## Association Mapping

- Mendelian versus Complex Phenotypes
- How to Perform an Association Study
- Why Association Studies (Can) Work
- Introduction to LOD score analysis


## Common theme: linking genotype \& phenotype



Mutant identified in a model organism

segregating a trait


Protein acting in a biological process


946 ATT GTC TGT $A G C$ CGA TTG GAG GAG TAC AAC AGC CAT 1009 GGA CCT TTA CGG CGT AAT CCT GGA AAC CAT GAC AAA 1072 GCT GAT GTA GAA TTT TGC CTG AGT TTG ACC CAA TAT 1135 AAT TTC AGC TTT AGA AAT ACA CTG GAA GGA TTT GCT 1198 TCT CAA AGC AGC ATG CAC AAT GCC TTG CAC ATC TAT 1261 GGA TCT GCC AAC GAT CCT ATC TTC CTT CTT CAC CAT 1324 TGG CTC CGA AGG CAC CGT CCT CTT CAA GAA GTT TAT

## Mendelian Phenotypes



- Single gene
- Follows clear patterns of Mendelian Inheritance
- Strong relationship (correlation) between genotype and phenotype


## Complex (aka "multifactorial") Phenotypes



- Multiple genes
- Familial aggregation, but no clear pattern of Mendelian Inheritance
- Weak relationship (correlation) between genotype and phenotype


## Complications of Genotype-Phenotype Relationship

Expressivity and penetrance can vary
Fraction of individuals with a genotype exhibit the phenotype expected of that genotype
The degree to which a genotype is expressed - e.g., different individuals inheriting the same disease gene may be affected to different extents

Important Concept: disease causing -vs- susceptibility alleles

## Complications of Genotype-Phenotype Relationship



Hydrangea

The genotype is an indication of the potential phenotype. The actual phenotype depends on the environment also.

## Why Are We Talking About Association Studies?



Frequency
modified from D. Altschuler

## How Do We Measure Effect Size?

Effect size - measure of how much familial aggregation is seen for a trait (disease) of interest

Familial relative risk measures the risk of disease in someone with an affected relative compared to the risk of the general population

$$
\lambda_{S}=\underline{\mathrm{P}(\text { sib } 2 \text { has a disease } \mid \text { sib } 1 \text { has the disease })}
$$

P (diseased individual in the general population)

## Example: $\lambda_{\mathrm{S}}$ (Sibling relative risk) of Cystic Fibrosis

CF is a rare autosomal recessive mendelian disease

## Population frequency ~8/100,000

What is the $\lambda_{S}$ of CF?


$$
\begin{aligned}
\lambda_{S} & =\frac{\mathrm{P}(\text { sib } 2 \text { has a disease } \mid \text { sib } 1 \text { has the disease })}{\mathrm{P}(\text { diseased individual in the general population })} \\
& =\frac{1 / 4}{8 / 100,000}
\end{aligned}
$$

$$
=3,125
$$

## $\lambda_{s}$ of Some Complex Diseases



## Complex Diseases Have Proven Refractory to Linkage Analysis



## Association Studies

- Population based gene mapping method
- Collect unrelated individuals with a disease (cases) and individuals without a disease (controls)
- Goal is to find an association between marker alleles and disease


## A Simple Association Study



## What is the genetic basis of the frowny faced gingerbread man (FFGM) disease?

1. Collect FFGM cases from the population

2. Collect controls from the population


## A Simple Association Study

3. Genotype a genetic marker of interest (SNP1) in:


## A Simple Association Study

4. Compare frequency in cases and controls


How Can We Determine Significance?

$2 \times 2$ "Contingency Table"
A case for our old friend $\chi^{2}=\sum \frac{(0-E)^{2}}{E}$

## What is the Expectation? What's the Null Hypothesis?

6 Cases 6 Controls
12 Calleles 12 Talleles


## Calculating $\chi^{2}$ for an Association Study



## Calculating $\chi^{2}$ for an Association Study



## Calculating $\chi^{2}$ for an Association Study

|  |  | Cases | Controls |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | c | 9 | 3 | 12 |  |
|  | T | 3 | 9 | 12 |  |
|  |  | 12 | 12 | 24 |  |
|  | Obs |  | Exp | (0-E) ${ }^{2}$ | (0-E) ${ }^{2} / \mathrm{E}$ |
| Cases C | 9 | (12 | 2)/24 $=6$ | 9 | 1.5 |
| Cases T | 3 | (12 | 2)/24 $=6$ | 9 | 1.5 |
| Controls C | 3 | (12 | 2)/24 $/ 2$ | -9 | 1.5 |
| Controls T | 9 | (12) | 2)/24 $/ 2$ | - 9 | 1.5 |
|  |  |  |  |  | $\chi^{2}=6.0$ |

$\chi^{2}$ table

| P | 0.995 | 0.975 | 0.900 | 0.500 | 0.100 | 0.050 | 0.025 | 0.010 | 0.005 |  |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| df |  |  |  |  |  |  |  |  |  |  |
| 1 | 0.000 | 0.000 | 0.016 | 0.455 | 2.706 | 3.841 | 5.02 | 6.635 | 7.879 |  |
| 2 | 0.010 | 0.051 | 0.211 | 1.386 | 4.605 | 5.991 | 7 | 78 | 9.210 | 10.597 |
| 3 | 0.072 | 0.216 | 0.584 | 2.366 | 6.251 | 7.815 | 9.348 | 11.345 | 12.838 |  |
| 4 | 0.207 | 0.484 | 1.064 | 3.357 | 7.779 | 9.488 | 11.143 | 13.277 | 14.860 |  |
| 5 | 0.412 | 0.831 | 1.610 | 4.351 | 9.236 | 11.070 | 12.832 | 15.086 | 16.750 |  |
| 6 | 0.676 | 1.237 | 2.204 | 5.348 | 10.645 | 12.592 | 14.449 | 16.912 | 18.548 |  |
|  |  |  |  |  |  |  |  |  |  |  |

## What does this $\mathbf{P}$ value mean?

Would expect a deviation from the hypothesis of this magnitude (from chance alone) about $1 \%$ of the time

Therefore, reject the null hypothesis (boo-ya)

## Why Do Genetic Association Studies Work?

- SNP1 is associated with FFGM

C allele more frequent in FFGM cases compared to controls

- Does this mean the C allele causes FFGM?

No - it could just be on the same haplotype as the FFGM disease allele

Alleles between two or more loci can be correllated

## Why Genetic Association Studies Work: Part I

| A | C | A |  | A | c | 0 | A |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| A | G | G | FFGM | A | G | d | A |
| T | G | G | $\xrightarrow[\text { Disease }]{ }$ | T | G | d | G |
| A | G | G | Mutation | A | C | d | G |



Mutations arise on particular halotype backgrounds

Creates association among alleles
This is why association studies "work"

Population

## Why Genetic Association Studies Work: Part II



How could we ever map anything if allelic associations extend over a whole chromosome?

## The Case of Linkage -v- Association

What is the primary difference between the concepts of linkage and association?


Linkage: relationship between two or more loci

Association: relationship between the alleles of two or more loci

## Beyond the Basics

## Genome-Wide Association Studies (GWAS)

"A genome-wide perspective of genetic variation in human metabolism"
Nat. Genet. 2009, 42:137
Measured 163 metabolites in 1,809 individuals and performed a GWAS:



## LOD Score Analysis in Humans

Gene mapping in humans
»Mapping using pedigrees-LOD score analysis, haplotype analysis
»Mapping using populations-association studies


## Mapping and cloning human genes

## Based on position "positional cloning"

» Find linkage (or association) of disease gene to a chromosomal landmark (e.g., a polymorphic site)
»Clone the sequences from that region
»Identify candidate genes in that region (does it look like a gene, act like a gene, etc.)
» Tests: are the candidates mutated in disease patients?
» Model organism or tissue culture: If we knock out that gene, do we get the predicted mutant phenotype?

## Linkage mapping of "familial" traits



Li-Fraumeni syndrome: p53 checkpoint defect

## Positional cloning of the BRCA1 gene


(M-C King lab, 1990)


The problem with humans

Stumbling blocks...
» Which polymorphic loci to test?
» Not all meioses are informative
»Pedigrees may be too small to detect linkage with confidence

## Which polymorphic loci to test for linkage?

Don't know ahead of time... so do trial and error!

- look for linkage between the disease and polymorphic site \#1
- then repeat with polymorphic site \# 2
...etc.
A molecular marker map-




Variation in DNA sequence at specific chromosomal locations is mapped
These sites are used as landmarks in
mapping genes



## The problem with humans

Stumbling blocks...
» Which polymorphic loci to test?
» Not all meioses are informative
»Pedigrees may be too small to detect linkage with confidence

Not all matings are informative...

A test for informative vs. non-informative meiosis: can we tell if the gamete was recombinant?

If we can tell: the meiosis is informative

$\left.\begin{array}{l}\text { cannot tell if the gamete } \\ \text { was recombinant }\end{array}\right\} \rightarrow$ non-informative

## Practice question

The two pedigrees show inheritance of an autosomal dominant trait ( $\mathbf{D}=$ disease, dominant; d = normal, recessive). Numbers in \{curly brackets \} indicate alleles of a microsatellite repeat polymorphic locus. For each pedigree, state whether the meiosis in II-1 is informative or uninformative, giving the parental types for II-1 in each case.


## The problem with humans

Stumbling blocks...
» Which polymorphic loci to test?
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Mapping a gene using molecular markers (cont'd)

Stumbling blocks...
» Which polymorphic loci to test?
» Not all meioses are informative
"Pedigrees may be too small to detect linkage with confidence

A solution-
Play the odds: What is more likely to give this pedigree outcome, linkage or non-linkage?

