Stand Attributes and Stand Sampling Techniques PROBLEM SET 3 – Due 17 Feb 2016

- 1. <u>Stand Attributes.</u> Some information measured on a 0.1-acre fixed-area plot randomly located in a stand from a forest under your care is available (Table 1). Compute and report the following stand attribute descriptors to characterize present conditions.
 - a. number of trees per acre
 - b. stand basal area per acre
 - c. mean diameter, quadratic mean diameter
 - d. Stand Density Index (SDI), relative SDI, and Curtis' Relative Density (RD)
 - e. Mean height, Lorey's height, H40 (avg. height of 40 largest diameter trees per acre)
 - f. species composition, using tree frequency first, then using basal area as the basis
 - g. If stand b.h. age is 31 yr., what is Site Index according to King? Site Class? (Remember: For King's curves use only Douglas-fir trees to compute dominant height defined as the average height of trees in the 80th or higher percentile by DBH)

Challenges 2 & 3 are based on Figure 1, a "map" of a 40-acre "forest" exhaustively divided up into 0.10-acre plots. The numbers appearing in each "plot" represent 100's of bd-ft. on that plot.

- Systematic sampling. Use a random number generator to pick a starting plot for a 25 plot systematic sample with a random start. Mark the systematically selected plots on the map (Figure 1) and append it to your answer sheet. Compute mean volume **per acre**, its standard error, and a 90% confidence interval. Compute the observed margin of error, E (the half-width of the confidence interval), you observed. From this, find observed percent error (E%).
- 3. <u>Sample size calculation</u>. Find the sample size necessary to achieve an allowable error, E%, of the same size as was observed as in (2), but instead using 70% confidence. Explain how your computed sample size compares with n = 25 from question (2).
- 4. <u>Ratio Estimation</u>. Weight scaling of sawlogs. We want to estimate the total volume of N truckloads of timber removed from a particular timber sale. Each truckload of logs has to be weighed (W in pounds) to pay the truckers, so we randomly sample n= 4 (*) of the N = 10 truckloads and scale the logs for board foot volume (V in BF). The data follow:

| Load: | 1 | 2* | 3 | 4* | 5 | 6* | 7 | 8* | 9 | 10 |
|----------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| W (lbs): | 51,000 | 43,600 | 68,000 | 60,000 | 52,000 | 49,400 | 56,000 | 63,000 | 48,000 | 54,000 |
| V (BF): | _ | 5,000 | - | 5,600 | - | 5,800 | _ | 6,400 | - | - |

Derive an estimate for total volume using the ratio-of-means and a 90% confidence interval.

- 5. <u>Double Sampling.</u> [*Extra Credit.*] A very homogenous longleaf pine stand was systematically sampled using a sample size of six 1-acre plots and resulted in the data appearing in Table 2.
 - a. What is the estimate of volume per acre from this systematic sample?
 - b. Calculate the standard error of the estimate in part a.
 - c. Now suppose that as part of the sampling tree counts only were obtained on ten additional plots. The number of trees observed on these plots is as follows:

7, 11, 10, 7, 8, 10, 8, 6, 10, 5.

What is the double-sampling estimate of volume per acre?

- d. Calculate the standard error of the estimate in part c.
- e. How do the two standard errors (from b and from d) compare? What is the relative efficiency of double sampling compared to systematic sampling for this case?

| PLT | SPP. | DBH (in.) | <u> </u> |
|-----|------|-----------|----------|
| 1 | 202 | 5.5 | 45.8 |
| 1 | 202 | 5.6 | 45.8 |
| | | | |
| 1 | 202 | 6.8 | 56.7 |
| 1 | 202 | 7.5 | 62.5 |
| 1 | 202 | 7.7 | 64.2 |
| 1 | 202 | 8.8 | 73.3 |
| 1 | 202 | 9 | 75 |
| 1 | 202 | 9.2 | 76.7 |
| 1 | 202 | 10.2 | 85 |
| 1 | 202 | 10.2 | 85 |
| 1 | 202 | 10.5 | 87.5 |
| 1 | 202 | 10.6 | 88.3 |
| 1 | 202 | 11.4 | 95 |
| 1 | 202 | 11.5 | 95.8 |
| 1 | 202 | 11.5 | 95.8 |
| 1 | 202 | 11.5 | 95.8 |
| 1 | 202 | 11.8 | 98.3 |
| 1 | 202 | 12.1 | 100.8 |
| 1 | 202 | 12.5 | 104.2 |
| 1 | 202 | 12.8 | 106.7 |
| 1 | 202 | 12.8 | 106.7 |
| 1 | 202 | 14.1 | 117.5 |
| 1 | 202 | 14.3 | 119.2 |
| 1 | 202 | 14.9 | 124.2 |
| 1 | 202 | 15.1 | 125.8 |
| 1 | 351 | 4.5 | 37.5 |
| 1 | 351 | 5.1 | 42.5 |
| 1 | 351 | 5.4 | 45 |
| 1 | 351 | 6.5 | 54.2 |
| 1 | 351 | 6.8 | 56.7 |
| 1 | 351 | 11.5 | 95.8 |
| 1 | 492 | 5.8 | 48.3 |
| 1 | 492 | 6.5 | 54.2 |
| 1 | 920 | 4.7 | 39.2 |
| 1 | 920 | 4.9 | 40.8 |
| 1 | 920 | 5.2 | 43.3 |

Table 1. Data from a 1/10-acre, fixed-area, circular plot (PLT) no. 1, in a 2nd-growth Douglas-fir forest. (NOTE: SPP = 202 is Douglas-fir, 492 is Pacific dogwood, 351 is red alder, 920 is willow)

Table 2. PLT refers to plot, No. Trees is the number of trees measured on the plot, Vol/ac refers to cubic-foot volume of longleaf pine trees.

| | | / I |
|-----|----------|--------|
| PLT | No.Trees | Vol/ac |
| 1 | 10 | 3523 |
| 2 | 7 | 2546 |
| 3 | 6 | 2201 |
| 4 | 9 | 3458 |
| 5 | 9 | 3520 |
| 6 | 9 | 3404 |

Measured volume on 0.1-acre plots in a 40 acre forest tract

(in 100 boardfeet)

| | _ | | | | | | | | | | | | | | | | | | |
|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|
| 22 | 26 | 26 | 19 | 34 | 18 | 17 | 25 | 20 | 28 | 0 | 0 | 2 | 0 | 6 | 0 | 3 | 0 | 0 | 4 |
| 21 | 18 | 23 | 22 | 28 | 24 | 33 | 36 | 23 | 15 | 17 | 0 | 2 | 11 | 15 | 0 | 17 | 5 | 2 | 8 |
| 30 | 28 | 23 | 21 | 29 | 18 | 14 | 30 | 25 | 28 | 20 | 14 | 8 | 1 | 15 | 2 | 5 | 0 | 0 | 4 |
| 28 | 19 | 21 | 20 | 26 | 20 | 38 | 23 | 20 | 27 | 24 | 11 | 6 | 4 | 0 | 5 | 5 | 9 | 2 | 5 |
| 17 | 14 | 20 | 26 | 25 | 22 | 22 | 19 | 15 | 20 | 25 | 26 | 15 | 9 | 12 | 0 | 0 | 16 | 8 | 5 |
| 38 | 42 | 37 | 39 | 22 | 44 | 47 | 17 | 25 | 29 | 34 | 39 | 20 | 24 | 14 | 10 | 12 | 1 | 0 | 0 |
| 43 | 34 | 23 | 46 | 47 | 46 | 39 | 35 | 31 | 30 | 24 | 35 | 23 | 26 | 18 | 25 | 21 | 12 | 5 | 1 |
| 36 | 45 | 47 | 36 | 35 | 29 | 49 | 44 | 31 | 42 | 33 | 47 | 31 | 28 | 15 | 18 | 20 | 23 | 9 | 12 |
| 38 | 48 | 42 | 51 | 17 | 54 | 47 | 52 | 30 | 34 | 30 | 46 | 24 | 12 | 21 | 12 | 32 | 29 | 27 | 16 |
| 17 | 24 | 45 | 47 | 52 | 28 | 43 | 45 | 46 | 27 | 40 | 32 | 51 | 28 | 25 | 41 | 20 | 27 | 14 | 21 |
| 47 | 56 | 43 | 37 | 30 | 60 | 56 | 43 | 29 | 33 | 41 | 30 | 30 | 20 | 15 | 18 | 20 | 23 | 13 | 28 |
| 38 | 36 | 27 | 38 | 24 | 31 | 48 | 32 | 25 | 31 | 35 | 31 | 22 | 15 | 10 | 24 | 22 | 19 | 18 | 16 |
| 46 | 54 | 34 | 46 | 37 | 43 | 44 | 34 | 25 | 44 | 43 | 40 | 28 | 14 | 26 | 33 | 18 | 34 | 17 | 31 |
| 47 | 47 | 35 | 40 | 39 | 39 | 50 | 28 | 50 | 36 | 44 | 27 | 16 | 21 | 36 | 17 | 27 | 21 | 33 | 31 |
| 22 | 37 | 11 | 29 | 28 | 33 | 29 | 35 | 53 | 18 | 26 | 20 | 29 | 12 | 23 | 25 | 15 | 17 | 26 | 21 |
| 37 | 22 | 20 | 22 | 14 | 29 | 25 | 21 | 30 | 31 | 27 | 16 | 21 | 36 | 17 | 27 | 21 | 17 | 14 | 12 |
| 18 | 25 | 26 | 20 | 27 | 26 | 26 | 22 | 19 | 30 | 15 | 2 | 7 | 3 | 4 | 15 | 9 | 7 | 0 | 3 |
| 22 | 34 | 37 | 17 | 24 | 28 | 26 | 25 | 30 | 33 | 18 | 6 | 0 | 3 | 0 | 0 | 6 | 5 | 7 | 6 |
| 13 | 28 | 27 | 27 | 31 | 20 | 21 | 21 | 16 | 27 | 12 | 0 | 17 | 3 | 1 | 1 | 0 | 0 | 0 | 5 |
| 32 | 31 | 30 | 22 | 16 | 26 | 8 | 32 | 19 | 22 | 3 | 3 | 0 | 0 | 0 | 2 | 0 | 5 | 10 | 2 |

Figure 1. "Map" of example population for use in designing a SYStematic sample (SYS) survey with random start.