

```

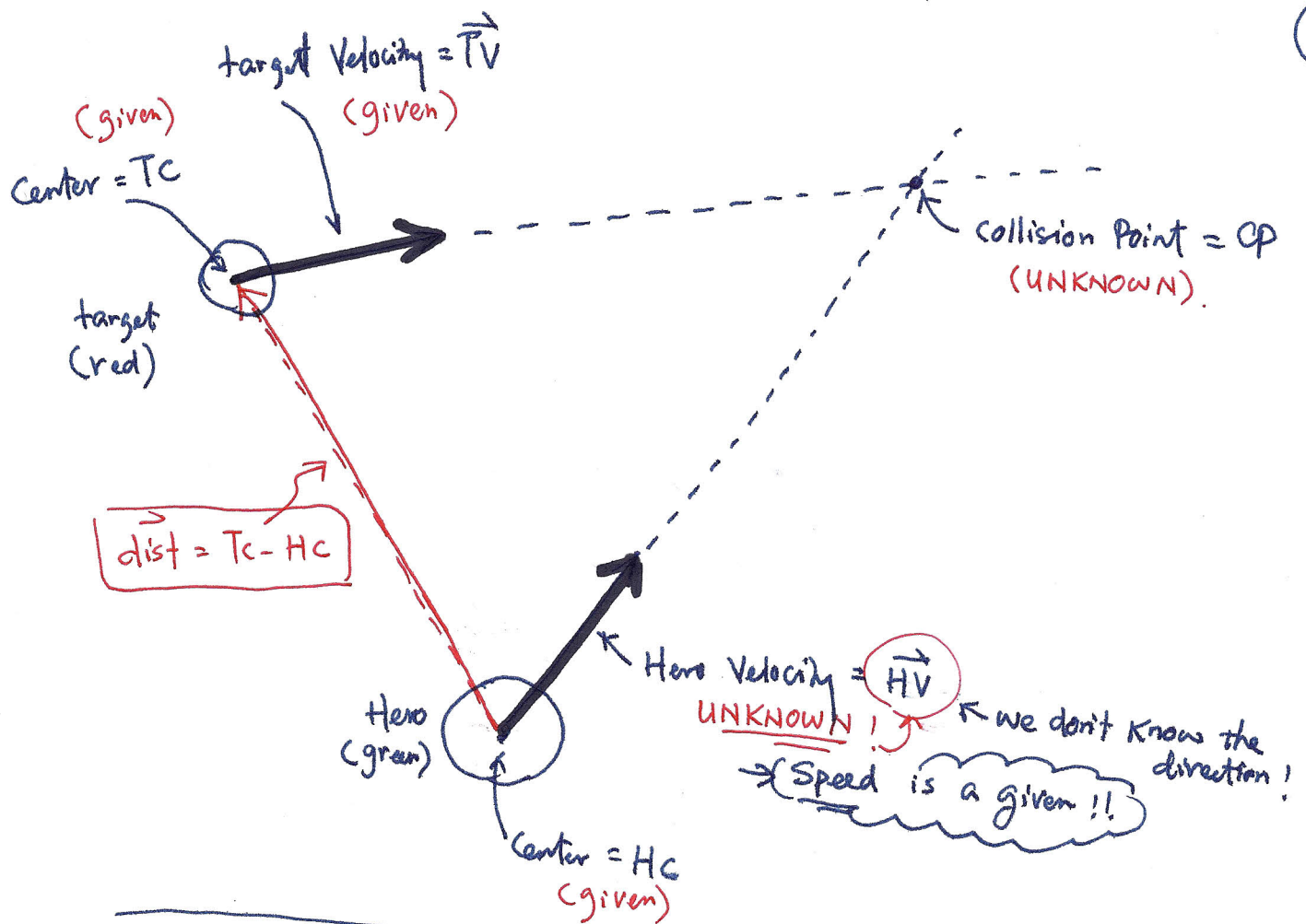
//
// we want:
//     hv - hero velocity (hvx, hvy)
//
// given:
//     hs - hero speed
//     hp - current hero position
//     tv - target velocity (tvx, tvy)
//     tp - current target position
//
// we know:  $hvx \cdot hvx + hvy \cdot hvy = hs \cdot hs$ 
//
// we want to find tm, hvx, hvy such that:
//
//     tpx + tm * tvx = hpx + tm * hvx
//     tpy + tm * tvy = hpy + tm * hvy
//     hvx * hvx + hvy * hvy = hs * hs
//
private float ComputeHeroVDirection()
{
    Vector2 dist = mTheTarget.Center - mTheHero.Center;
    // a * mt * mt + b * mt + c = 0
    float a = mTheTarget.Velocity.LengthSquared() -
              (mTheHero.Speed * mTheHero.Speed);
    float b = 2f * Vector2.Dot(mTheTarget.Velocity, dist);
    float c = dist.LengthSquared();

    mCollidPt.RemoveFromAutoDrawSet();
    float tm = 0f;

    float dm = (b * b) - (4 * a * c);
    if (dm > 0f)
    {
        dm = (float)(Math.Sqrt(dm));
        float t1 = (-b + dm) / (2f * a);
        float t2 = (-b - dm) / (2f * a);
        if (t1 > 0)
        {
            if (t2 > 0)
            {
                tm = (t1 < t2) ? t1 : t2;
            }
            else
            {
                tm = t1;
            }
        }
        else
        {
            if (t2 > 0)
            {
                tm = t2;
            }
        }
        if (tm > 0)
        {
            Vector2 collidPt = mTheTarget.Center + tm * mTheTarget.Velocity;
            Vector2 toHero = collidPt - mTheHero.Center;
            mTheHero.Velocity = (1f / tm) * toHero;

            mCollidPt.Center = collidPt;
            mCollidPt.AddToAutoDrawSet();
        }
    }
    return tm;
}

```



Let $\underline{t_m}$ - time it takes for target to travel to cp

t_m - Hero cp

$$\Rightarrow \left. \begin{aligned} H_c + t_m * \vec{H\vec{V}} &= cp \quad - (1) \\ T_c + t_m * \vec{T\vec{V}} &= cp \quad - (2) \end{aligned} \right\} \Rightarrow \boxed{H_c + \overbrace{t_m}^{\text{unknown}} * \overbrace{\vec{H\vec{V}}}^{\text{Speed is given, Direction is unknown}} = T_c + t_m * \vec{T\vec{V}}}$$

$$\vec{H\vec{V}} = \frac{1}{t_m} [(T_c + t_m \vec{T\vec{V}}) - H_c] \quad - (3)$$

③ is a vector equation.

②

$$\left\{ \begin{array}{l} \text{is actually 2 equations} \end{array} \right. \rightarrow HV = \frac{1}{tm} \left[(TC + tm \vec{TV}) - HC \right] \quad \text{--- ③}$$

$$\left\{ \begin{array}{l} HV.x = \frac{1}{tm} \left[(TC.x + tm \cdot TV.x) - HC.x \right] \quad \text{--- ④} \\ HV.y = \frac{1}{tm} \left[(TC.y + tm \cdot TV.y) - HC.y \right] \quad \text{--- ⑤} \end{array} \right.$$

But we know the Speed of the Hero = (given = S)

$$S = \|\vec{HV}\| = \sqrt{HV.x^2 + HV.y^2}$$

or

$$S^2 = HV.x^2 + HV.y^2 \quad \text{--- ⑥}$$

Substitute ④ + ⑤ into ⑥ :

$$S^2 = \left\{ \frac{1}{tm} [TC.x + tm \cdot TV.x - HC.x] \right\}^2 + \left\{ \frac{1}{tm} [TC.y + tm \cdot TV.y - HC.y] \right\}^2$$

→ The only unknown is tm !!

∴ simplify + collect terms

$$tm^2 \underbrace{(TV.x^2 + TV.y^2 - S^2)}_a + tm \cdot \underbrace{2 \cdot [(TC.x - HC.x)(TV.x) + (TC.y - HC.y)(TV.y)]}_b + \underbrace{(TC.x - HC.x)^2 - (TC.y - HC.y)^2}_c = 0$$

$$\left. \begin{array}{l} a \cdot tm^2 + b \cdot tm + c = 0 \end{array} \right\} \begin{array}{l} a = TV.length()^2 - S^2 \\ b = (dist \cdot TV) \cdot 2 \\ c = (dist.length)^2 \end{array}$$