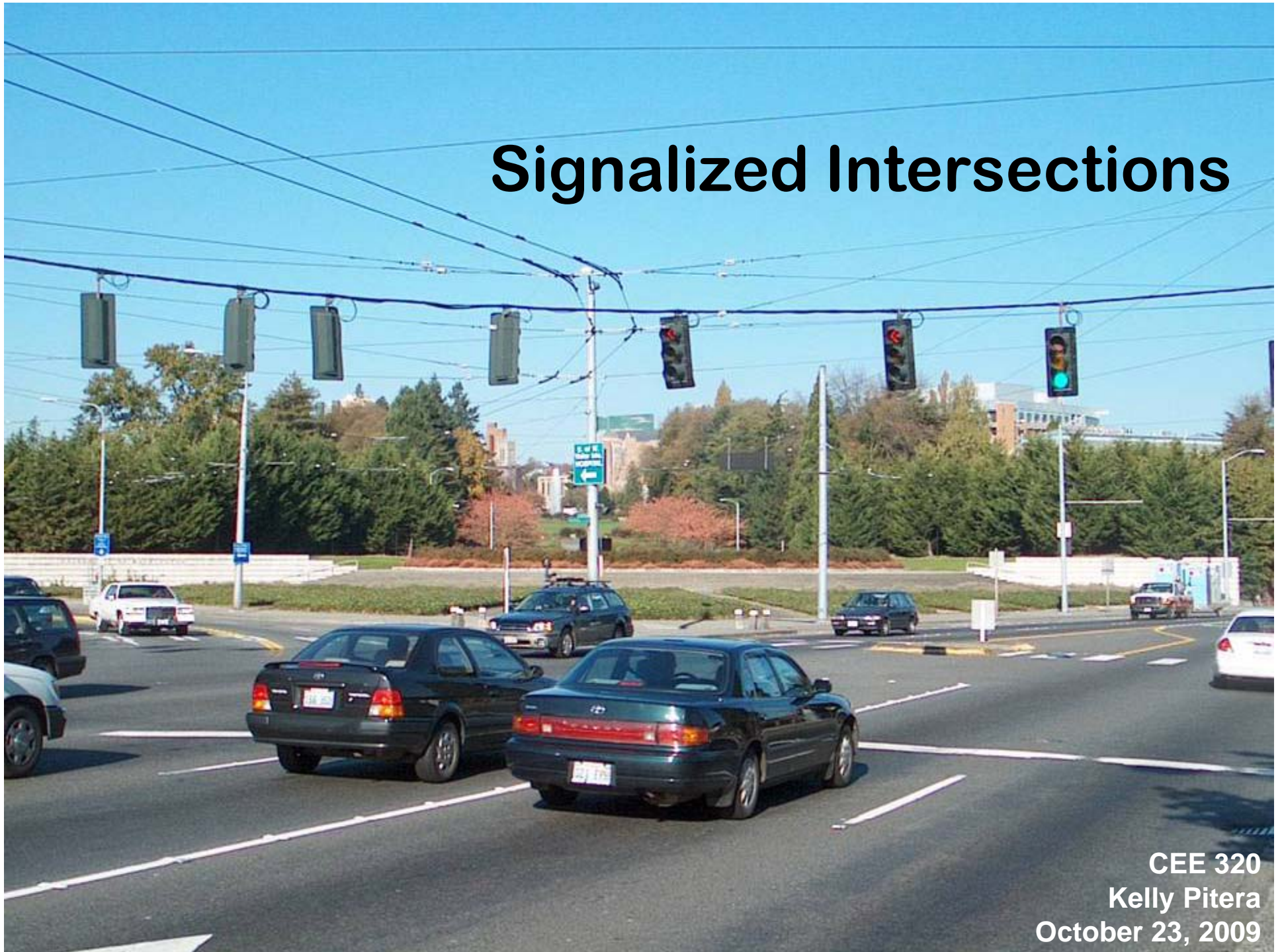


# Signalized Intersections



CEE 320  
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# Topics to be Covered

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- Introduction/Definitions
- D/D/1 Queueing
- **Phasing and Timing Plan**
- **Level of Service (LOS)**

# Signal Optimization

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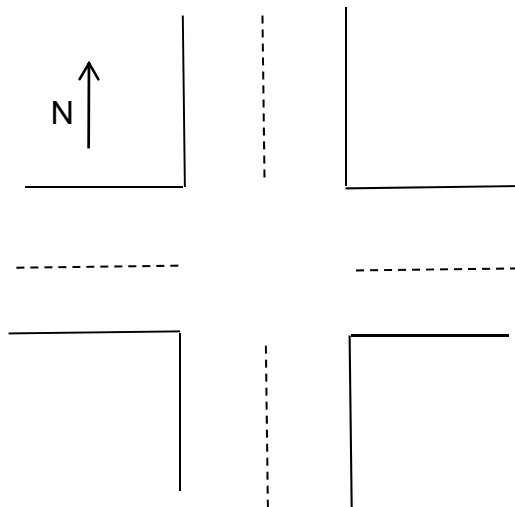
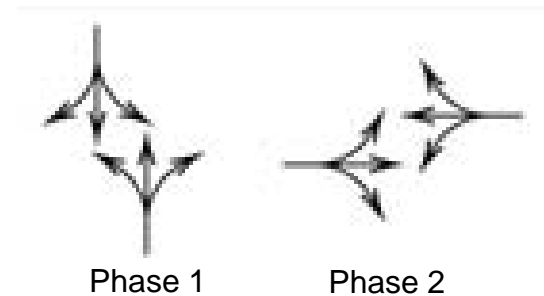
- **Conflicting Operational Objectives**
- **What should be optimized?**
  - minimize vehicle delay
  - minimize vehicle stops
  - minimize lost time
  - maximize major street green time
  - maximize pedestrian service
  - minimize accidents/severity

# Traffic Signal Phasing & Timing Plan

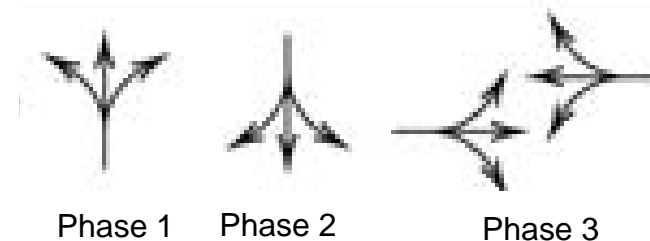
1. **Select signal phasing**
2. **Establish analysis lane groups**
3. **Calculate analysis flow rates and adjusted saturation flow rates**
4. **Determine critical lane groups and total cycle lost time**
5. **Calculate cycle length**
6. **Allocate green time**
7. **Calculate change and clearance intervals**
8. **Check pedestrian crossing time**

# 1. Select Signal Phasing

- A cycle is made up of phases
- Most basic: Two-phase signal:



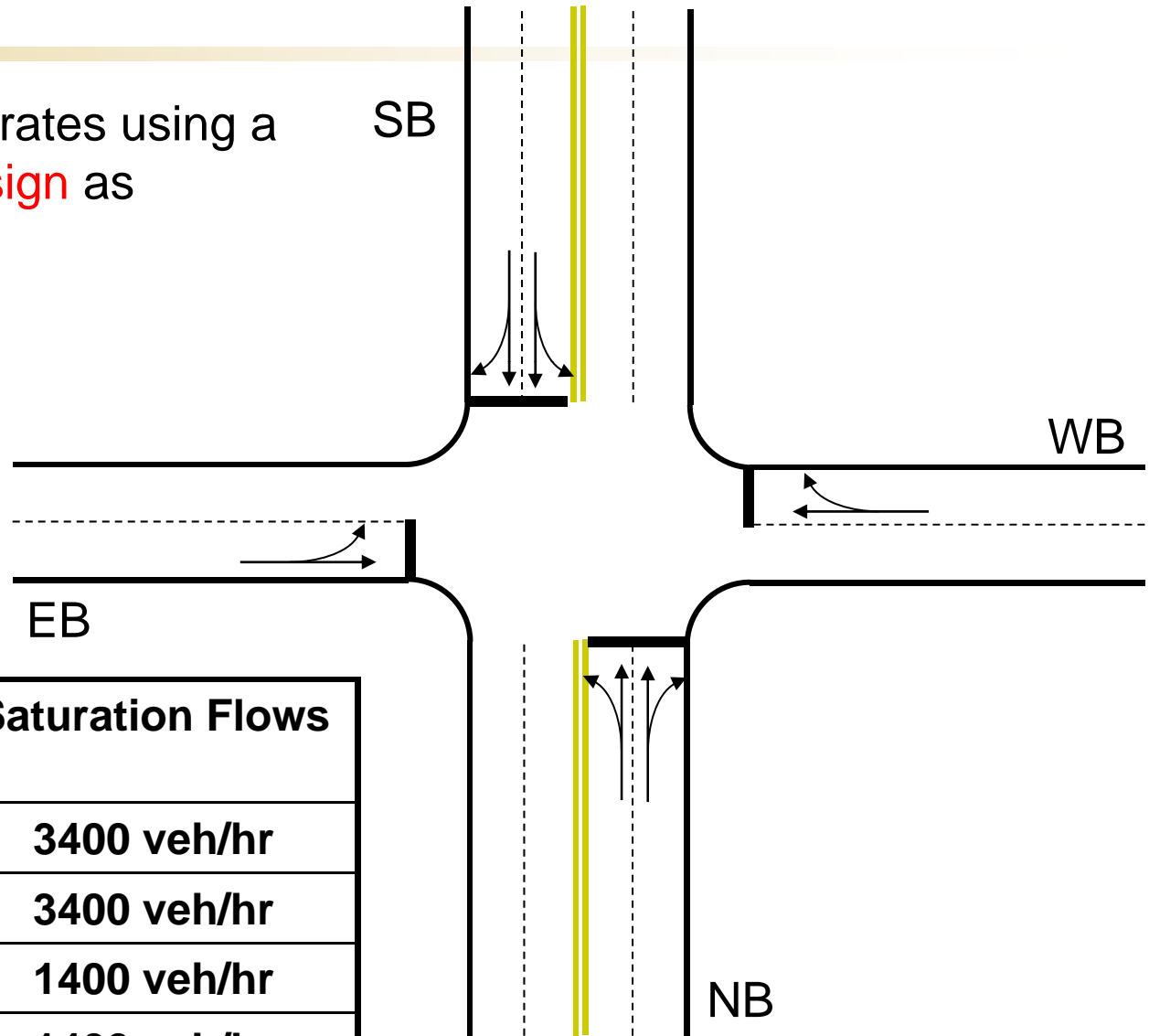
- Same street configuration but as a three-phase signal



- In this class, number of phases will be given to you

# EXAMPLE

An intersection operates using a simple **3-phase design** as pictured.














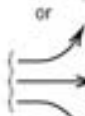


Phase	Lane group	Saturation Flows
1	SB	3400 veh/hr
2	NB	3400 veh/hr
3	EB	1400 veh/hr
	WB	1400 veh/hr

## 2. Establish Analysis Lane Groups

- **Lane Group**: A set of lanes established at an intersection approach for separate analysis
- **Guidelines for establishing lane groups**
  - Movements made simultaneously from the same lane must be treated as a lane group
  - If an exclusive turn lane (or lanes) is present, it is usually treated as a separate lane group
  - If a lane (or lanes) with shared movements exists in a multiple lane approach, it must first be determined whether it really serves multiple movements or whether it is a de facto lane for one of the movements

## 2. Establish Analysis Lane Groups

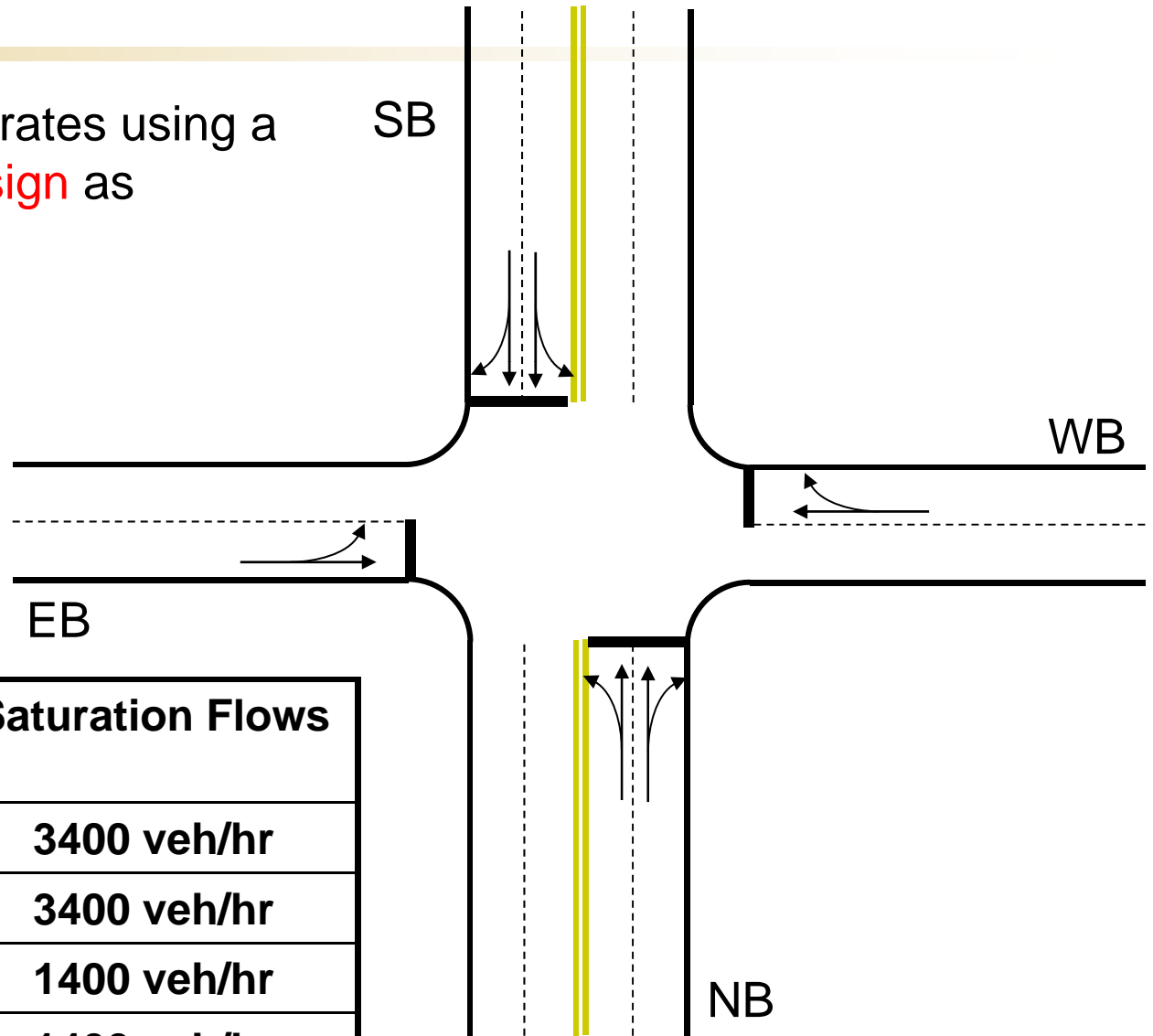
Number of lanes	Movements by lane	Number of possible lane groups
1	LT + TH + RT 	①  (Single-lane approach)
2	EXC LT  TH + RT 	② 
2	LT + TH  TH + RT 	①  or ② 
3	EXC LT  TH  TH + RT 	②  or ③ 

(Figure 7.12 in text)



# EXAMPLE

An intersection operates using a simple **3-phase design** as pictured.



Phase	Lane group	Saturation Flows
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### 3. Calculate Analysis Flow Rates and Adjusted Saturation Flow Rates

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- Need to account for the peak 15-minute flow within an hour (calculate PHF)
- Similar to analysis of uninterrupted flow (chapter 6)
- For our work, **assume that the approach volumes and saturation flow rates have already been adjusted**

## 4. Determine critical lane groups and total cycle lost time

- **Critical Lane Group**: The lane group that has the highest flow ratio (traffic intensity) ( $v/s$ ) for a given signal phase (lane group with the greatest demand)
- Calculate the sum of flow ratios for critical lane groups,  $Y_c$  (to be used in step 5)

$$Y_c = \sum_{i=1}^n \left( \frac{v}{s} \right)_{ci}$$

$(v/s)_{ci}$  = flow ratio for critical lane group  $i$

$n$  = number of critical lane groups

## 4. Determine critical lane groups and total cycle lost time

- Total lost time for the cycle,  $L$  (to be used in step 5)

$$L = \sum_{i=1}^n (t_L)_{ci}$$

$(t_L)_{ci}$  = total lost time for critical lane group  $i$ , in seconds

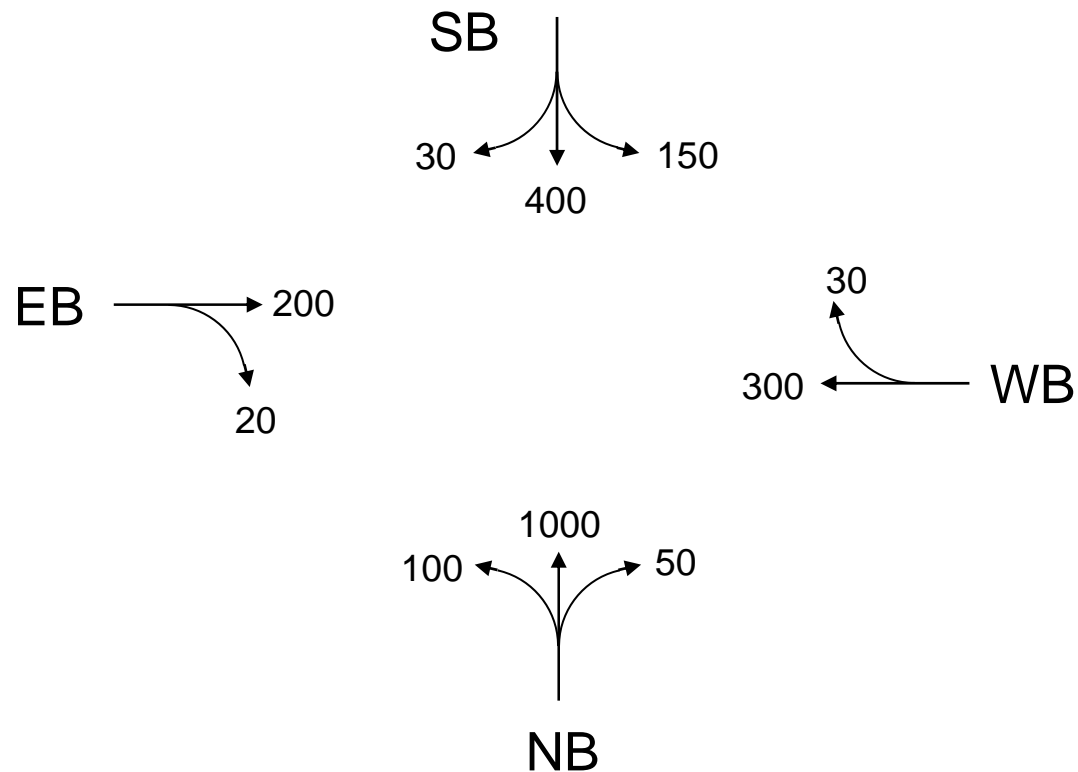
$n$  = number of critical lane groups

- Assume the total lost time for each critical lane group (or phase) is 4 seconds

# EXAMPLE

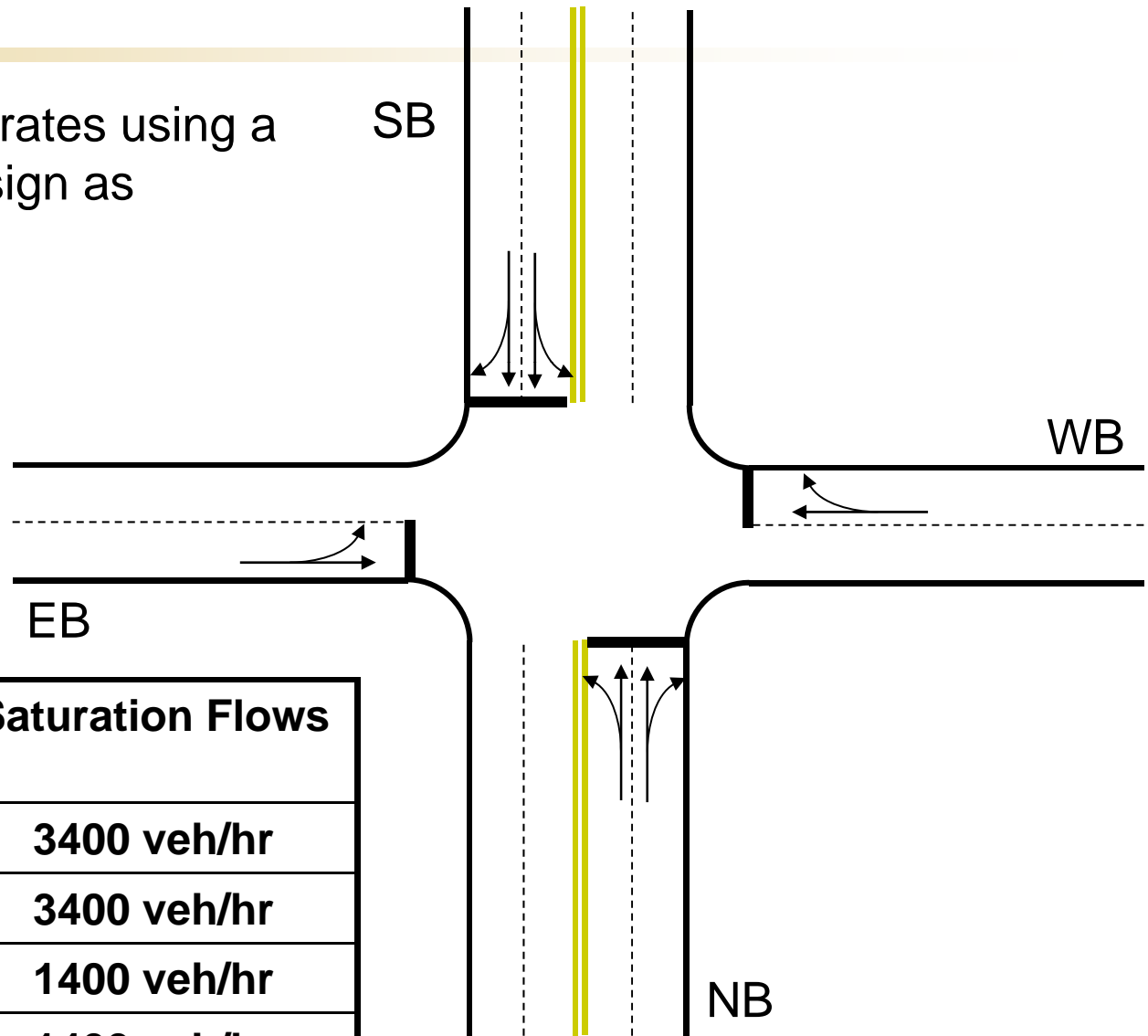
What is the sum of the flow ratios for the critical lane groups ( $Y_c$ )?

What is the total lost time for a signal cycle assuming 2 seconds of clearance lost time and 2 seconds of startup lost time per phase?



# EXAMPLE

An intersection operates using a simple 3-phase design as pictured.



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1	SB	3400 veh/hr
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# EXAMPLE

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# EXAMPLE

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## 5. Calculate Cycle Length

- Minimum cycle length

$$C_{\min} = \frac{L \times X_c}{X_c - \sum_{i=1}^n \left( \frac{v}{s} \right)_{ci}}$$

$C_{\min}$  = estimated minimum cycle length (seconds)

$L$  = total lost time per cycle (seconds), 4 seconds per phase is typical

$(v/s)_{ci}$  =  $Y_c$  = flow ratio for critical lane group,  $i$  (seconds)

$X_c$  = critical v/c ratio for the intersection

## 5. Calculate Cycle Length

- $X_c$ , the critical v/c ratio, indicates the desired degree of intersection utilization
- $X_c = 1.0$  would mean the intersection operates a full capacity, *which is desired but not practical*
- Therefore, often values less than 1 are assumed for  $X_c$  (such as **0.90**)
- $C_{\min}$  formula calculates the minimum cycle length needed for the intersection to operate at the given capacity utilization, *but does not necessarily minimize delay*

## 5. Calculate Cycle Length

- Calculate the cycle length to minimize delay using:

$$C_{opt} = \frac{1.5(L) + 5}{1 - \sum_{i=1}^n \left( \frac{v}{s} \right)_{ci}}$$

$C_{opt}$  = estimated optimum cycle length (seconds) to minimize vehicle delay

$L$  = total lost time per cycle (seconds), 4 seconds per phase is typical

$(v/s)_{ci}$  = flow ratio for critical lane group,  $i$  (seconds)

## 5. Calculate Cycle Length

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- Round  $C$  up to the nearest 5 seconds
- Which  $C$  should we use???
  - In practice, an engineer would test out both cycle lengths in the field to see which works “better”
  - In this example and in the homework, lets just use  $C_{\min}$

# EXAMPLE

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Calculate both an optimal cycle length and a minimum cycle length

## 6. Allocate Green Time

- Decide how much green time should be allotted to each phase

$$g_i = \left( \frac{v}{s} \right)_i \left( \frac{C}{X_c} \right)$$

$g$  = effective green time for phase,  $i$  (seconds)

$(v/s)_i$  = flow ratio for lane group,  $i$  (seconds)

$C$  = cycle length (seconds)

$X_c$  = v/c ratio

- There will be a  $g$  value for each phase

## 6. Allocate Green Time

- Used a desired  $X_c$  to calculate  $C_{\min}$ , but then rounded up  $C_{\min}$
- Recalculate  $X_c$  using:

$$X_c = \frac{\sum_{i=1}^n \left( \frac{v}{s} \right)_i \times C}{C - L}$$

# EXAMPLE

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**Determine the green times allocation (assume  $C=70$  seconds)**



# EXAMPLE

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# Steps 7 and 8

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- **Calculate change and clearance intervals**
  - In other words, find the yellow (Y) and all-red (AR) times
  - Based on how long (distance) it takes a vehicle to safely stop
- **Check pedestrian crossing time**
  - Make sure there is adequate crossing time
- **Sections 7.5.7-7.5.8**
- **Simple plug and chug formulas**

# Level of Service (LOS) Analysis

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- Based on control delay measure
- Applies to both signalized and not signalized intersections
- Referred to as signal delay for a signalized intersection
- Total delay experienced by the driver as a result of the control
- Includes deceleration time, queue move-up time, stop time, and acceleration time

# Signalized Intersection LOS

- **Based on control delay per vehicle**
  - How long you wait, on average, at the stop light

EXHIBIT 16-2. LOS CRITERIA FOR SIGNALIZED INTERSECTIONS

LOS	Control Delay per Vehicle (s/veh)
A	$\leq 10$
B	> 10–20
C	> 20–35
D	> 35–55
E	> 55–80
F	> 80

from *Highway Capacity Manual 2000*

- **LOS determination approach:**  
**Lane group → Approach → Intersection**

# Typical Approach (from HCM)

- **Split control delay into three parts**
  - **Part 1**: Delay calculated assuming uniform arrivals ( $d_1$ ) (this is essentially a D/D/1 analysis)
  - **Part 2**: Delay due to random arrivals ( $d_2$ )
  - **Part 3**: Delay due to initial queue at start of analysis time period ( $d_3$ )

$$d = d_1(PF) + d_2 + d_3$$

$d$  = Average signal delay per vehicle in s/veh

$PF$  = progression adjustment factor

$d_1, d_2, d_3$  = as defined above

# Uniform Delay ( $d_1$ )

$$d_1 = \frac{0.5C \left(1 - \frac{g}{C}\right)^2}{1 - \left[ \min(1, X_c) \frac{g}{C} \right]}$$

$d_1$  = delay due to uniform arrivals (s/veh)

$C$  = cycle length (seconds)

$g$  = effective green time for lane group (seconds)

$X_c$  = v/c ratio for lane group

- **PF accounts for the effect of signal progression on quality of delay**
- **Use PF = 1**

# Incremental/Random Delay ( $d_2$ )

$$d_2 = 900T \left[ (X_c - 1) + \sqrt{(X_c - 1)^2 + \frac{8kIX_c}{cT}} \right]$$

$d_2$  = delay due to random arrivals (s/veh)

$T$  = duration of analysis period (hours). If the analysis is based on the peak 15-min flow then  $T = 0.25$ , if flow based on the peak 1-hr flow then  $T = 1$  hr...

$k$  = delay adjustment factor that is dependent on signal controller mode. For pretimed intersections  $k = 0.5$ . For more efficient intersections  $k < 0.5$ .

$I$  = upstream filtering/metering adjustment factor. Adjusts for the effect of an upstream signal on the randomness of the arrival pattern.  $I = 1.0$  for completely random.  $I < 1.0$  for reduced variance.

$c$  = lane group capacity (veh/hr)

$X_c$  = v/c ratio for lane group

# Initial Queue Delay ( $d_3$ )

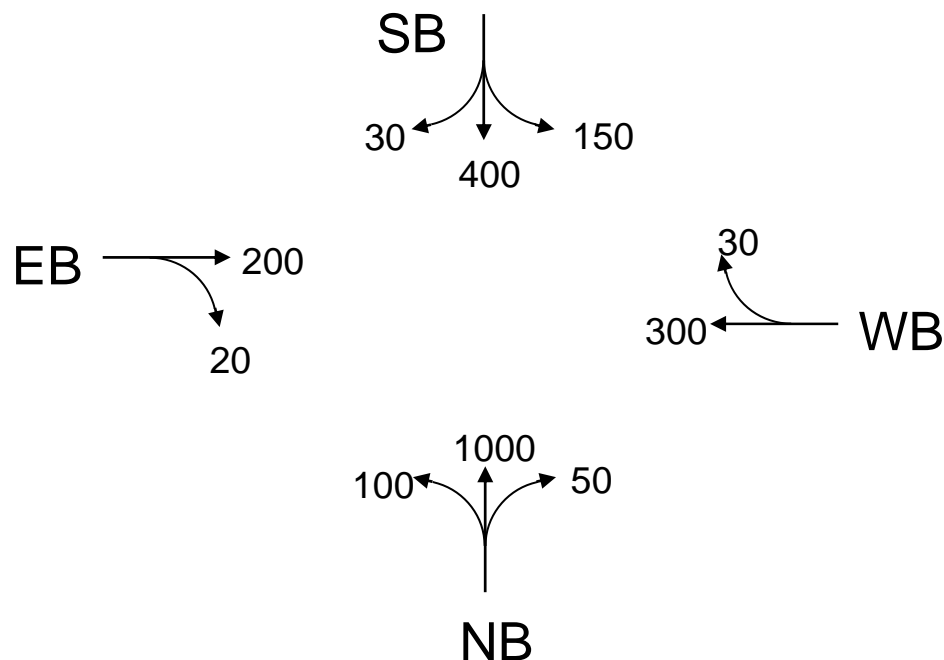
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- Applied in cases where  $X > 1.0$  for the analysis period
  - Vehicles arriving during the analysis period will experience an additional delay because there is already an existing queue
- When no initial queue...
  - $d_3 = 0$



# EXAMPLE

What is the intersection LOS? Assume in all cases that  $PF = 1.0$ ,  $T = 1.0$  (flow based on 1-hr volumes),  $k = 0.5$  (pretimed intersection),  $I = 1.0$  (no upstream signal effects).



Phase	Lane group	Saturation Flows
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1. Calculate delay for each lane group in an approach
2. Calculate delay for each approach in an intersection
3. Calculate delay for the intersection

# EXAMPLE

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**There is only 1 lane group for each approach, therefore lane group delay = approach delay in this example**

**Determine delay for Southbound Approach:**

# EXAMPLE

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- **Northbound Approach**

# EXAMPLE

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- **Eastbound Approach**

# EXAMPLE

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- **Westbound Approach**

# EXAMPLE

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- To get intersection delay, find the weighted average (by flow) of delay for the four approaches