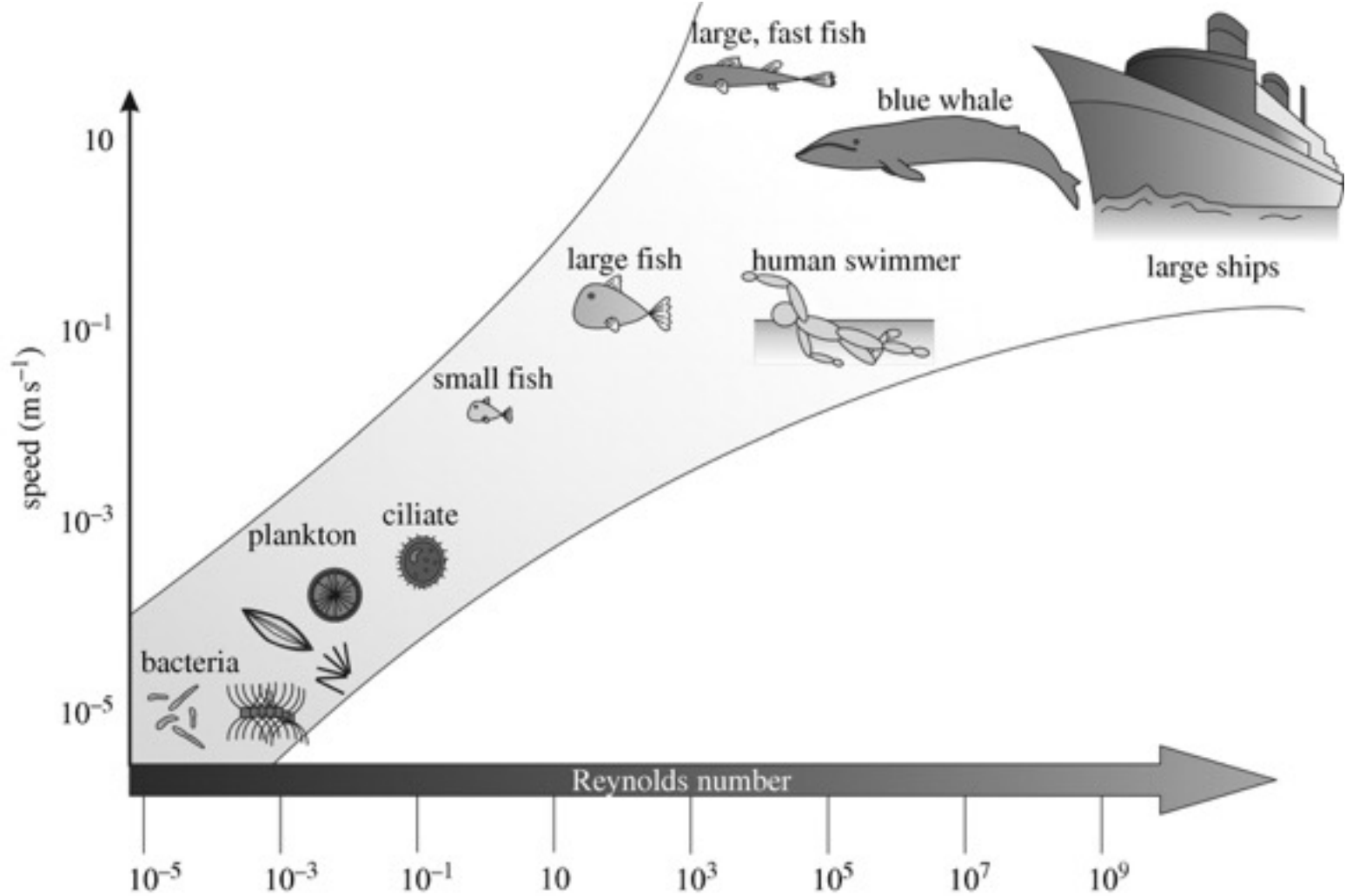


Lecture 25. Life at Low Reynolds Numbers

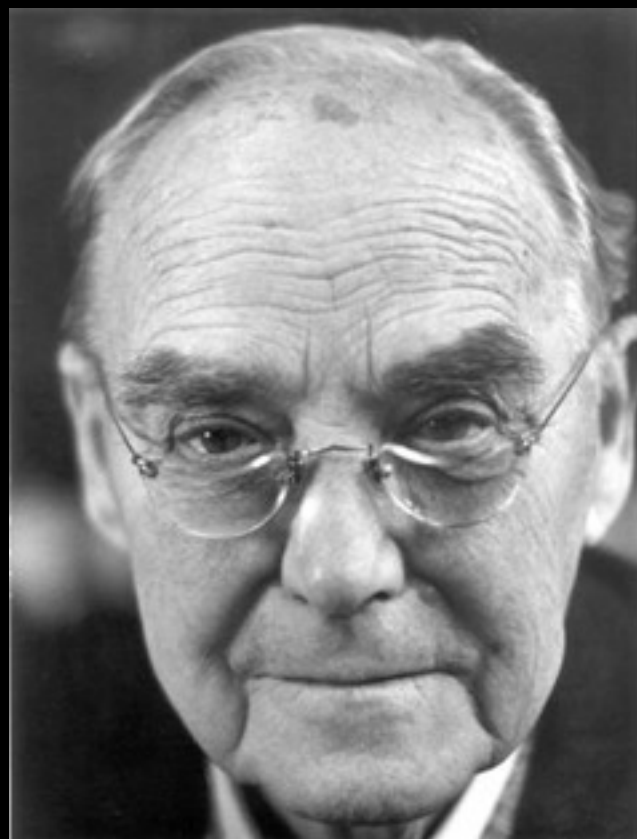
- Low Reynolds numbers
- Principles of low Re flows
- Gliding bacteria
- Vesicle transport
- Spores illustrated



## Designing biomimetic antifouling surfaces

Maria Salta, Julian A. Wharton, Paul Stoodley, Simon P. Dennington, Liam R. Goodes, Stéphane Werwinski, Ugar Mart, Robert J. K. Wood, Keith R. Stokes

Published 20 September 2010. DOI: 10.1098/rsta.2010.0195



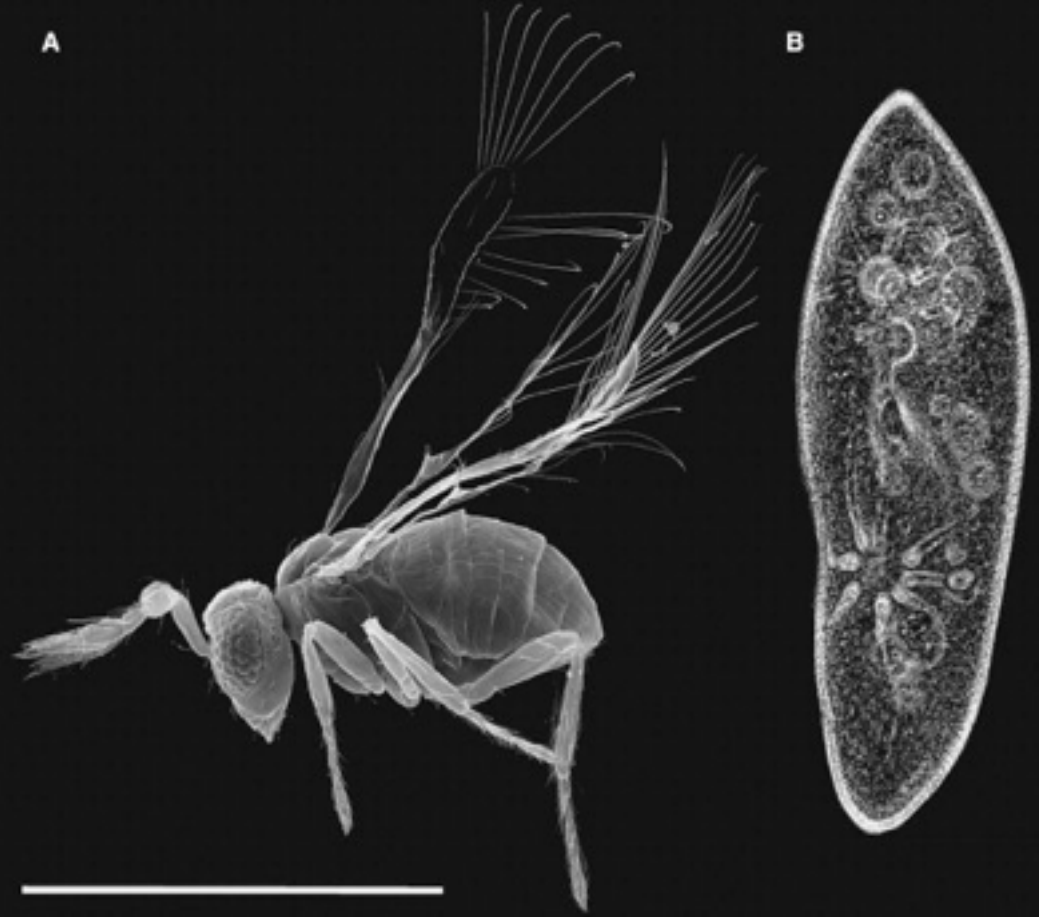
Sir G. I. Taylor

Taylor cone  
Taylor dispersion  
Taylor number  
Taylor vortex  
Taylor–Couette flow  
Taylor–Goldstein equation  
Rayleigh–Taylor instability  
Taylor–Proudman theorem  
Taylor–Green vortex  
Taylor microscale  
Taylor column

## Life at Low Reynolds numbers ( $Re \ll 1$ )

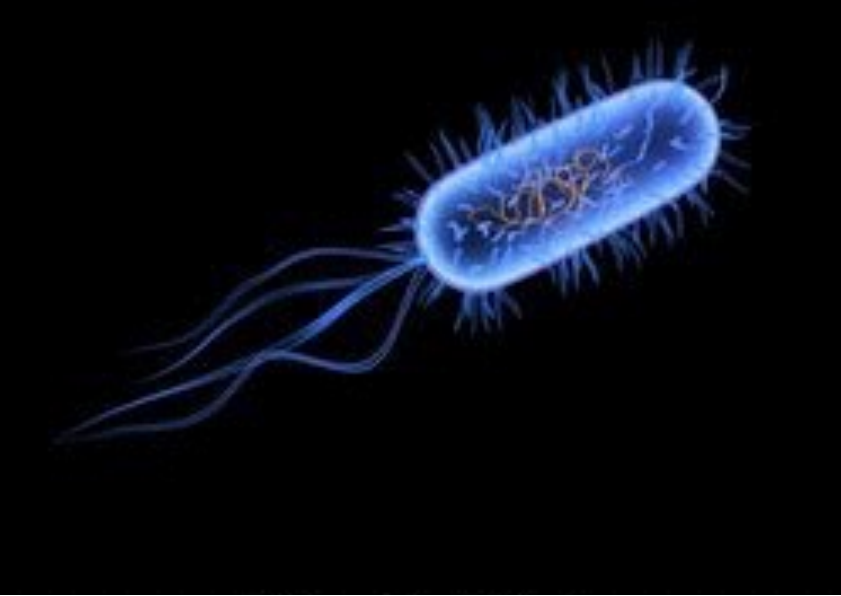
Phenomenological issues:

- disturbances are manifest over huge relative distances.  
(boundaries are all important)
- inertia is negligible
- flow is reversible (flow equations are linear)
- shape matters considerably less (no wakes)



Myrmecodia wasps:  
paddles versus rakes





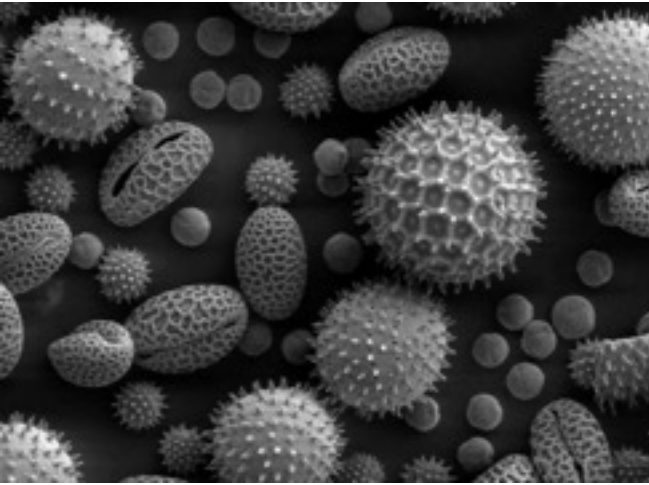
How far will this glide if the flagella stop?

$$m \frac{dU}{dt} = -6\pi r \mu U$$

$$U = U_0 e^{-6\pi r t \mu / m}$$

A Mathematica demonstration

Spores illustrated: what is their trajectory upon ejection?

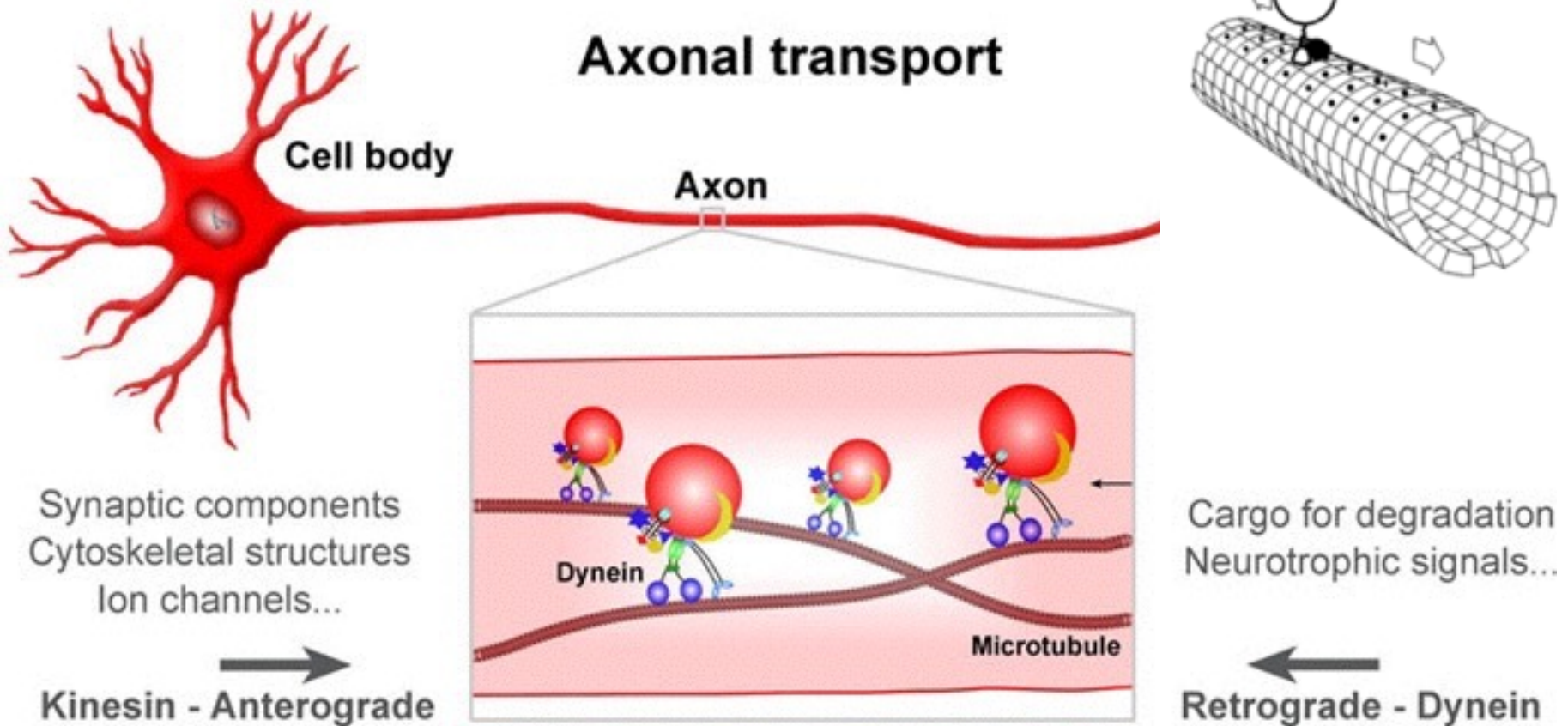


$$m \frac{dU}{dt} = 6\pi r \mu U$$

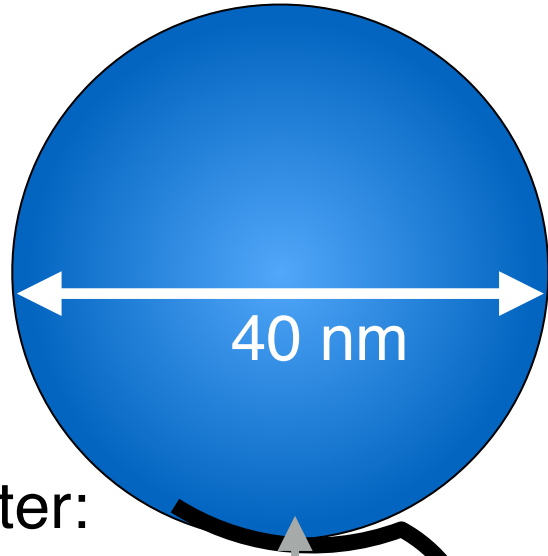
$$m \frac{dV}{dt} = 6\pi r \mu V - mg$$

A Mathematica demonstration

# Axonal transport: Rate of energy expenditure to move a vesicle?





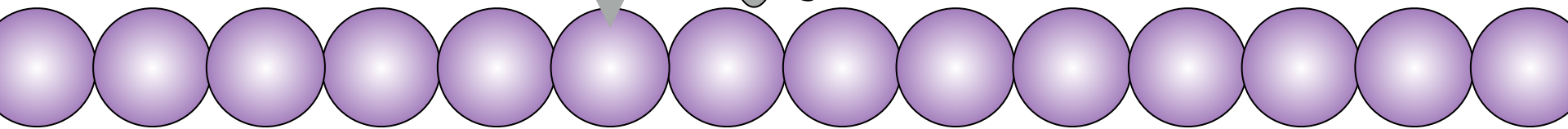


$$\textit{Drag} = 6\pi r\mu U$$

$$\textit{Power} = 6\pi r\mu U^2$$

Viscosity of water:  
 $9 \cdot 10^{-4} \text{ Pa s}$

17 nm

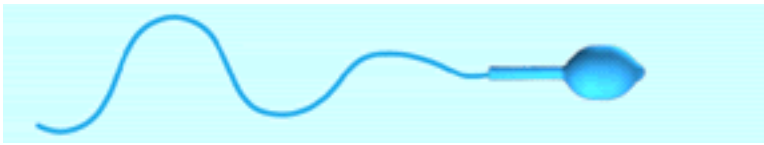


Data: 400 mm/day  
step size = 8 nm.

How many steps/second?  
How many ATP/second ?

Data: 1 ATP :  $9 \cdot 10^{-20} \text{ J}$

How many J/second ?  
How fast?



$$D = \frac{4\pi\mu U\mu l}{\ln\left(\frac{l}{a}\right) + 0.193}$$

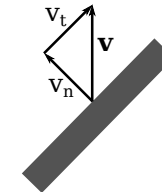
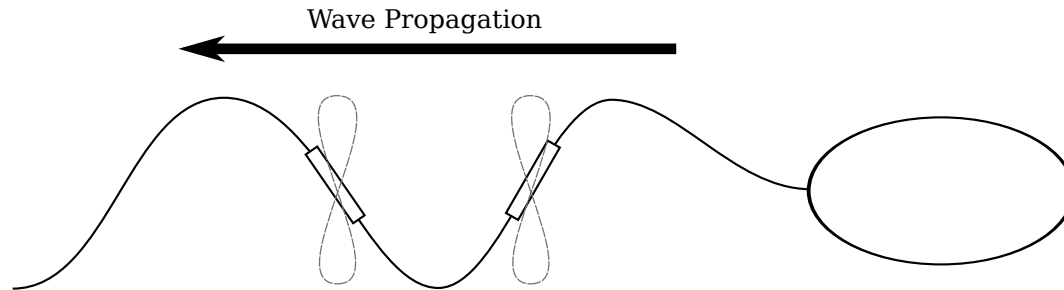
Cross flow

$$D = \frac{2\pi\mu U\mu l}{\ln\left(\frac{l}{a}\right) - 0.897}$$

Longitudinal flow

Two questions:

- What are the cellular mechanisms that generate force?
- What are the fluid dynamic mechanisms that propel the animal?





A  
L + R  
P

