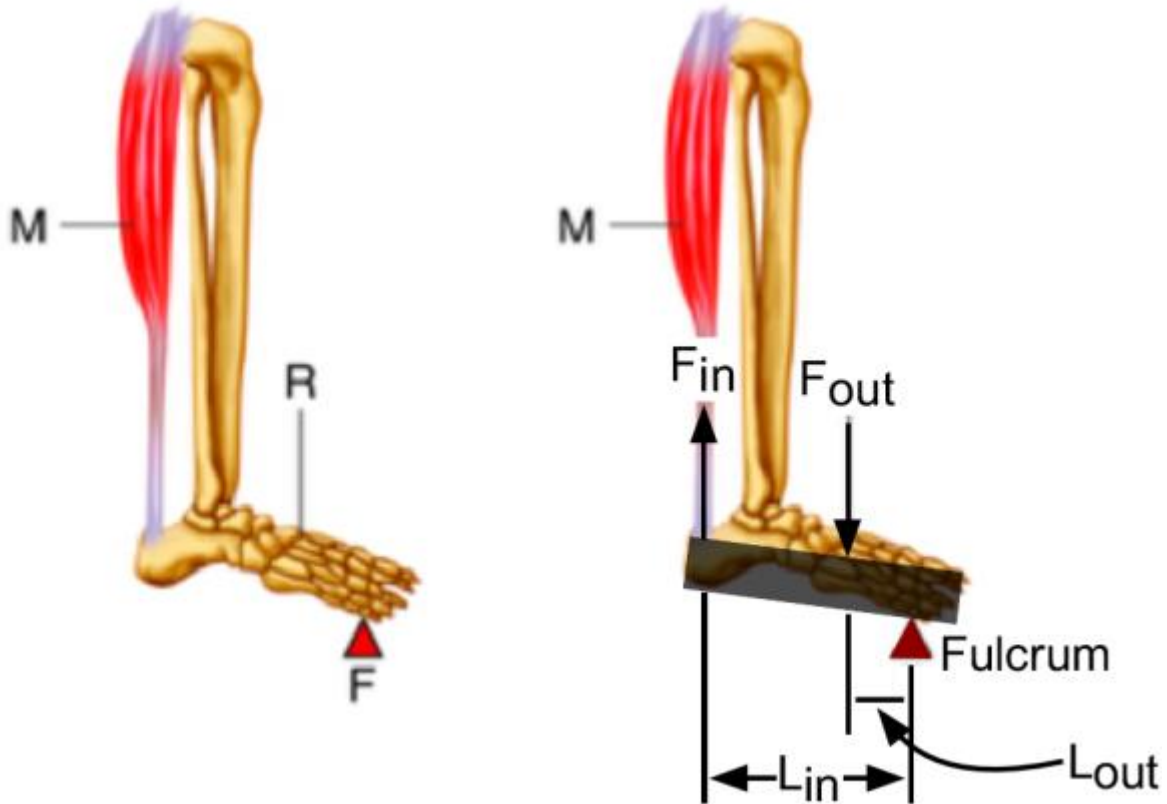


## 1. Tendon stress

- a. **2<sup>nd</sup> class lever.** The fulcrum is located at the ball of the foot as denoted by the figure that was provided. The force exerted by the gastrocnemius is  $F_{in}$ . The force resisting the motion—the weight of the foot—is  $F_{out}$ .



## b. Given:

Mass of the individual =  $m = 70 \text{ kg}$

$L_{in} = 15 \text{ cm} = 0.015 \text{ m}$

$L_{out} = 10 \text{ cm} = 0.01 \text{ m}$

It is important to remember that  $L_{in}$  and  $L_{out}$  correspond to the distance between the fulcrum and  $F_{in}$  and  $F_{out}$  respectively.  $L_{in}$  is **NOT** the length of the muscle.

$$F_{out} = F_{Resistance} = mg = (70 \text{ kg}) \cdot (9.8 \frac{\text{m}}{\text{s}^2})$$

$$F_{in} = F_{Generated \text{ by muscle}} = ?$$

$$F_{in} L_{in} = F_{out} L_{out}$$

$$F_{in} = \frac{L_{out}}{L_{in}} F_{out} = \left( \frac{0.01 \text{ m}}{0.015 \text{ m}} \right) (70 \text{ kg}) (9.8 \frac{\text{m}}{\text{s}^2}) = 457.3 \text{ N}$$

c. Given:

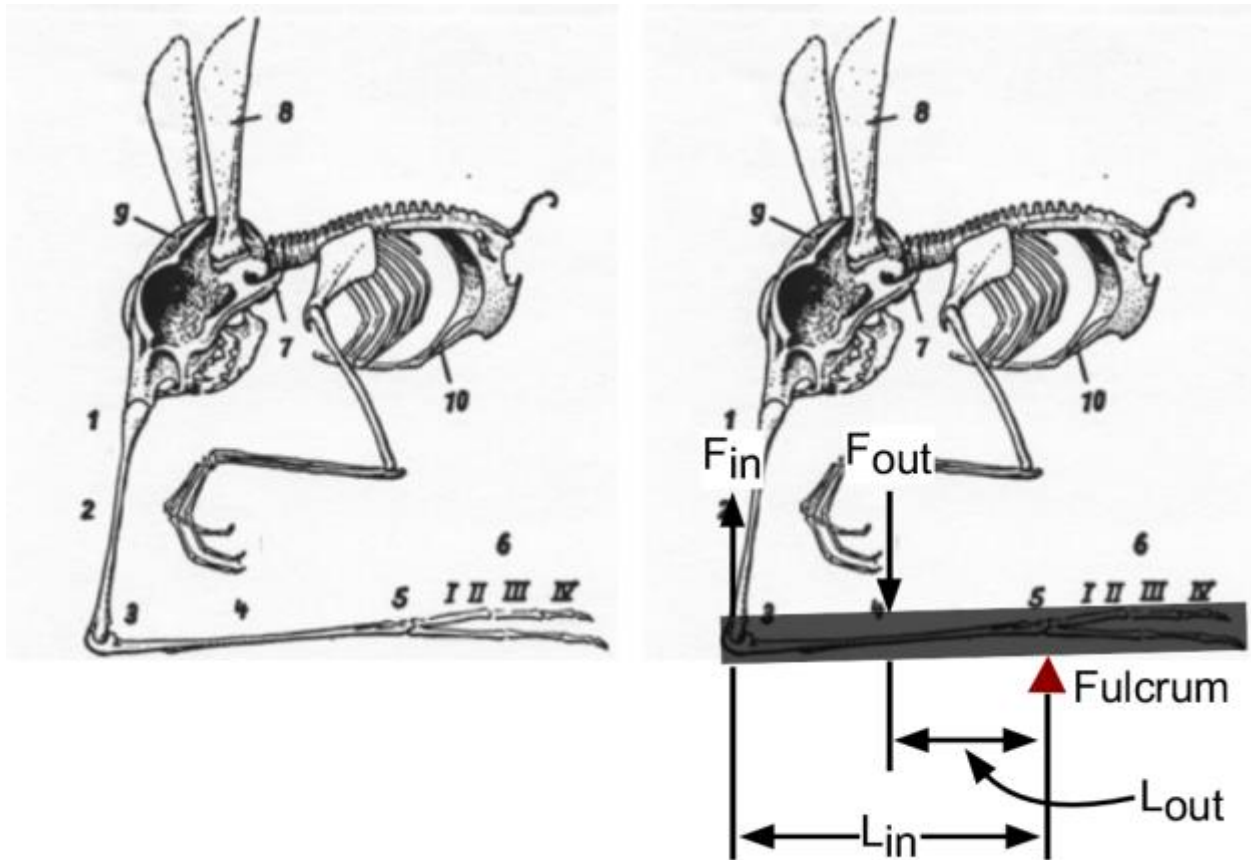
$$d_{tendon} = 1 \text{ cm} = 0.01 \text{ m}$$

$$A_{tendon} = \pi * r^2$$

$$\sigma_{tendon} = \frac{F_{in}}{A_{tendon}} = \frac{457.3 \text{ N}}{\pi \left(\frac{0.01 \text{ m}}{2}\right)^2} = 5.823 \text{ MPa}$$

2. *Otopteryx volitans*- The Rhinogrades

a. **2<sup>nd</sup> class lever**. Similar to the gastrocnemius problem above.



b. Speed ratio (SR) and mechanical advantage (MA) are dimensionless numbers. Therefore, you only need the **ratio of the lengths** to compute both SR and MA.

- c. What is relevant is the ratio of lengths. Note that the foot bone is 5 cm in length (when you measure it out with a ruler). This yields  $L_{in}$  to be ~5 cm, and  $L_{out}$  to be ~3.75 cm.

$$\text{Mechanical advantage} = MA = \frac{L_{in}}{L_{out}} = \frac{5 \text{ cm}}{3.75 \text{ cm}} = 1.33$$

$$\text{Speed ratio} = SR = \frac{1}{MA} = \frac{L_{out}}{L_{in}} = \frac{3.75 \text{ cm}}{5 \text{ cm}} = 0.75$$

Points were awarded as long as SR was larger (and inversely proportional) to MA.

For more information on the Rhinogrades, check this out:

[http://speculativeevolution.wikia.com/wiki/The\\_Snouters:\\_Form\\_and\\_Life\\_of\\_the\\_Rhinogrades](http://speculativeevolution.wikia.com/wiki/The_Snouters:_Form_and_Life_of_the_Rhinogrades)

They almost seem too weird to be true, right?

### 3. Skater

a.

$$m = 70 \text{ kg}$$

$$R = 0.5 \text{ m}$$

Convert  $\omega$  from rotations per minute to radians per second as follows:

$$\omega = 308 \frac{\text{rotations}}{\text{minute}} \left( \frac{1 \text{ minute}}{60 \text{ seconds}} \right) \left( \frac{2\pi \text{ radians}}{1 \text{ rotation}} \right) = 32.25 \frac{\text{radians}}{\text{second}}$$

$$I = \frac{1}{2} mR^2 = (0.5)(70 \text{ kg})(0.5 \text{ m})^2 = 8.75 \text{ kg} \cdot \text{m}^2$$

$$\text{Kinetic rotational energy} = \frac{1}{2} I \omega^2 = (0.5)(8.75 \text{ kg m}^2) \left( 32.25 \frac{\text{rad}}{\text{s}} \right)^2$$

$$= 4550 \text{ Joules}$$

- b. The rotational energy would **stay the same** because we assumed no energy loss, and energy is conserved.
- c. As the skater spread her arms outward, her rotational speed ( $\omega$ ) would **decrease**. This is because kinetic energy is conserved and the skater's action of spreading her arms increases her moment of inertia ( $I$ ).

4. Get creative. You MUST convert mechanical energy by manipulating some body motion into electrical energy.