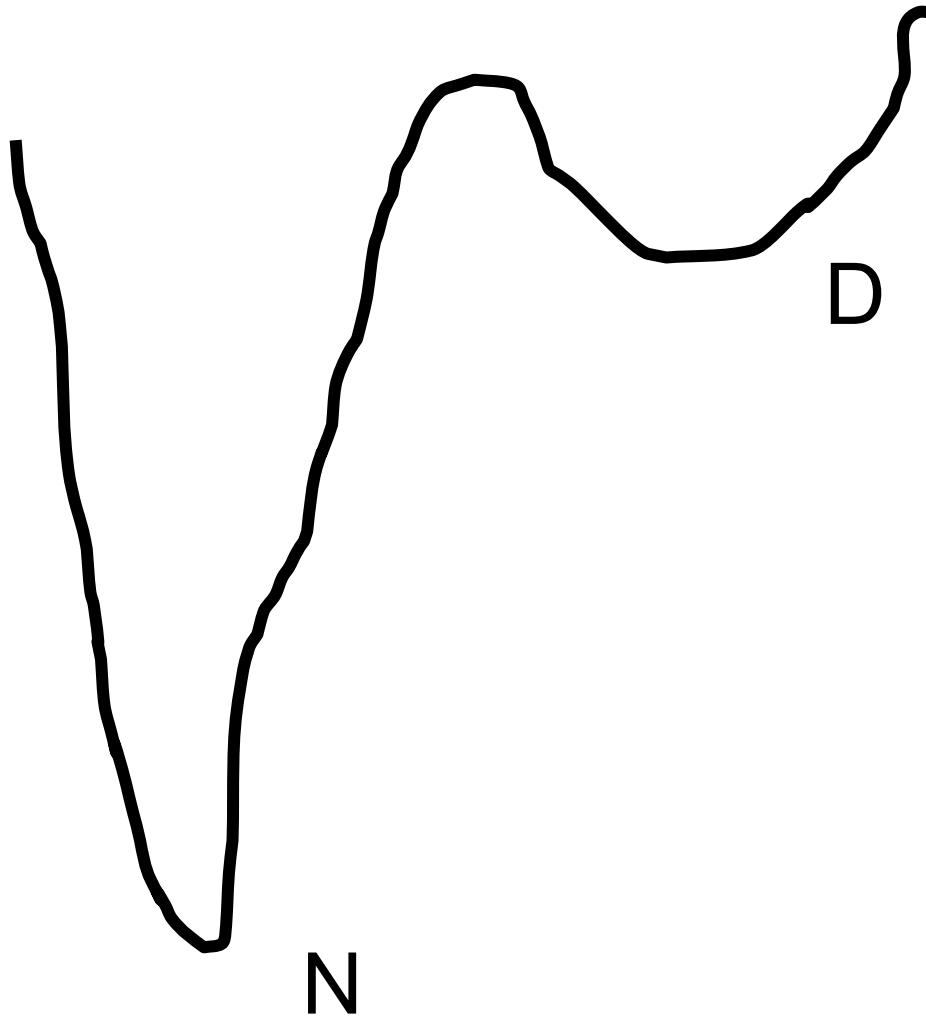
↓ 228K w/ substrate  
cooled to 212K

No longer reversible

∴ flexibility (correlated, anharmonic motion) important for binding and enzymatic activity

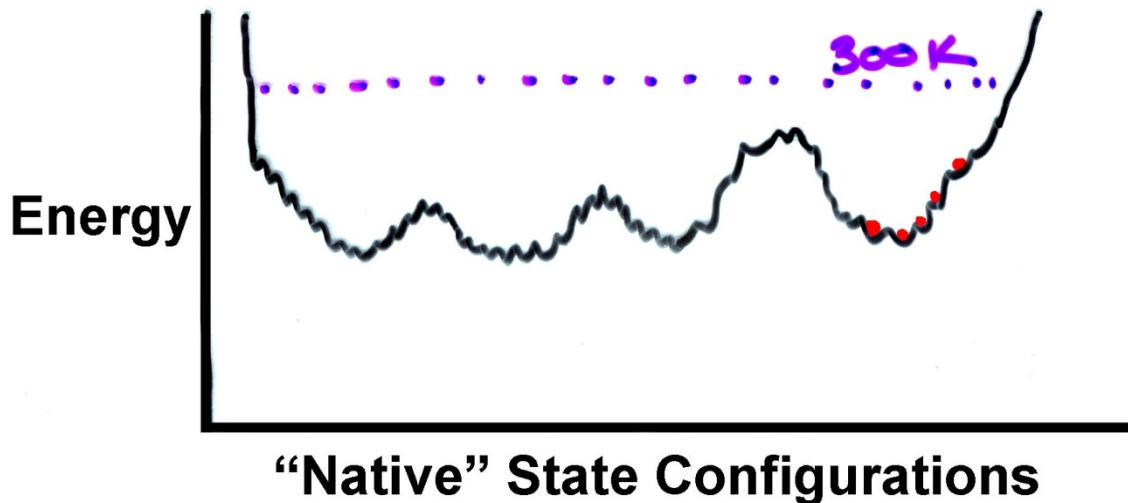
*Petsko and co-workers, Nature 357:423*

# Conformational States



# Conformational Substates

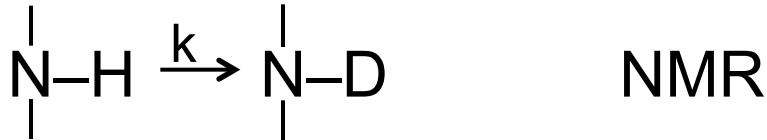
- Below the glass transition, proteins “frozen” into particular conformational states
- At room temperature, proteins rapidly convert between substates



- Low  $T$ ,  $< T_{gl}$ , bond vibrations - local
- Higher  $T$ ,  $> T_{gl}$ , coupled, correlated motion

# Hydrogen Exchange

- Measure rate of exchange



- In general, exposed NH groups exchange rapidly
- Majority of interior NH groups also exchange but more slowly
- 2 Models for slow exchange
  - Solvent Penetration 1
  - Local Unfolding 2
- *Englander & Kallenbach (1984) Quart. Rev. of Biophys. 16:521*

# 1 Support for Penetration Model

- H/D Exchange in crystalline myoglobin using neutron diffraction



- No unfolding occurs, the protein is constrained by the crystal lattice



## 2 Support for Local Unfolding Model

- H/D exchange in the S peptide-S protein complex
- All HN in S peptide exchange at similar rates yet some are buried and some are on the surface
- Local unwinding of helix?
- Re. folding see:  
*Woodward. Curr. Opin. Struct. Biol. 4:112 (1994)*
- Re. sequence effects see:  
*Englander, Proteins, 17: 75, 87 (1993)*

# NMR

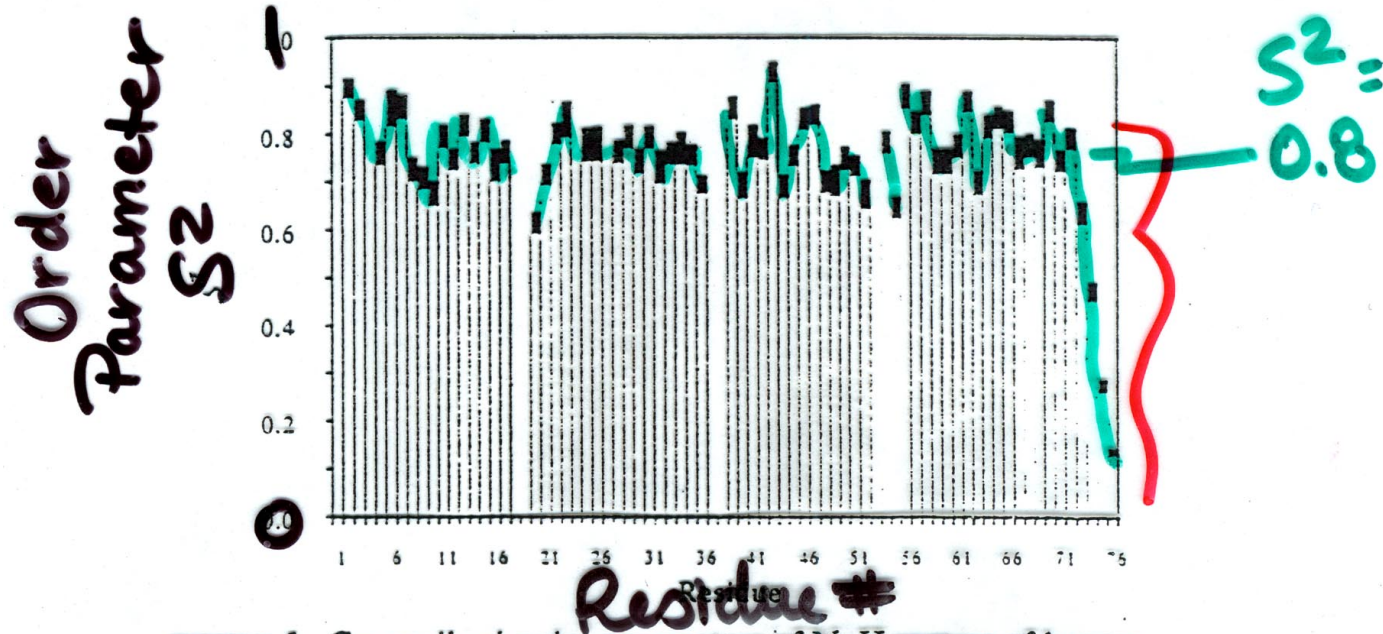
- Advantages
  - In solution
  - Sensitive to time scale & magnitude of motion
- Relaxation Experiments

*See Wagner (1993) Curr Opin Struct Biol 3:748*

$\xrightarrow{\text{model free approach}}$   $S^2$  generalized order parameters

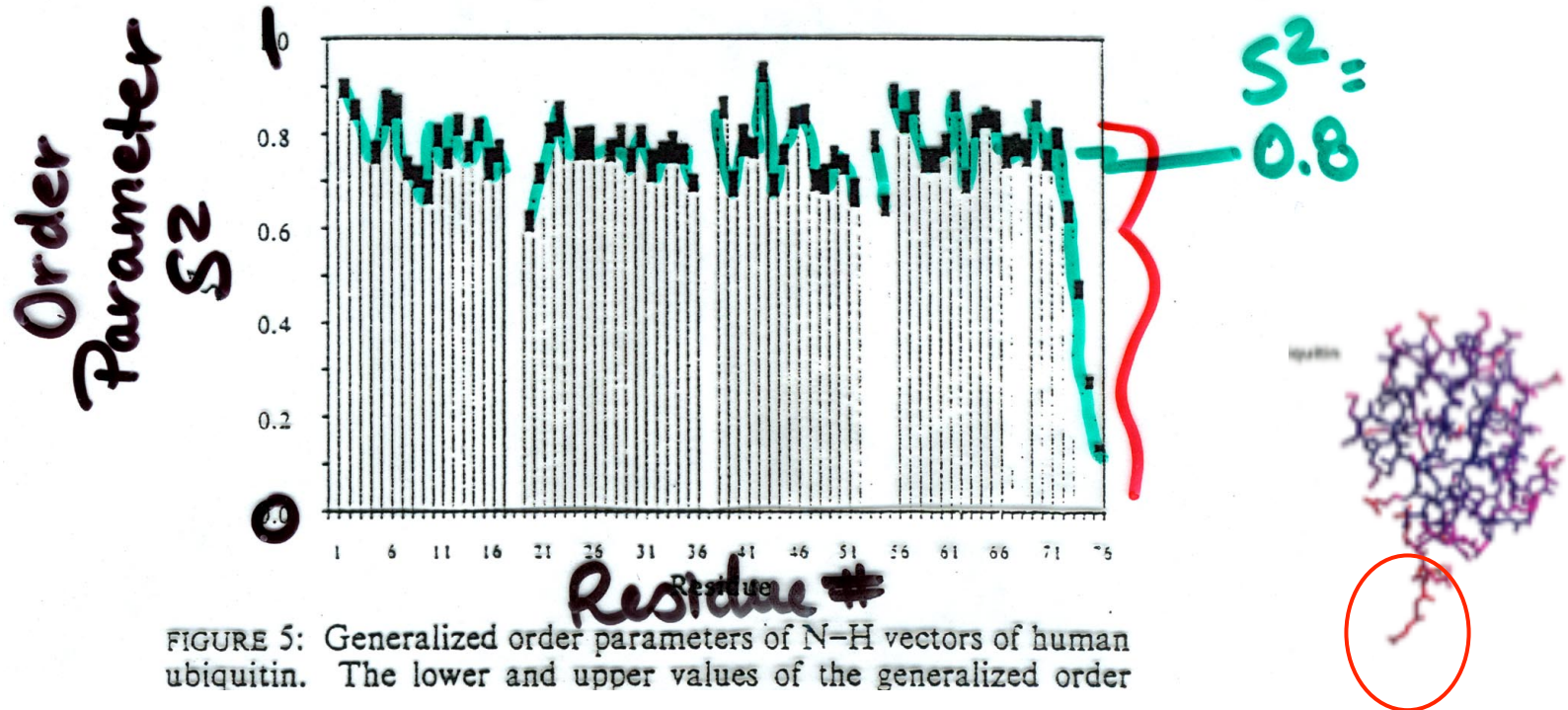
- Extent of angular motion
  - $S^2 = 0$  freely rotating bond
  - $S^2 = 1$  totally rigid
- Also, effective correlation time,  $\tau_e$  for reorientation of vector
- For methyl groups in BPTI  $\tau_e = 19\text{-}70$  ps  
 $S^2 = 0.6$

# Main Chain Dynamics of Ubiquitin



- $S^2$  not correlated w/  $2^\circ$  structure
- Correlated w/ HB e.g. when Hbonds formed  $\sim 0.8$ , when no HB  $S^2 \sim 0.6$
- Correlation time  $< 150\text{ps}$  (still fast, slower than Me)
- *Schneider, Dellwo & Wood (1992) Biochem 31:3645*

# Main Chain Dynamics of Ubiquitin



- $S^2$  not correlated w/  $2^\circ$  structure
- Correlated w/ HB e.g. when Hbonds formed  $\sim 0.8$ , when no HB  $S^2 \sim 0.6$
- Correlation time  $< 150\text{ps}$  (still fast, slower than Me)
- *Schneider, Dellwo & Wood (1992) Biochem 31:3645*

## 3

# Relative Motion

- X-ray

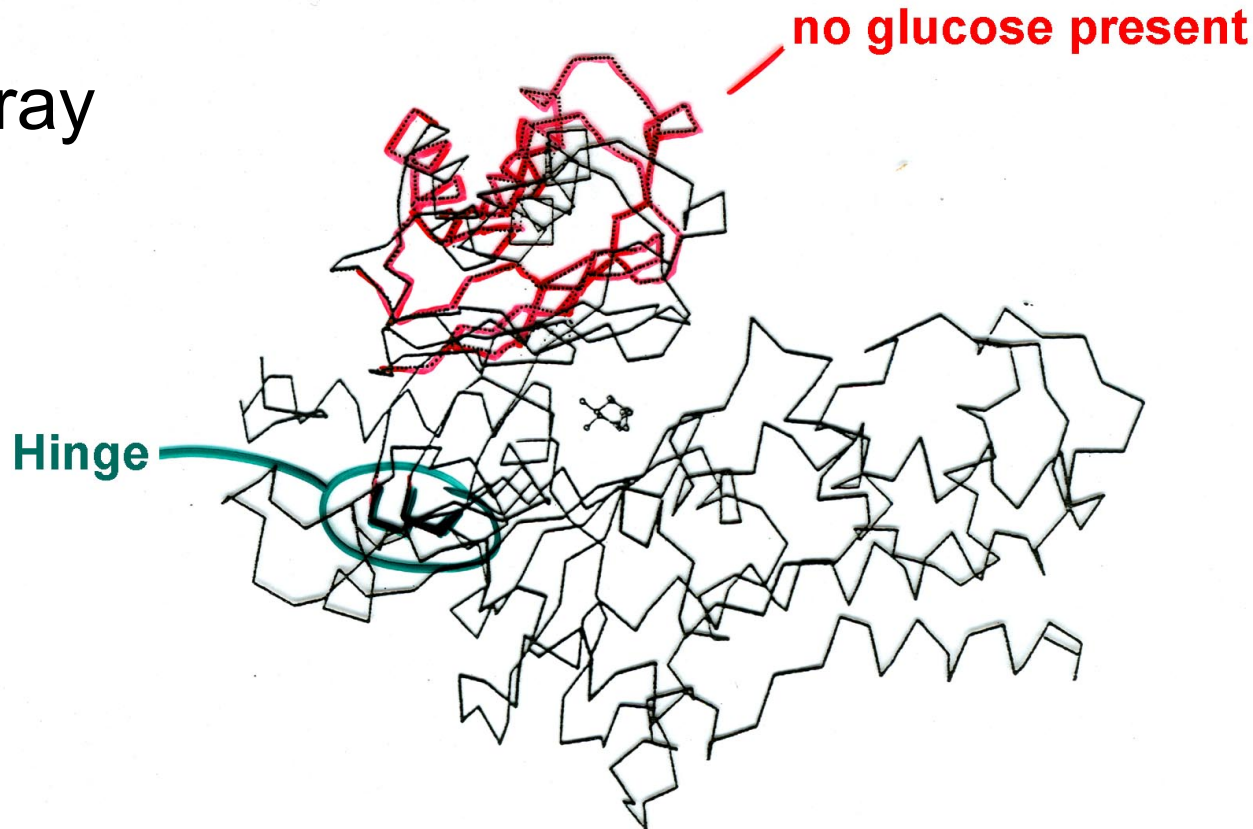


FIGURE 12-13. The conformational changes induced in hexokinase by glucose binding. The solid lines show the  $\alpha$ -carbon backbone of the A isozyme crystallized in the presence of glucose. The dotted lines show the backbone of the part of the B isozyme that has a different structure when crystallization occurs in the absence of glucose. [From W. S. Bennett and T. A. Steitz, *Fedn. Proc. Abstr.* (1977).]

- Conformational Changes in Hexokinase



# Theory

- Experiment clearly demonstrates that proteins are mobile, but no single experiment or combination of experiments can provide an all-inclusive view of the dynamic behavior of all atoms in a protein.
- Computer simulations can however
  - ea. atom as a function of time
- *Review: Karplus & Petsko (1990) Nature 347:631*



# Why Molecular Dynamics?

- System Size:  $n$ =# of atoms
  - Ab initio QM  $n^4$
  - Semiempirical QM  $n^3$
  - MM/Empirical force field methods  $n^2$ , or  $n$  w/ truncation
- Most realistic simulation method available
- Can provide structural and dynamic information unobtainable by experiment, but is experimentally testable
- 4<sup>th</sup> dimension to PDB, 3D structures moving through time

## But

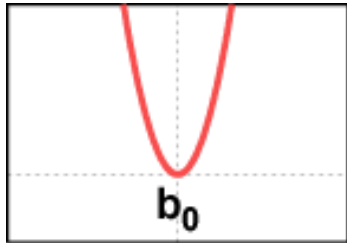
- Sampling is limited, the goal is to sample experimentally relevant regions of conformational space, not all of conformational space



# Methods

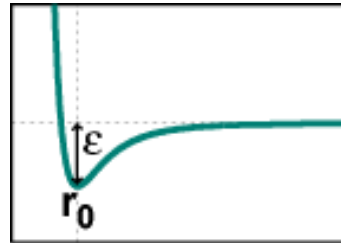
- Molecular mechanics force field

$$U = \text{Bond} + \text{Angle} + \text{Dihedral} + \text{van der Waals} + \text{Electrostatic}$$



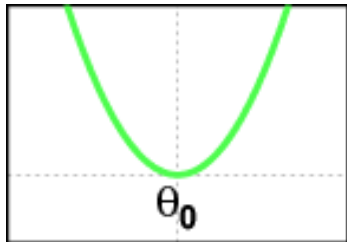
**Bond**

$$\sum_i^{\text{bonds}} K_{b,i} (b_i - b_{0,i})^2$$



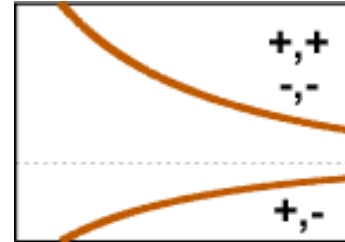
**van der Waals**

$$\sum_{\text{pairs } i,j} \left[ \epsilon_{ij} \left( \frac{r_{0,ij}}{r_{ij}} \right)^{12} - 2\epsilon_{ij} \left( \frac{r_{0,ij}}{r_{ij}} \right)^6 \right]$$



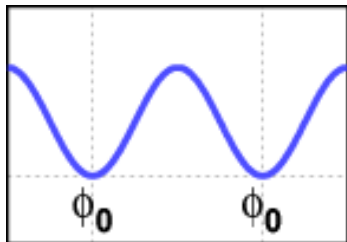
**Angle**

$$\sum_i^{\text{bond angles}} K_{\theta,i} (\theta_i - \theta_{0,i})^2$$



**Electrostatic**

$$332 \sum_{\text{pairs } i,j} \left( \frac{q_i q_j}{r_{ij}} \right)$$



**Dihedral**

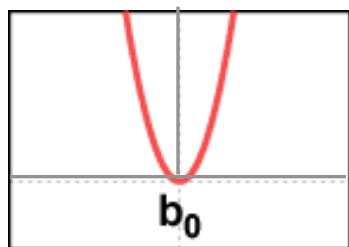
$$\sum_i^{\text{torsion angles}} K_{\phi,i} \{1 - \cos[n_i (\phi_i - \phi_{0,i})]\}$$

Levitt, Sharon, Hirshberg,  
& Daggett, 1995, *J. Comp. Phys.*  
Water Model: *J Phys Chem*, 1997

# Molecular Dynamics

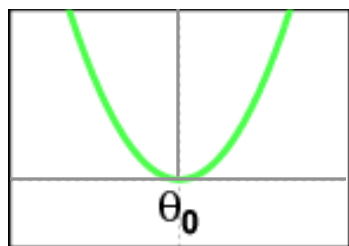
- Potential function for MD<sup>1,2</sup>

$$U = \text{Bond} + \text{Angle} + \text{Dihedral}$$



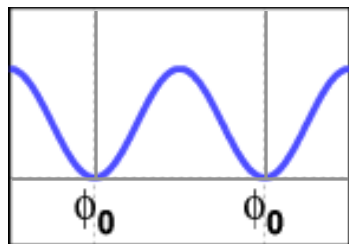
**Bond**

$$\sum_i^{\text{bonds}} K_{b,i} (b_i - b_{0,i})^2$$



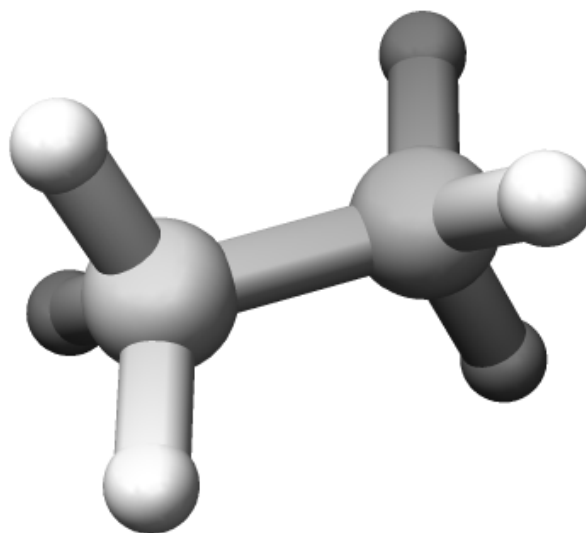
**Angle**

$$\sum_i^{\text{bond angles}} K_{\theta,i} (\theta_i - \theta_{0,i})^2$$



**Dihedral**

$$\sum_i^{\text{torsion angles}} K_{\phi,i} \{1 - \cos[n_i (\phi_i - \phi_{0,i})]\}$$

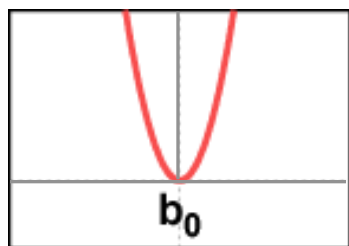


1. Levitt M. Hirshberg M. Sharon R. Daggett V. Comp. Phys. Comm. (1995) 91: 215-231
2. Levitt M. *et al.* J. Phys. Chem. B (1997) 101: 5051-5061

# Molecular Dynamics

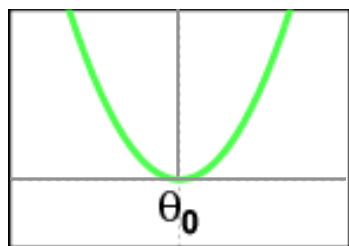
- Potential function for MD<sup>1,2</sup>

$U = \text{Bond} + \text{Angle} + \text{Dihedral} + \text{van der Waals} +$



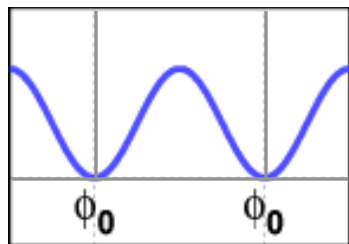
**Bond**

$$\sum_i^{\text{bonds}} K_{b,i} (b_i - b_{0,i})^2$$



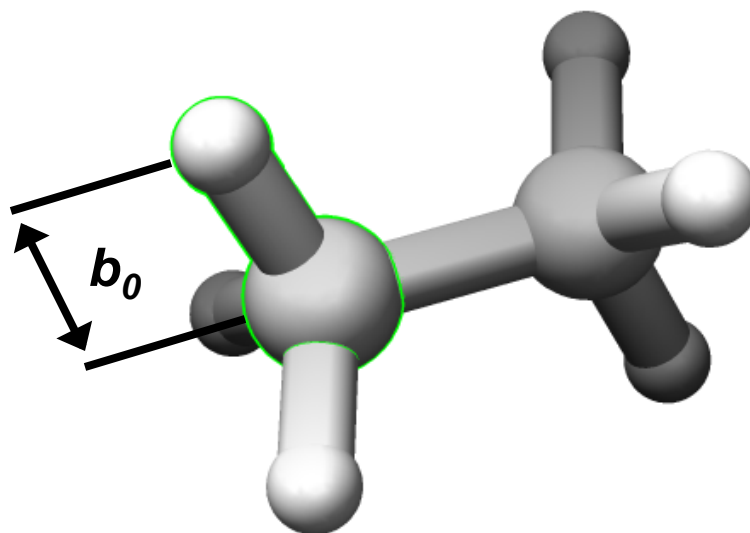
**Angle**

$$\sum_i^{\text{bond angles}} K_{\theta,i} (\theta_i - \theta_{0,i})^2$$



**Dihedral**

$$\sum_i^{\text{torsion angles}} K_{\phi,i} \{1 - \cos[n_i (\phi_i - \phi_{0,i})]\}$$

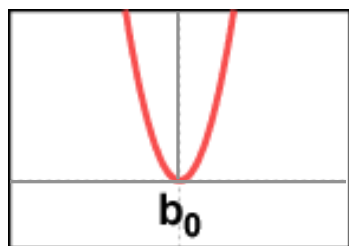


- Levitt M. Hirshberg M. Sharon R. Daggett V. Comp. Phys. Comm. (1995) 91: 215-231
- Levitt M. *et al.* J. Phys. Chem. B (1997) 101: 5051-5061

# Molecular Dynamics

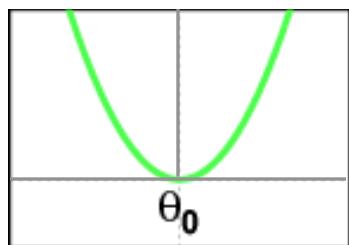
- Potential function for MD<sup>1,2</sup>

$U = \text{Bond} + \text{Angle} + \text{Dihedral} + \text{van der Waals} +$



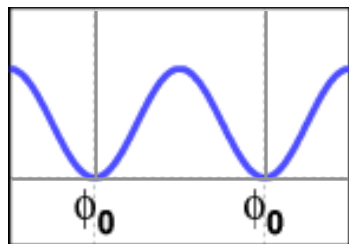
**Bond**

$$\sum_i^{\text{bonds}} K_{b,i} (b_i - b_{0,i})^2$$



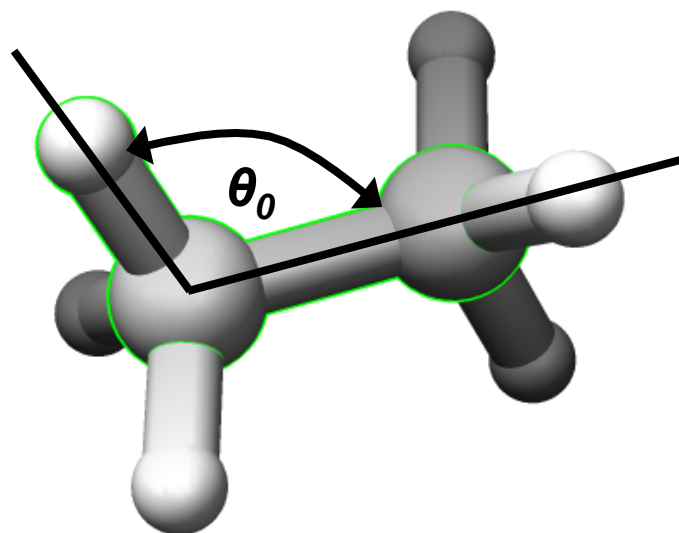
**Angle**

$$\sum_i^{\text{bond angles}} K_{\theta,i} (\theta_i - \theta_{0,i})^2$$



**Dihedral**

$$\sum_i^{\text{torsion angles}} K_{\phi,i} \{1 - \cos[n_i (\phi_i - \phi_{0,i})]\}$$



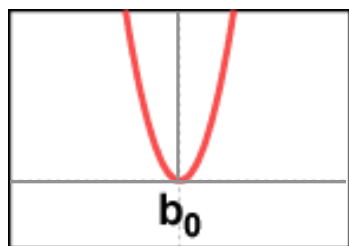
1. Levitt M. Hirshberg M. Sharon R. Daggett V. Comp. Phys. Comm. (1995) 91: 215-231

2. Levitt M. *et al.* J. Phys. Chem. B (1997) 101: 5051-5061

# Molecular Dynamics

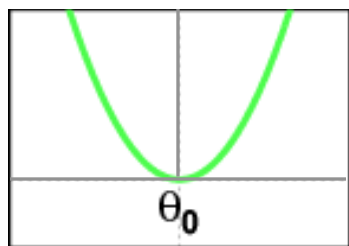
- Potential function for MD<sup>1,2</sup>

$U = \text{Bond} + \text{Angle} + \text{Dihedral} + \text{van der Waals} +$



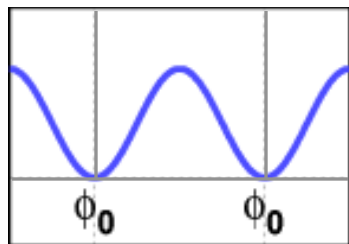
**Bond**

$$\sum_i^{\text{bonds}} K_{b,i} (b_i - b_{0,i})^2$$



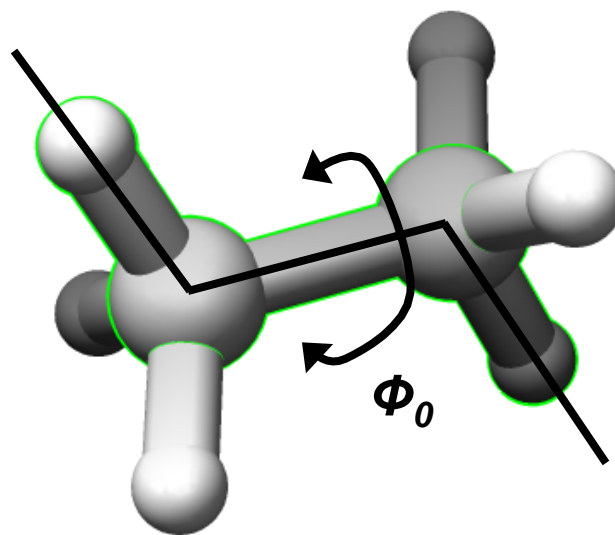
**Angle**

$$\sum_i^{\text{bond angles}} K_{\theta,i} (\theta_i - \theta_{0,i})^2$$



**Dihedral**

$$\sum_i^{\text{torsion angles}} K_{\phi,i} \{1 - \cos[n_i (\phi_i - \phi_{0,i})]\}$$



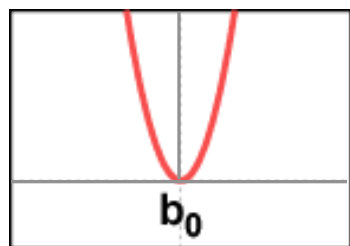
1. Levitt M. Hirshberg M. Sharon R. Daggett V. Comp. Phys. Comm. (1995) 91 215-231

2. Levitt M. *et al.* J. Phys. Chem. B (1997) 101:25 5051-5061

# Molecular Dynamics

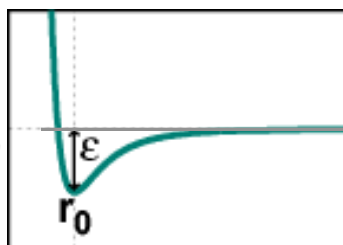
- Potential function for MD<sup>1,2</sup>

$$U = \text{Bond} + \text{Angle} + \text{Dihedral} + \text{vdW} + \text{Electrostatic}$$



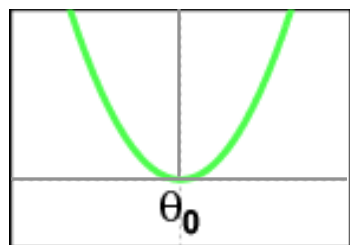
**Bond**

$$\sum_i^{\text{bonds}} K_{b,i} (b_i - b_{0,i})^2$$



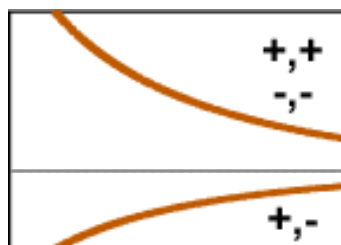
**van der Waals**

$$\sum_{\text{pairs } i,j} \left[ \epsilon_{ij} \left( \frac{r_{0,ij}}{r_{ij}} \right)^{12} - 2\epsilon_{ij} \left( \frac{r_{0,ij}}{r_{ij}} \right)^6 \right]$$



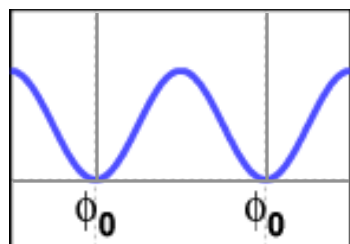
**Angle**

$$\sum_i^{\text{bond angles}} K_{\theta,i} (\theta_i - \theta_{0,i})^2$$



**Electrostatic**

$$332 \sum_{\text{pairs } i,j} \left( \frac{q_i q_j}{r_{ij}} \right)$$



**Dihedral**

$$\sum_i^{\text{torsion angles}} K_{\phi,i} \{1 - \cos[n_i (\phi_i - \phi_{0,i})]\}$$

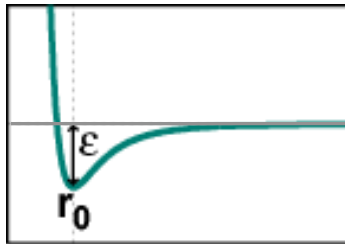
1. Levitt M. Hirshberg M. Sharon R. Daggett V. Comp. Phys. Comm. (1995) 91: 215-231

2. Levitt M. *et al.* J. Phys. Chem. B (1997) 101: 5051-5061

# Molecular Dynamics

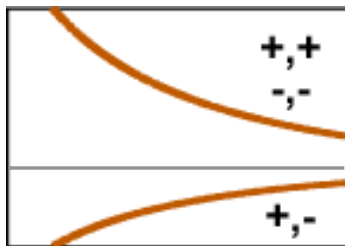
- Non-bonded components of potential function

$$U_{nb} = \text{van der Waals} + \text{Electrostatic}$$



van der Waals

$$\sum_{\text{pairs } i,j} \left[ \epsilon_{ij} \left( \frac{r_{0,ij}}{r_{ij}} \right)^{12} - 2\epsilon_{ij} \left( \frac{r_{0,ij}}{r_{ij}} \right)^6 \right]$$



Electrostatic

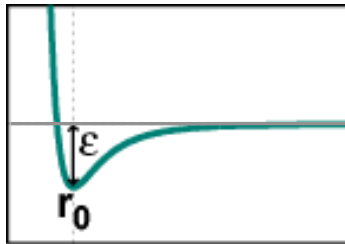
$$\frac{1}{4\pi\epsilon_0} \sum_{\text{pairs } i,j} \left( \frac{q_i q_j}{r_{ij}} \right)$$

- *To a large degree, protein structure is dependent on non-bonded atomic interactions*

# Molecular Dynamics

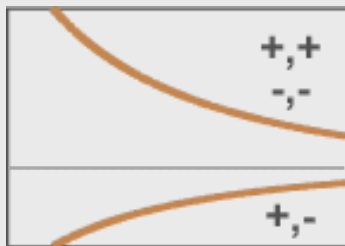
- Non-bonded components of potential function

$U_{nb}$  = van der Waals + Electrostatic



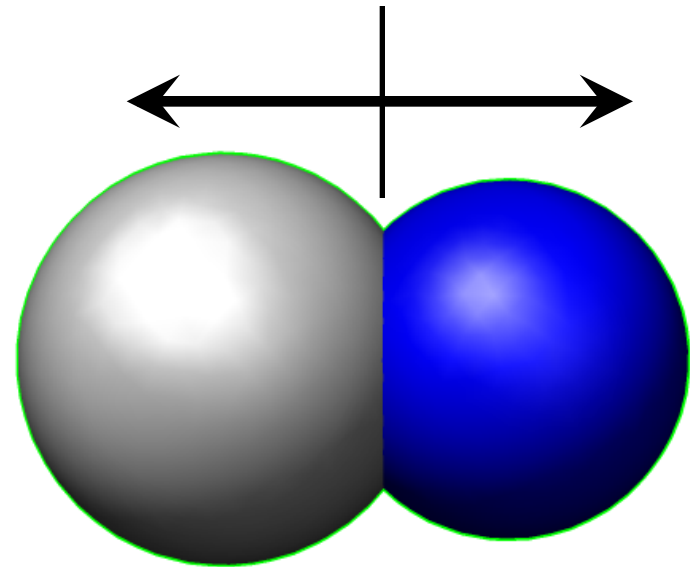
van der Waals

$$\sum_{pairs\ i,j} \left[ \epsilon_{ij} \left( \frac{r_{0,ij}}{r_{ij}} \right)^{12} - 2\epsilon_{ij} \left( \frac{r_{0,ij}}{r_{ij}} \right)^6 \right]$$



Electrostatic

$$\sum_{pairs\ i,j} \left( \frac{q_i q_j}{r_{ij}} \right)$$

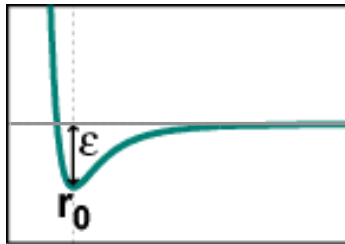




# Molecular Dynamics

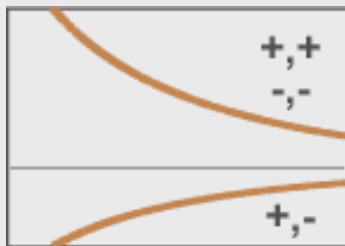
- Non-bonded components of potential function

$$U_{nh} = \text{van der Waals} + \text{Electrostatic}$$



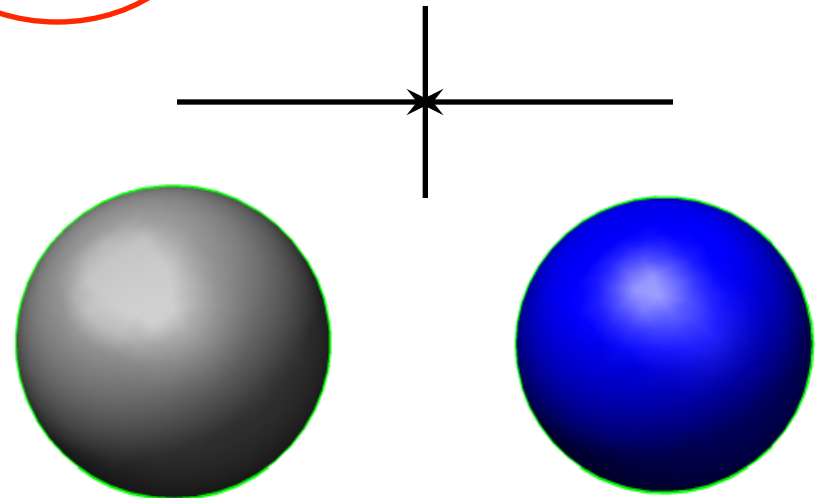
van der Waals

$$\sum_{\text{pairs } i,j} \left[ \epsilon_{ij} \left( \frac{r_{0,ij}}{r_{ij}} \right)^{12} - 2\epsilon_{ij} \left( \frac{r_{0,ij}}{r_{ij}} \right)^6 \right]$$



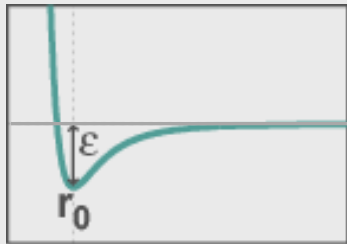
Electrostatic

$$\frac{1}{4\pi\epsilon_0} \sum_{\text{pairs } i,j} \left( \frac{q_i q_j}{r_{ij}} \right)$$



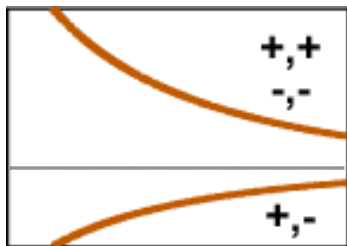
# Molecular Dynamics

- Non-bonded components of potential function



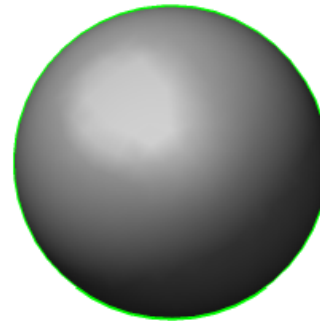
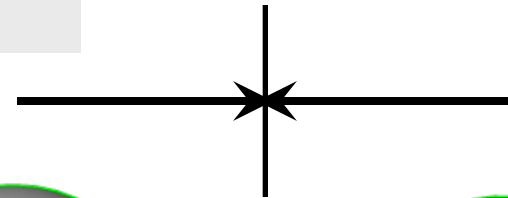
van der Waals

$$\sum_{pairs\cdot i,j} \left[ \epsilon_{ij} \left( \frac{r_{0,ij}}{r_{ij}} \right)^{12} - 2\epsilon_{ij} \left( \frac{r_{0,ij}}{r_{ij}} \right)^6 \right]$$



Electrostatic

$$332 \sum_{pairs\cdot i,j} \left( \frac{q_i q_j}{r_{ij}} \right)$$



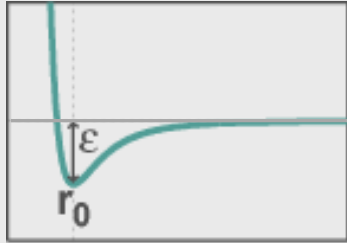
+



-

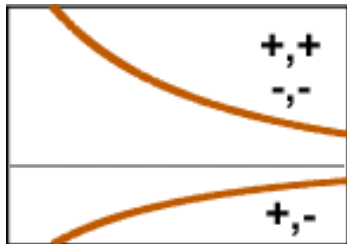
# Molecular Dynamics

- Non-bonded components of potential function



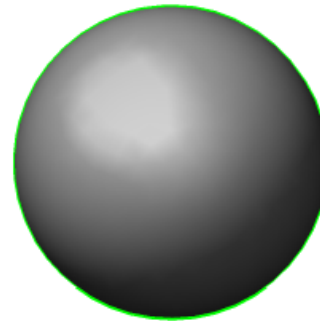
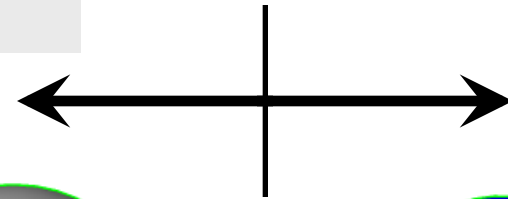
van der Waals

$$\sum_{\text{pairs } i,j} \left[ \epsilon_{ij} \left( \frac{r_{0,ij}}{r_{ij}} \right)^{12} - 2\epsilon_{ij} \left( \frac{r_{0,ij}}{r_{ij}} \right)^6 \right]$$

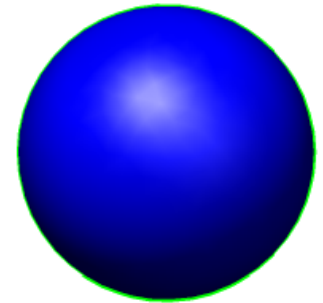


Electrostatic

$$332 \sum_{\text{pairs } i,j} \left( \frac{q_i q_j}{r_{ij}} \right)$$



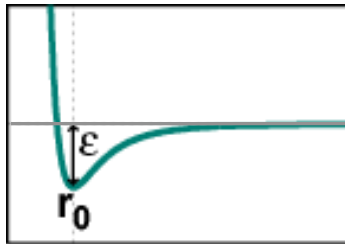
+



+

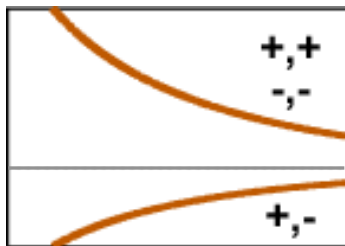
# Molecular Dynamics

- Non-bonded components of potential function



van der Waals

$$\sum_{pairs\cdot i,j} \left[ \epsilon_{ij} \left( \frac{r_{0,ij}}{r_{ij}} \right)^{12} - 2\epsilon_{ij} \left( \frac{r_{0,ij}}{r_{ij}} \right)^6 \right]$$



Electrostatic

$$\sum_{pairs\cdot i,j} \left( \frac{q_i q_j}{r_{ij}} \right)$$

**NOTE:**

Sum over all pairs of N atoms, or

$$\frac{N * N - 1}{2} \text{ pairs}$$

**N is often between  $5 \times 10^5$  to  $5 \times 10^6$**

**For  $5 \times 10^5$  that is  $1.25 \times 10^{11}$  pairs**

**THAT IS A LOT OF POSSIBLE PAIRS!**

# **What can you do with a force field?**

- Relax your structure
- Refine your structure
- Determine your structure
- Score structures
- Etc.

# Methods

- **Molecular dynamics (MD)**
  - time dependent integration of classical equations of motion

$$F = -\frac{\partial U}{\partial x}$$

$$F = ma$$

$$a = \frac{v_2 - v_1}{\partial t}$$

$$v = \frac{x_2 - x_1}{\partial t}$$

$$\partial t = 2 \text{ fs}$$

# Methods

- Molecular dynamics (MD)

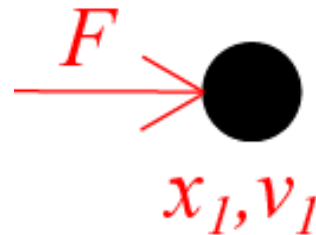
$$F = -\frac{\partial U}{\partial x}$$

$$F = ma$$

$$a = \frac{v_2 - v_1}{\partial t}$$

$$v = \frac{x_2 - x_1}{\partial t}$$

$$\partial t = 2 \text{ fs}$$



# Methods

- Molecular dynamics (MD)

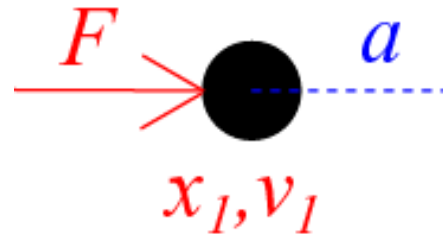
$$F = -\frac{\partial U}{\partial x}$$

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$$v = \frac{x_2 - x_1}{\partial t}$$

$$\partial t = 2 \text{ fs}$$





# Methods

- Molecular dynamics (MD)

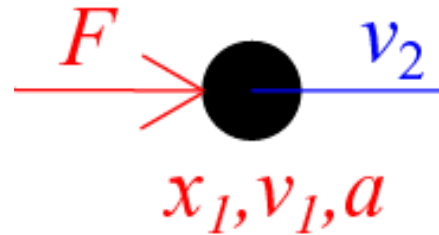
$$F = -\frac{\partial U}{\partial x}$$

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# Methods

- Molecular dynamics (MD)

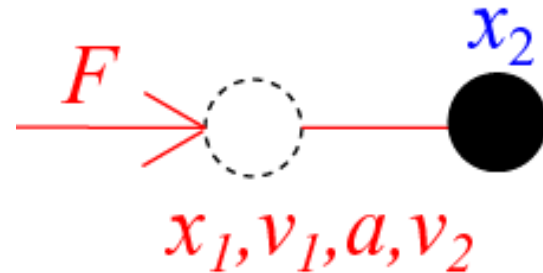
$$F = -\frac{\partial U}{\partial x}$$

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$$a = \frac{v_2 - v_1}{\partial t}$$

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$$\partial t = 2 \text{ fs}$$



# Methods

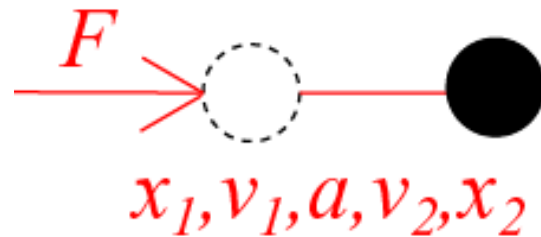
- Molecular dynamics (MD)

$$F = -\frac{\partial U}{\partial x}$$

$$F = ma$$

$$a = \frac{v_2 - v_1}{\partial t}$$

$$v = \frac{x_2 - x_1}{\partial t}$$



$$\partial t = 2 \text{ fs}$$

# Methods

- **Molecular dynamics (MD)**

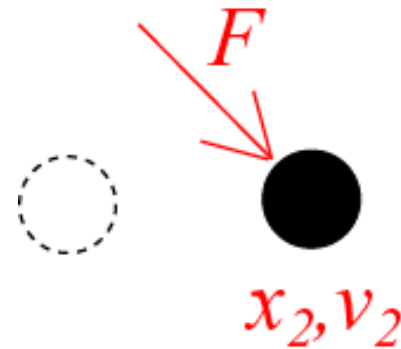
$$F = -\frac{\partial U}{\partial x}$$

$$F = ma$$

$$a = \frac{v_3 - v_2}{\partial t}$$

$$v = \frac{x_3 - x_2}{\partial t}$$

$$\partial t = 2 \text{ fs}$$



**Do it all over again and again and again**

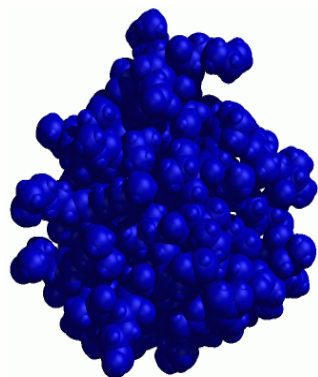
**50,000 atoms, each ps involves  
25,000,000 evaluations**

**20 ns (20,000 ps) requires  
 $5 \times 10^{11}$  evaluations**

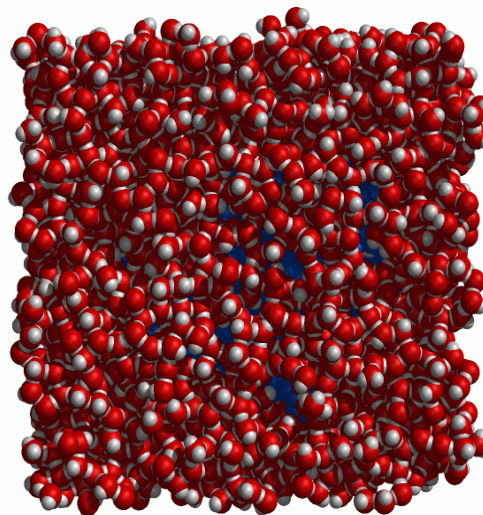
# Starting a Molecular Dynamics Simulation



Solvate with  
water or  
other solvent  
8 - 14 Å  
from protein

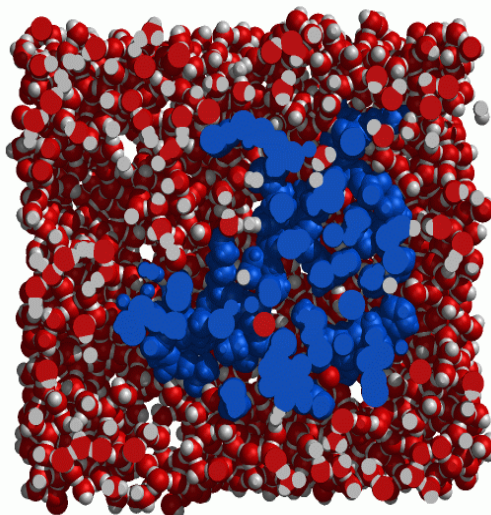


Crystal or  
NMR Structure



Heat to desired  
temperature and  
allow motion to  
evolve over time

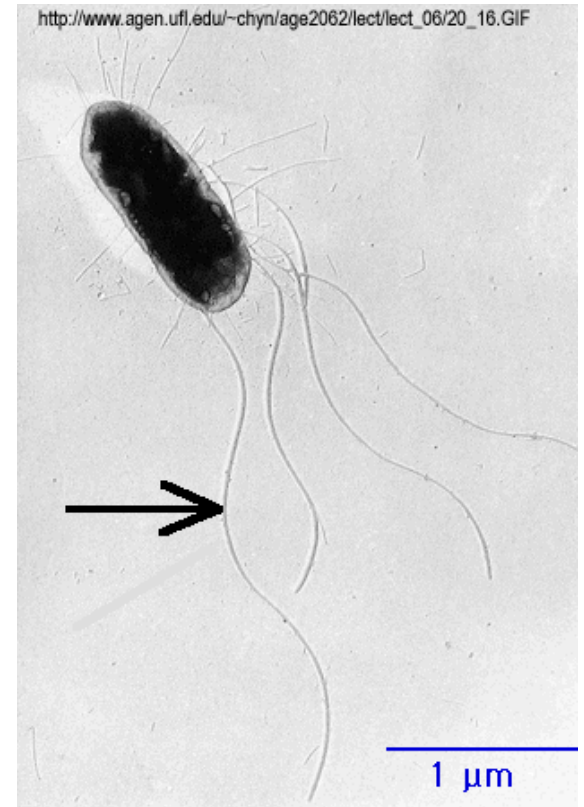
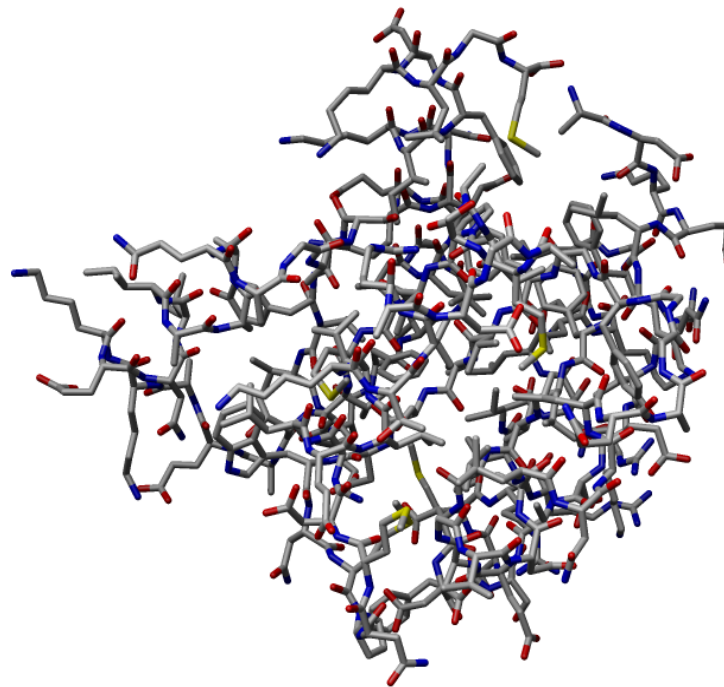
$T = 25\text{ }^{\circ}\text{C}$   
 $\rho = 0.997\text{ gm/ml}$



$T = 60\text{ }^{\circ}\text{C}$   
 $\rho = 0.983\text{ gm/ml}$

# Molecular Dynamics

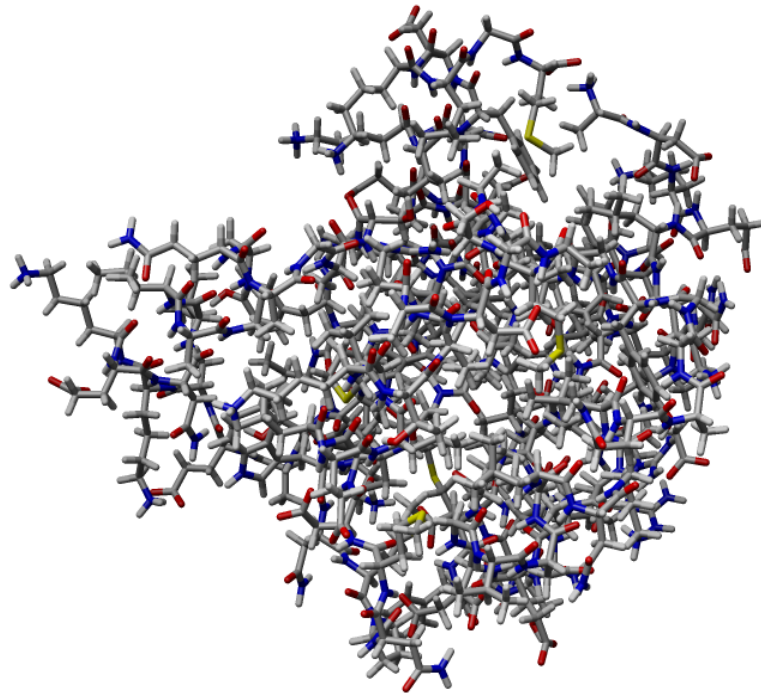
- MD provides atomic resolution of native dynamics



PDB ID: 3chy, *E. coli* CheY 1.66 Å X-ray crystallography

# Molecular Dynamics

- MD provides atomic resolution of native dynamics

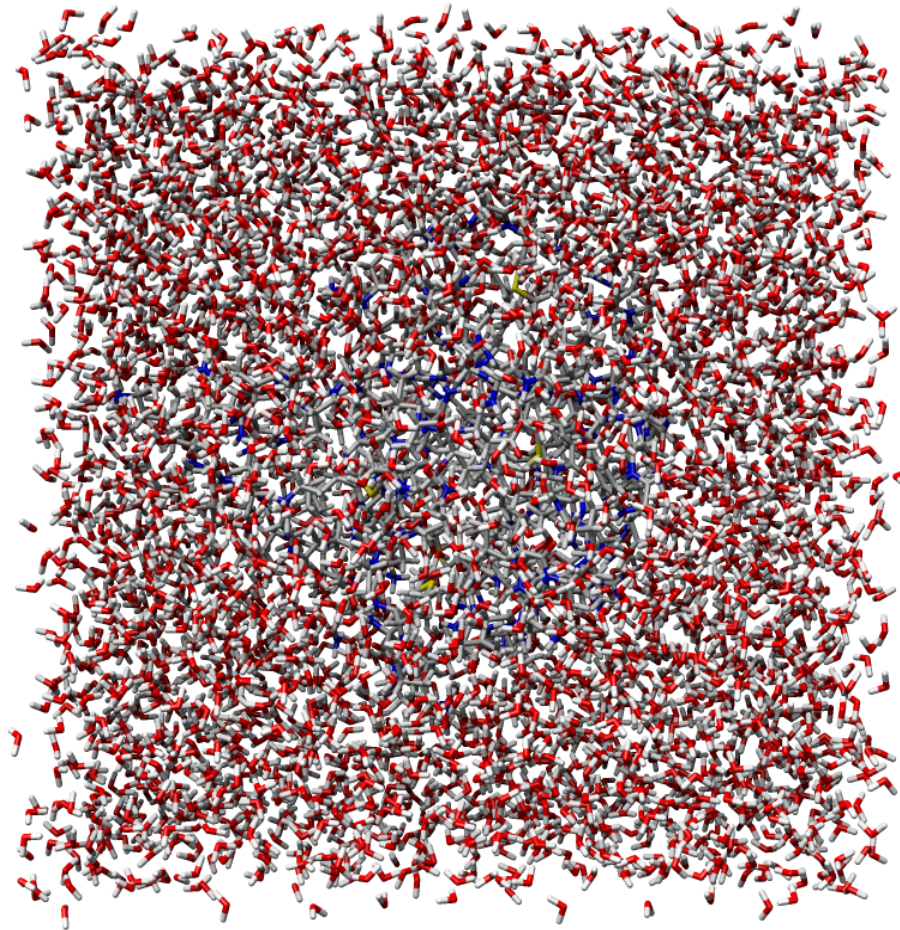


3chy, hydrogens added



# Molecular Dynamics

- MD provides atomic resolution of native dynamics

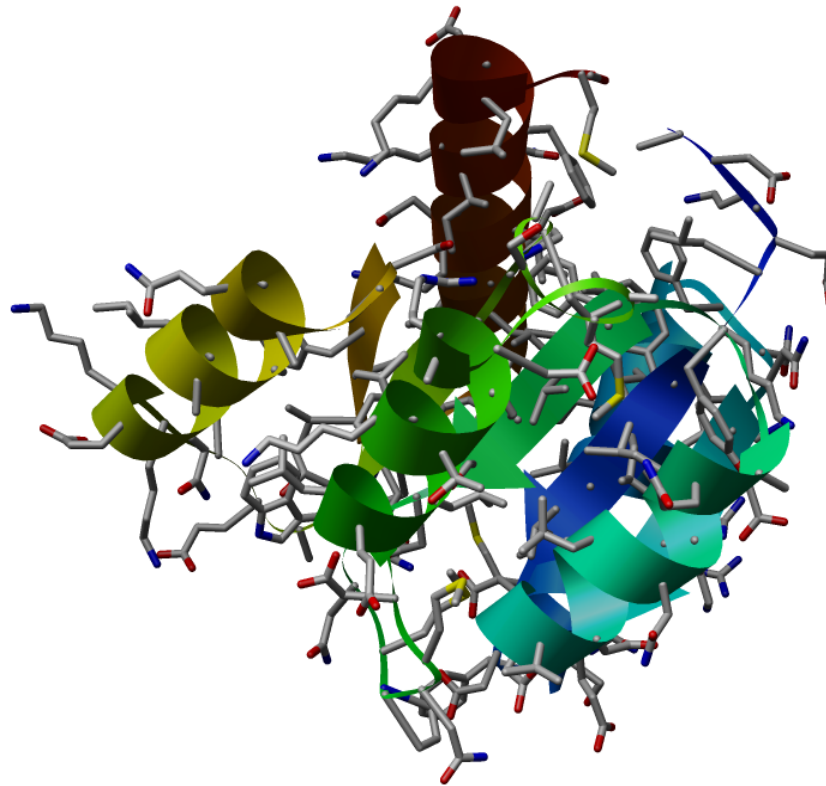


3chy, waters added (i.e. solvated)



# Molecular Dynamics

- MD provides atomic resolution of native dynamics



3chy, waters and hydrogens hidden

# Molecular Dynamics

- MD provides atomic resolution of native dynamics



native state simulation of 3chy at 298 Kelvin, waters and hydrogens hidden

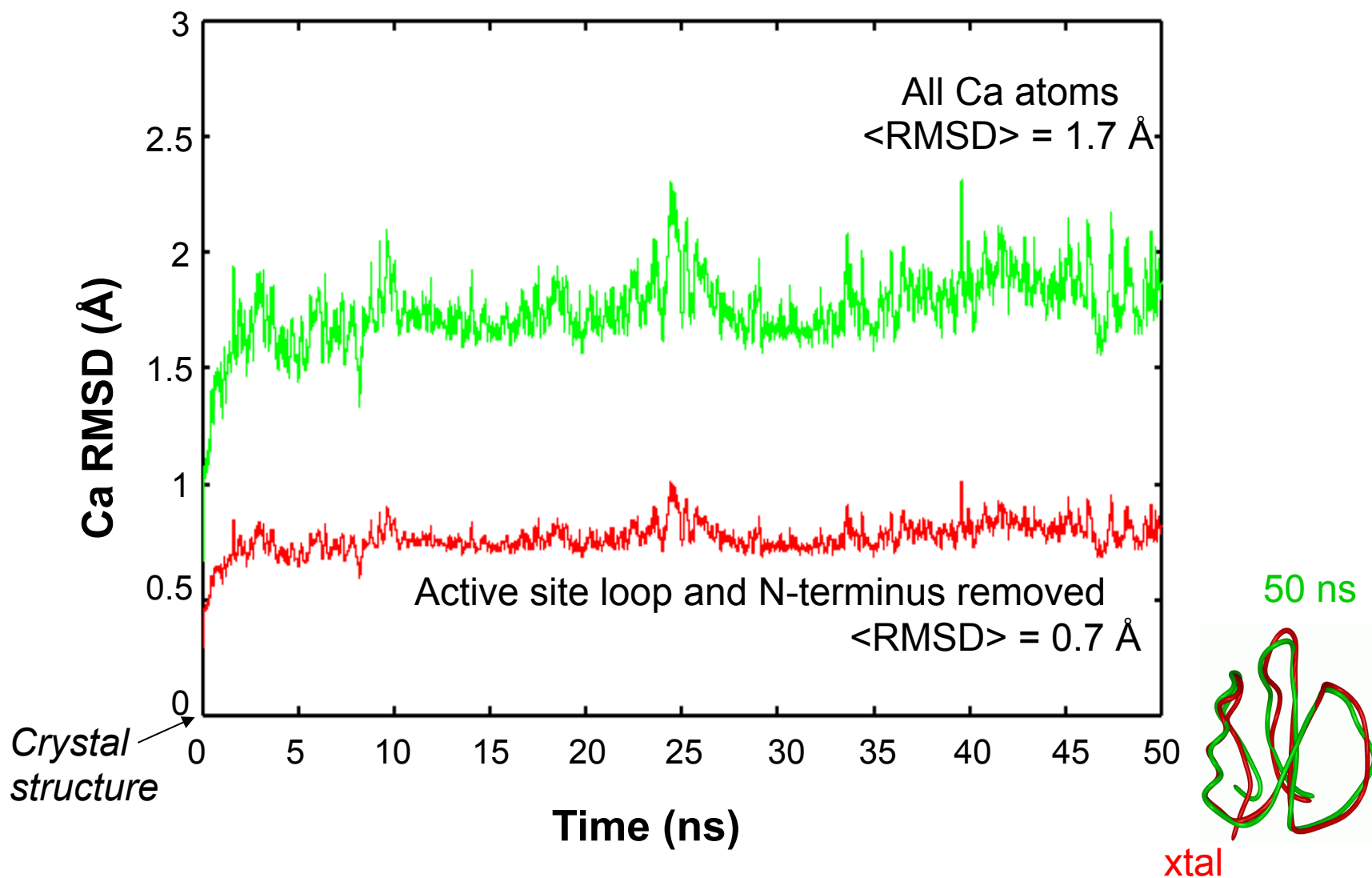
# Molecular Dynamics

- MD provides atomic resolution of folding / unfolding

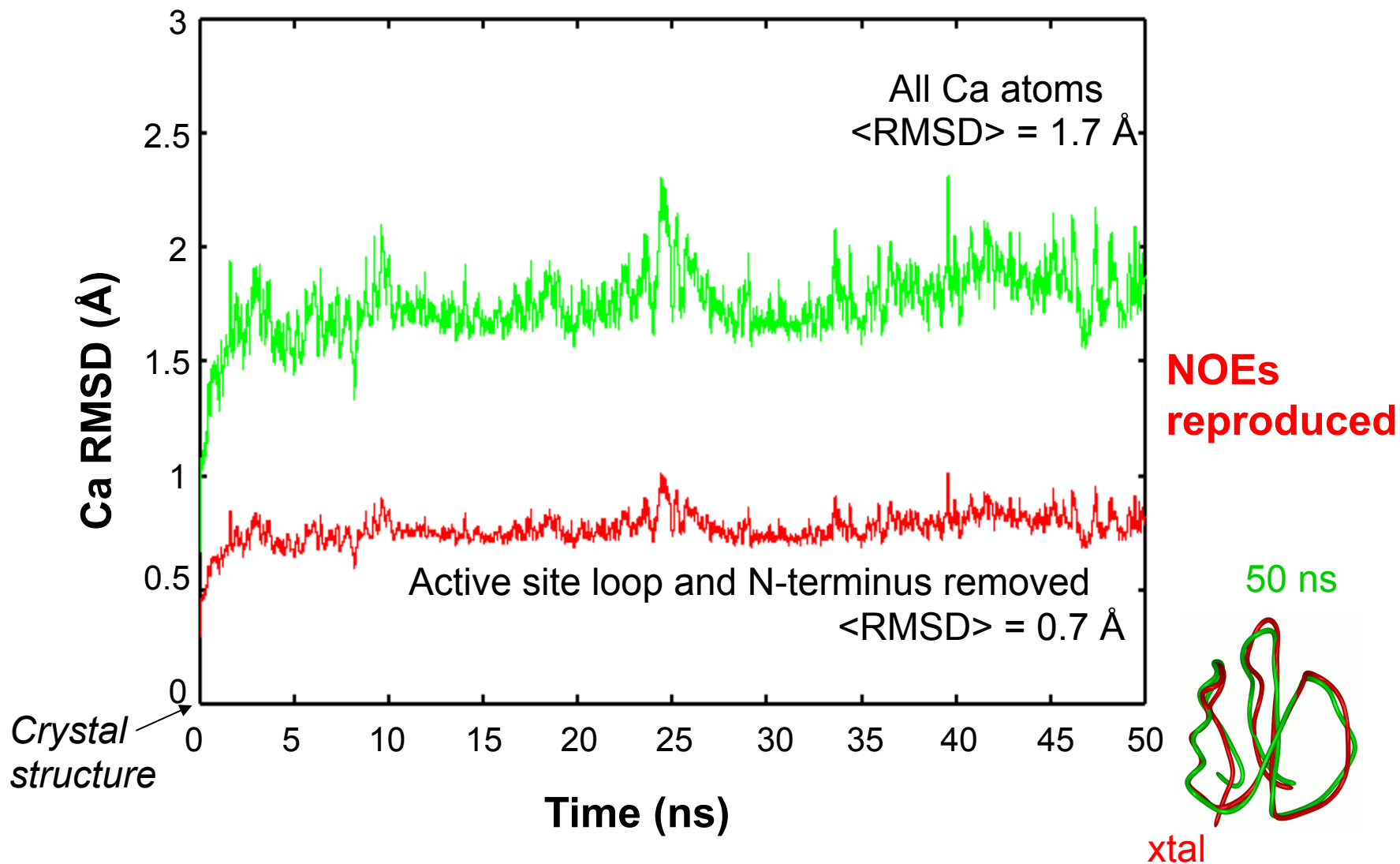


unfolding simulation (reversed) of 3chy at 498 Kelvin, waters & hydrogens hidden

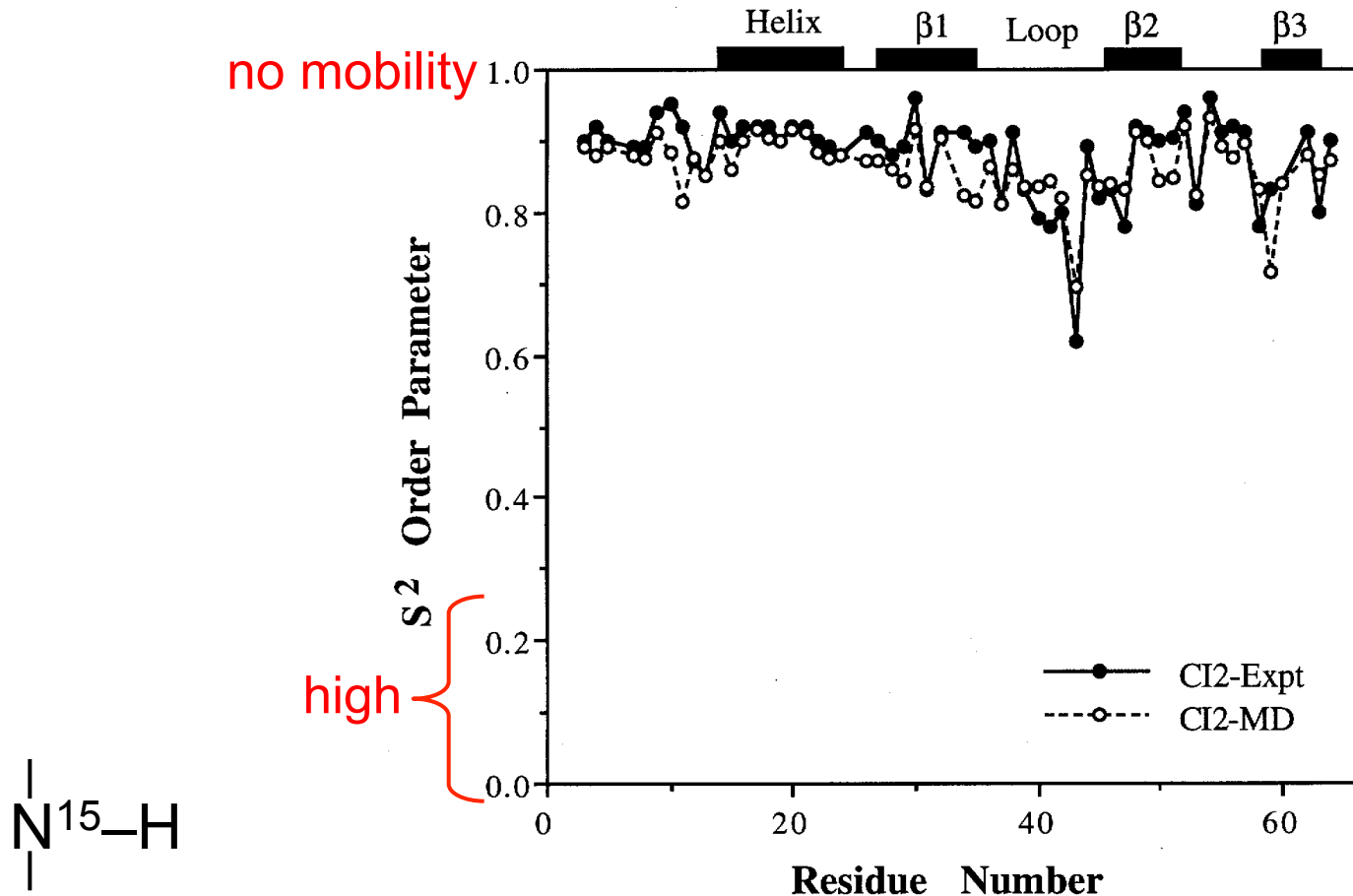
# Native Dynamics at 25 °C



# Native Dynamics at 25 °C

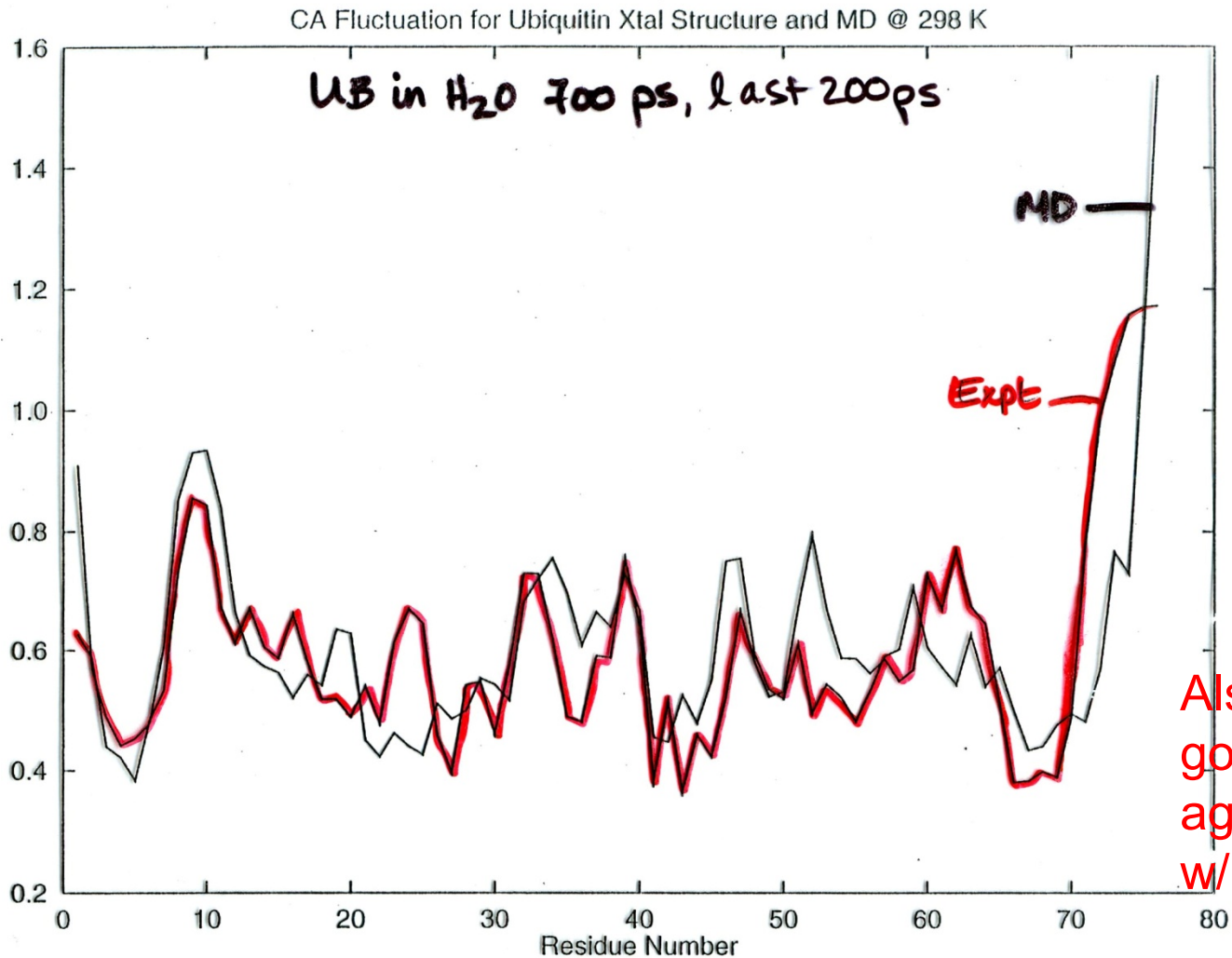


# Chymotrypsin Inhibitor 2



- Expt = Fersht and co-workers (1995) *Biochem* 34:2225
- MD = Li & Daggett (1995) *Prot. Eng.* 8(11)

# RMSF - B Value ( $\text{\AA}$ )



- Alonso & Daggett (1995) *J. Mol. Biol.* 247:501

Greg Petsko, “Not just your average structures”,  
Nat. Struct. Biol., 1996

Law of averages repealed → chaos

.....”We have designed our civilization around averages, but we understand that reality consists of fluctuations about those averages.”

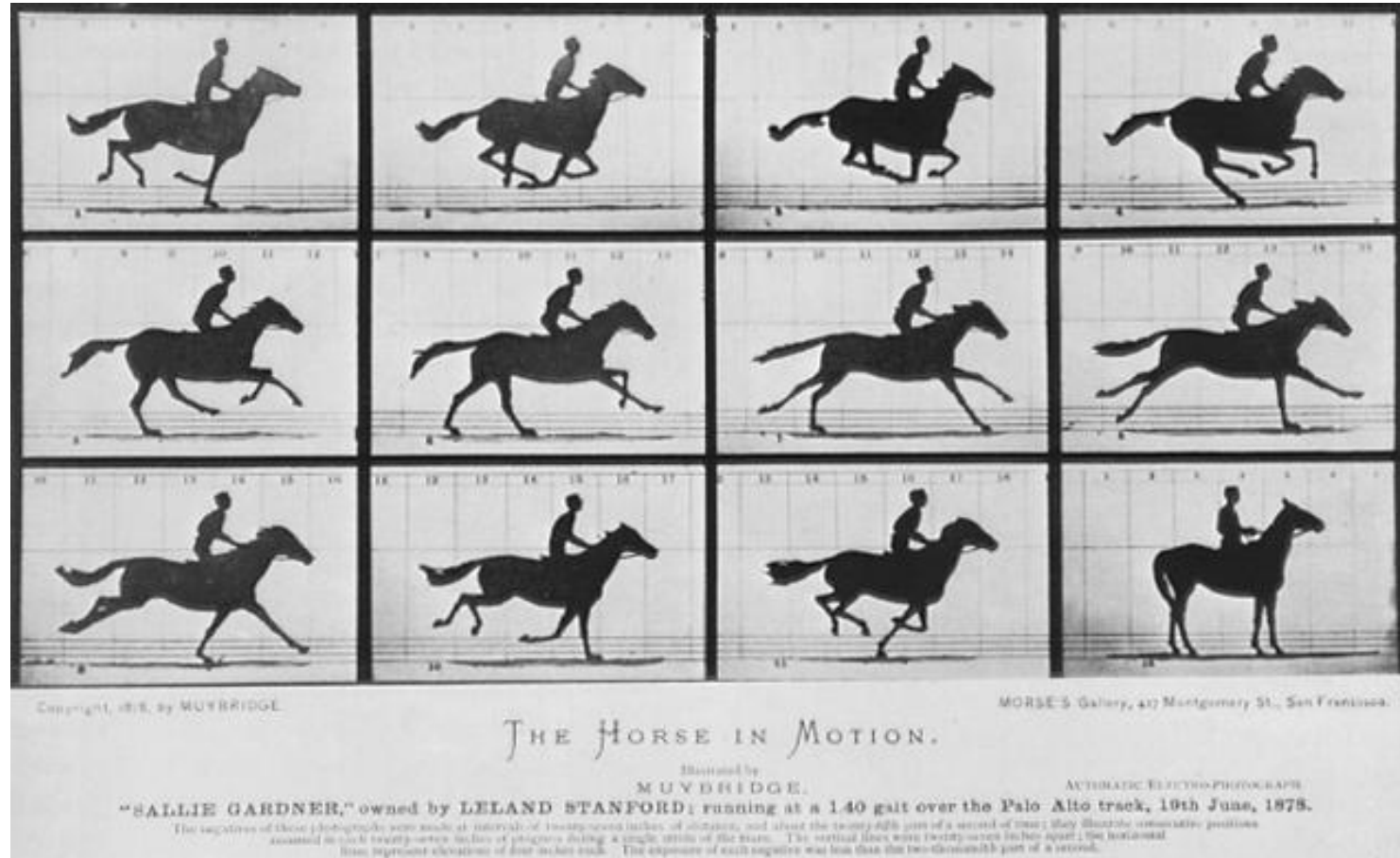


Proteins no exception. Beautiful static, time and ensemble averaged structures from NMR and crystallography only part of the story.

Protein function can depend on what we don't see: the excursions from average.

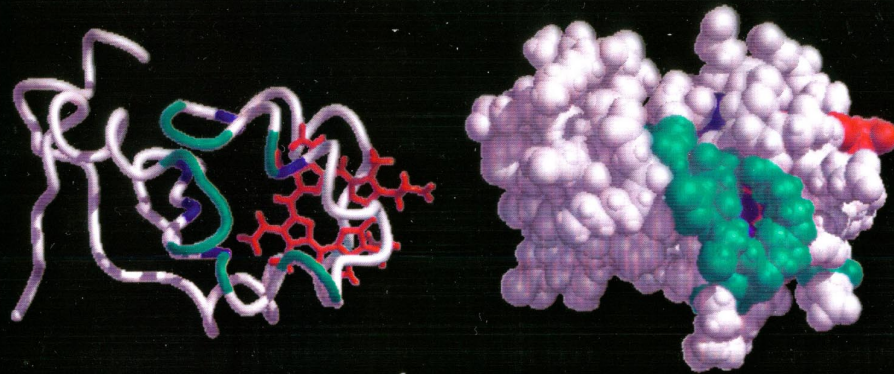


# Dynamics Necessary for Function

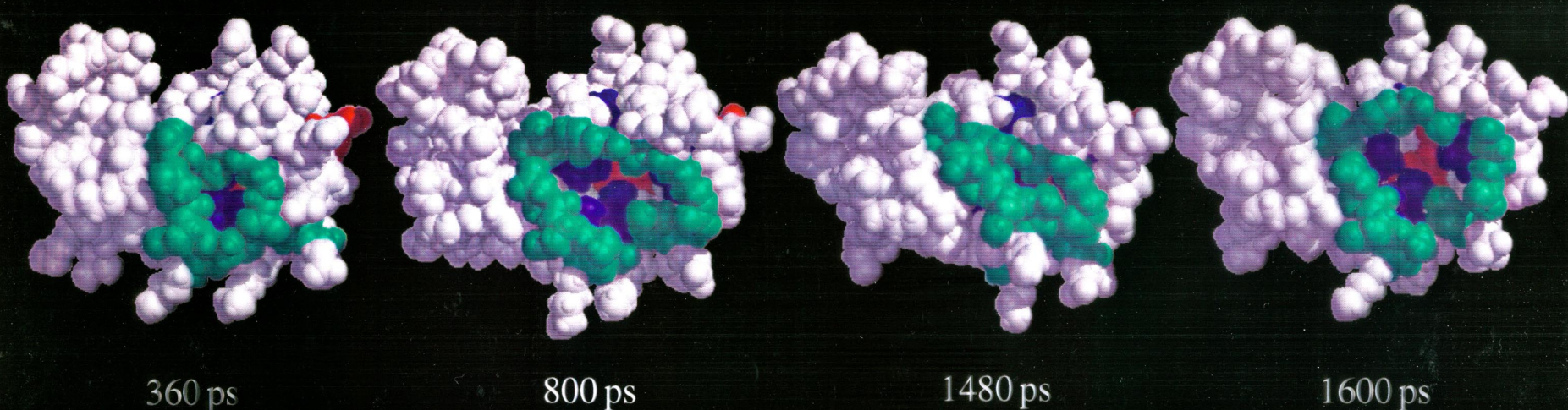
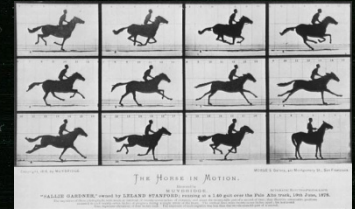


# Conformational Substates

Cytochrome  $b_5$

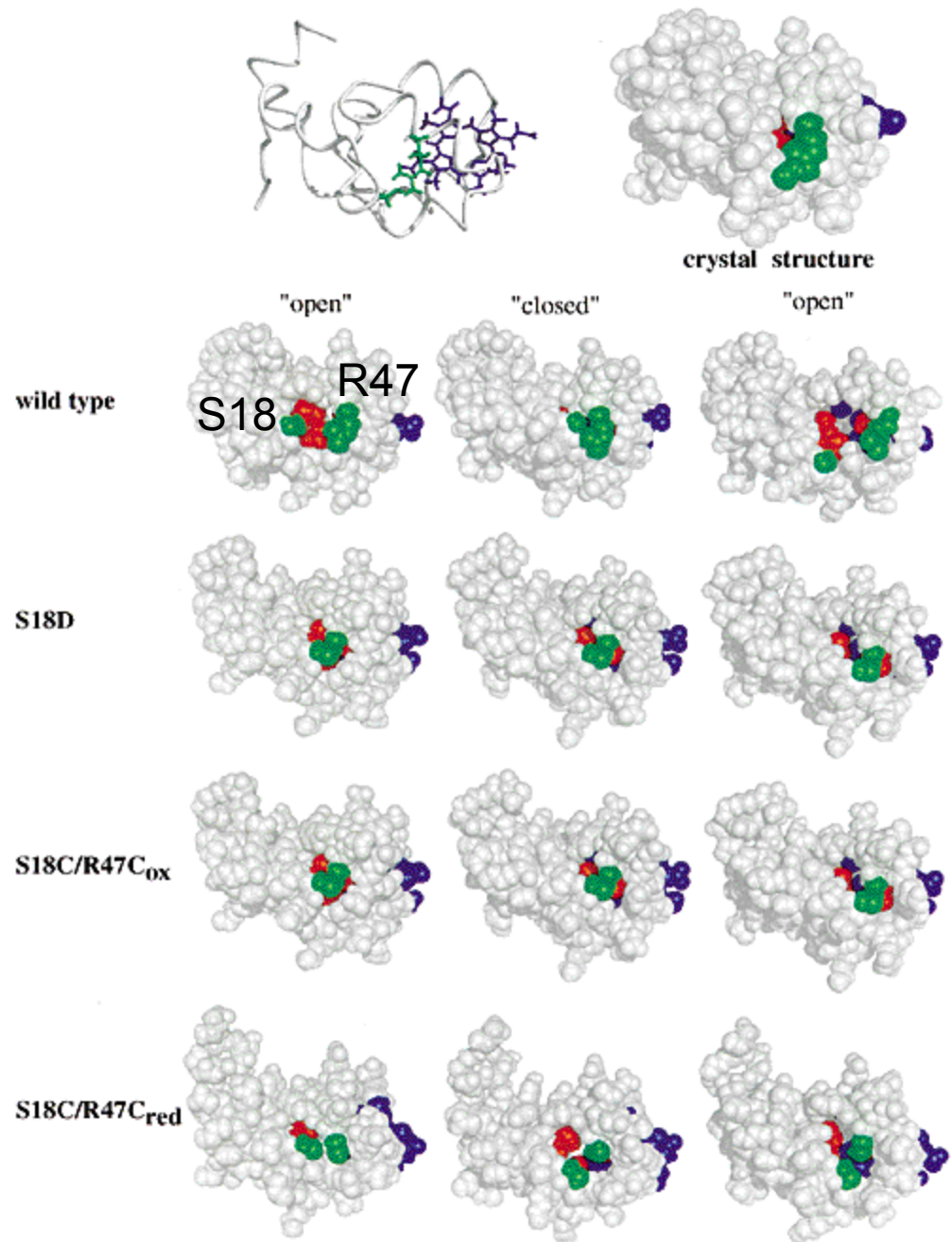


crystal structure





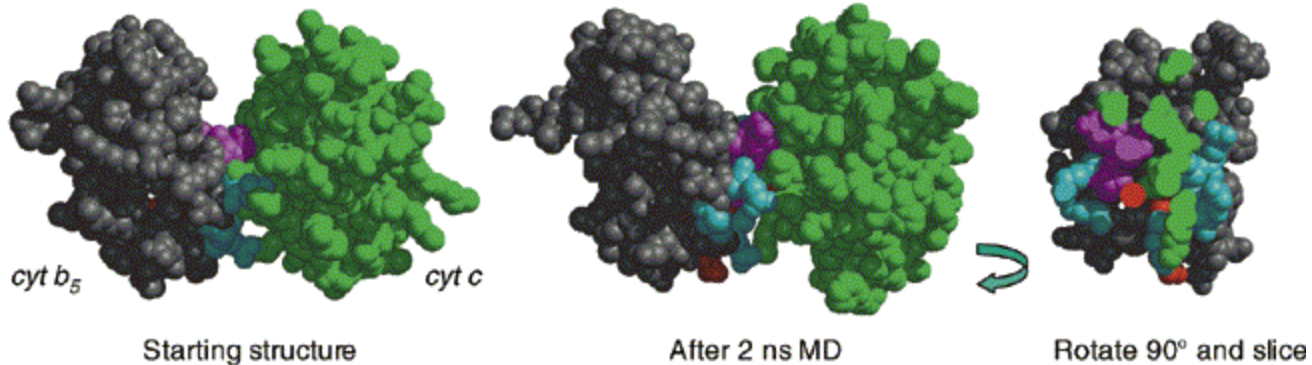
# Construction of mutants to test whether cleft forms



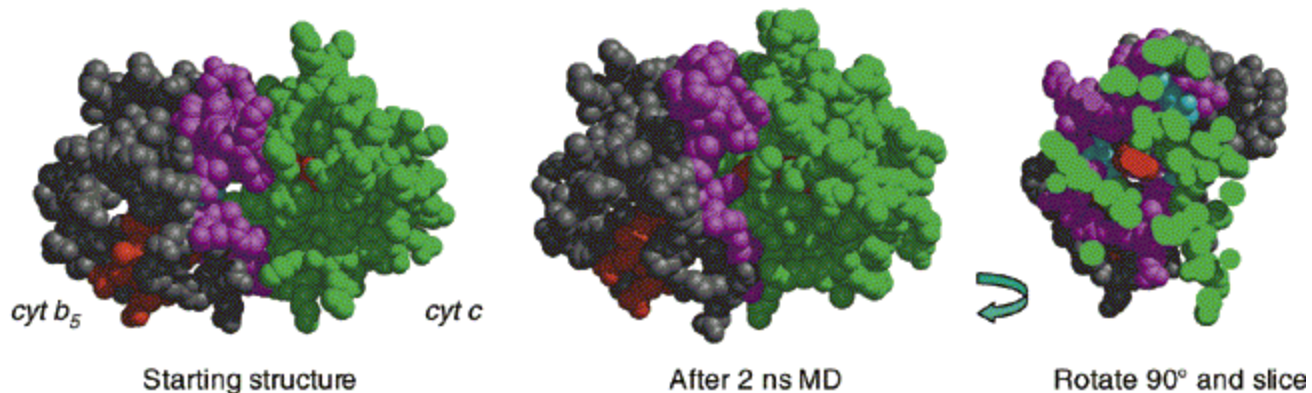
Storch et al., *Biochem*,  
1999

# Construction of cyt c – cyt b<sub>5</sub> complexes

## Salemme Binding Complex

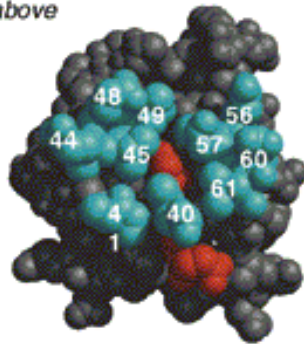


## Cleft Binding Complex

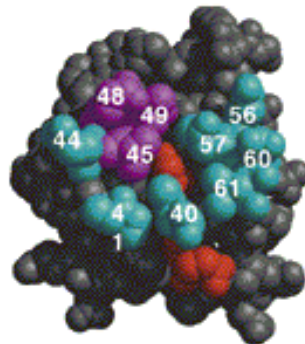


# Changes in cyt $b_5$ upon binding cyt c

*center above*




Residues at surface  
predicted to show  $\Delta\delta$



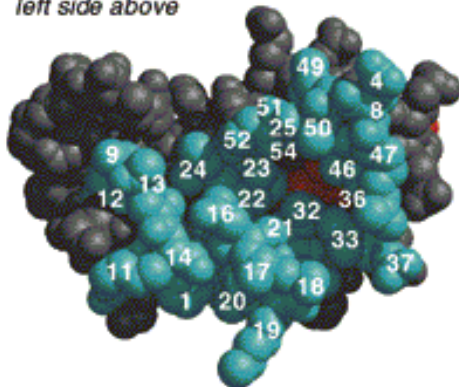
Residues with  $\Delta\delta \geq 0.06$   
in magenta

 = Predicted binding  
surface

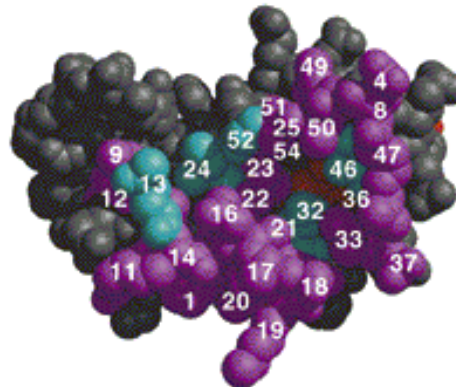
 = Change in  
chemical shift

## Proposed Cleft Binding Surface

*left side above*



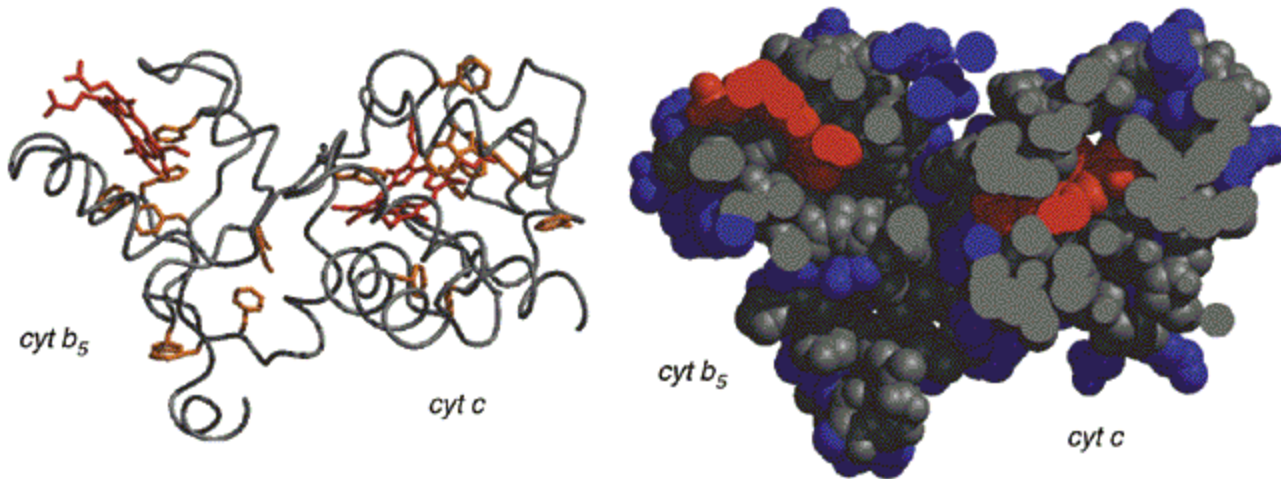
Residues at surface  
predicted to show  $\Delta\delta$





Residues with  $\Delta\delta \geq 0.06$   
in magenta

*Hom et al., Biochem, 2000*

# Cleft allows for electron transfer through the protein in channel lined with aromatics



 = Nonpolar  
 = Polar

# Native States

- Not rigid
- Not unique
- Diverse motion
  - Time scale
  - Amplitude
- > average motion - why?
  - Important for function

# Native States (cont)

- Functionally important motion & alternate states may not be well represented by an average structure
  - Conformational substates
    - » Mb - ligand binding
    - » Cyt b5 – recognition and electron transfer
    - » Rnase - binding
  - Catalysis
    - » RNase
    - » CI2 (inhibition of catalysis)
  - Evolution, adaptation to mutation
    - » Globins



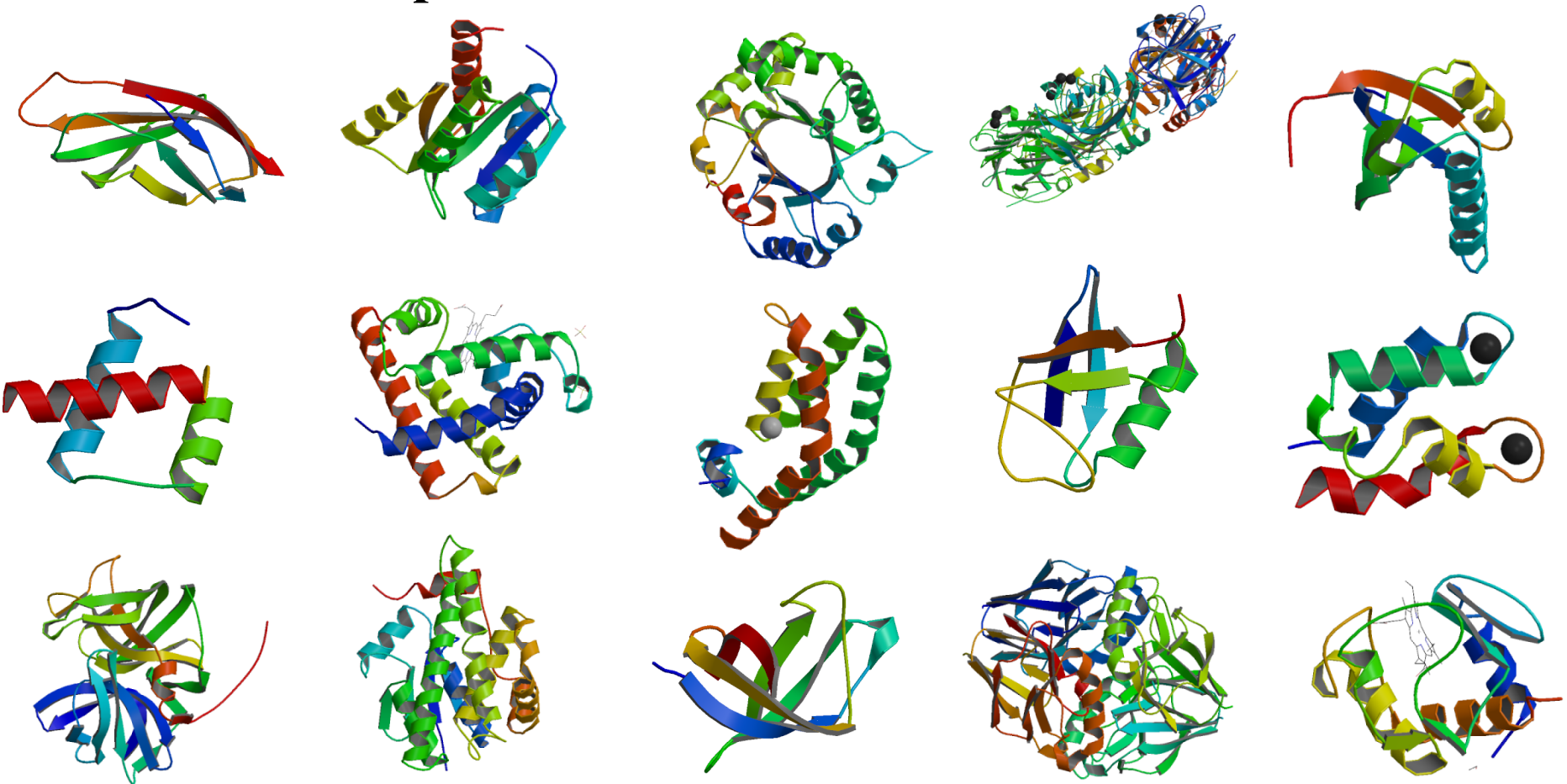
# Relevance of Protein Dynamics

- Native State
  - Adaptation to environment---solvent
  - Binding of ligands, ions, etc.
  - Binding to other proteins – recognition
  - Catalysis
  - Flexibility important for activity (thermophilic proteins)
  - Signal transduction
  - Protein translocation
  - etc

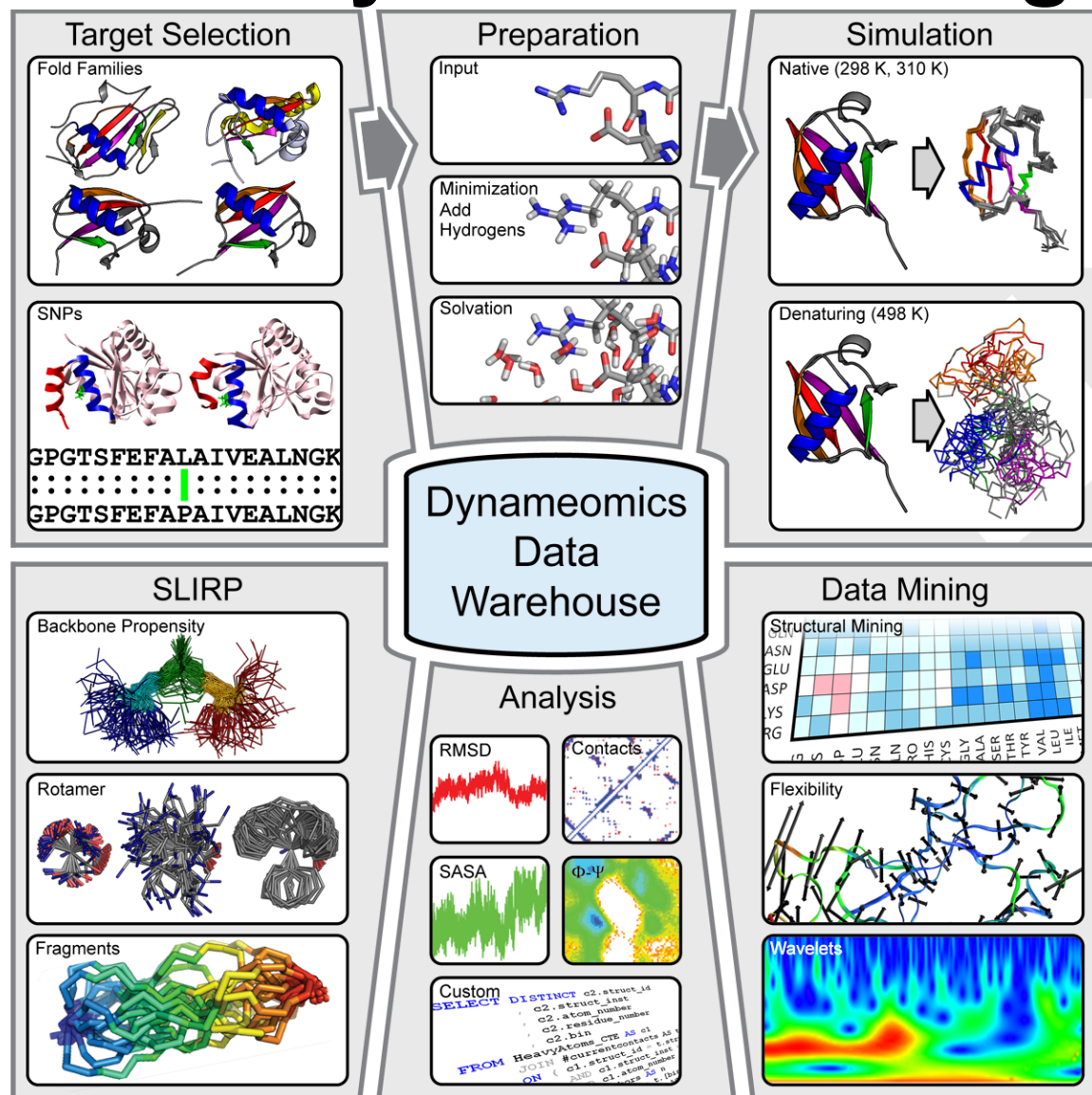
# Proteins

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**Many shapes, many sizes, >100,000 in PDB → 807 unique autonomous protein folds**



**www.dynameomics.org**



View standard results:

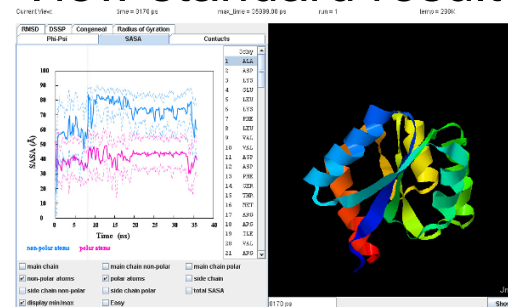


Figure 7.

## View movies

Create your own results:  
Request a login

## Top 100 targets and libraries

*Daggett and co-workers*  
*Structure, 14 April 2010*