

Ling 566  
Oct 2, 2006  
Context-Free Grammar

# Overview

- Formal definition of CFG
- Constituency, ambiguity, constituency tests
- Central claims of CFG
- Order independence
- Weaknesses of CFG
- If time: Work through Problems 1 and 4 in Chapter 2

# Context-Free Grammar

- A quadruple:  $\langle C, \Sigma, P, S \rangle$ 
  - $C$ : set of categories
  - $\Sigma$ : set of terminals (vocabulary)
  - $P$ : set of rewrite rules  $\alpha \rightarrow \beta_1, \beta_2, \dots, \beta_n$
  - $S$  in  $C$ : start symbol
- For each rule  $a \rightarrow \beta_1, \beta_2, \dots, \beta_n \in P$   
 $a \in C$ ;  $\beta_i \in C \cup \sigma$ ;  $1 \leq i \leq n$

# A Toy Grammar

## RULES

$S \longrightarrow NP VP$

$NP \longrightarrow (D) A^* N PP^*$

$VP \longrightarrow V (NP) (PP)$

$PP \longrightarrow P NP$

## LEXICON

D: the, some

A: big, brown, old

N: birds, fleas, dog, hunter, I

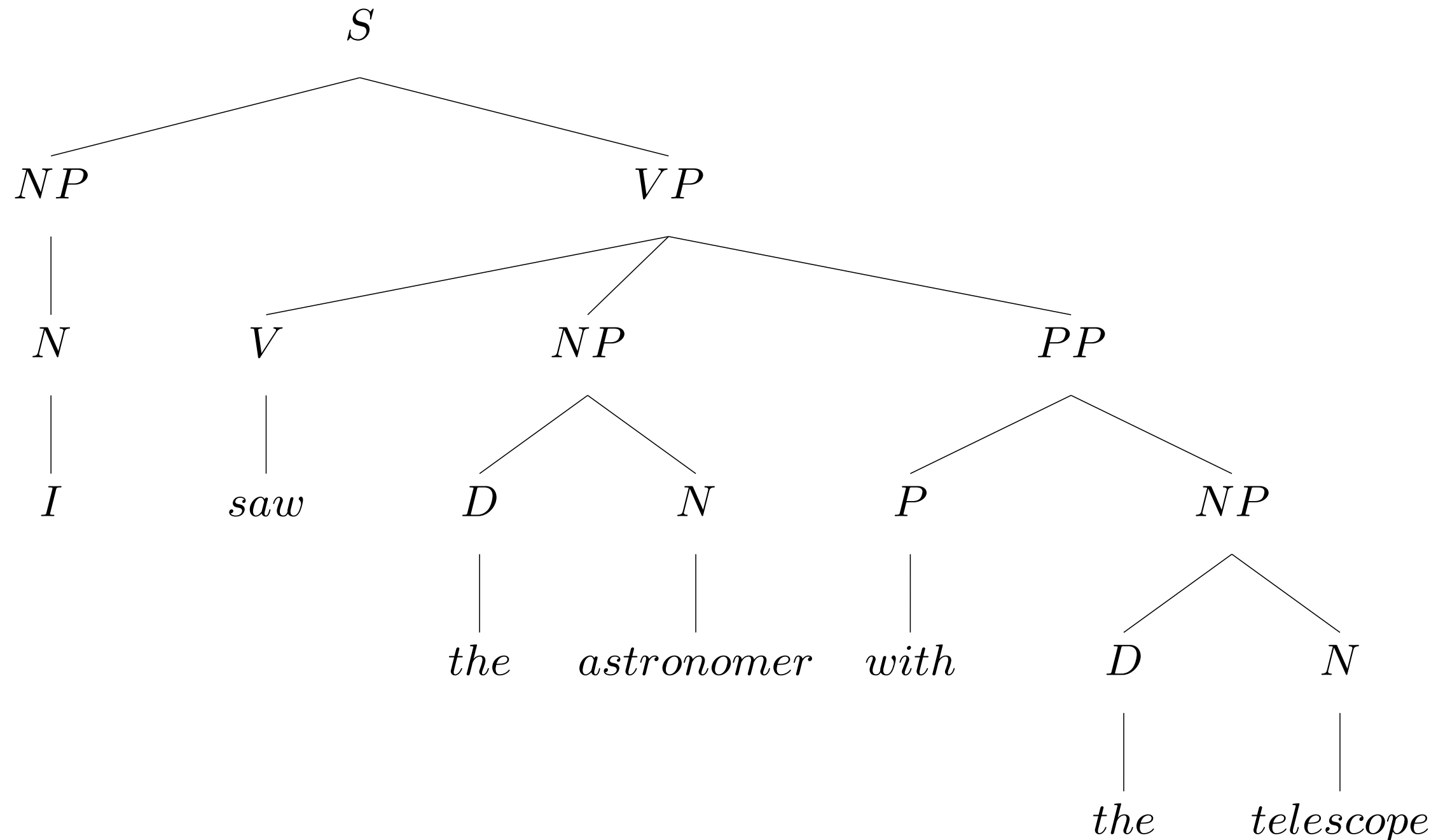
V: attack, ate, watched

P: for, beside, with

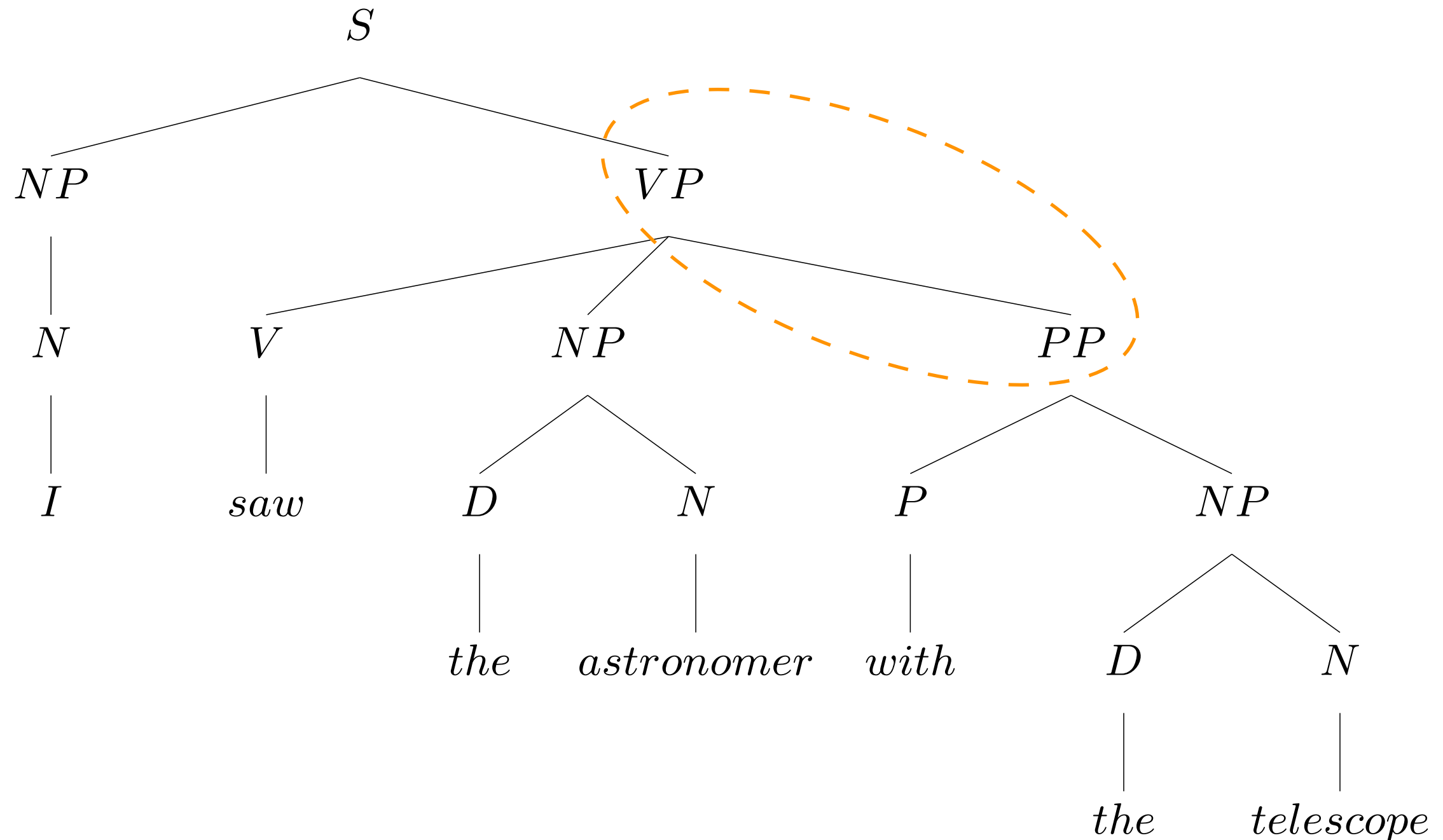
# Structural Ambiguity

I saw the astronomer with the telescope.

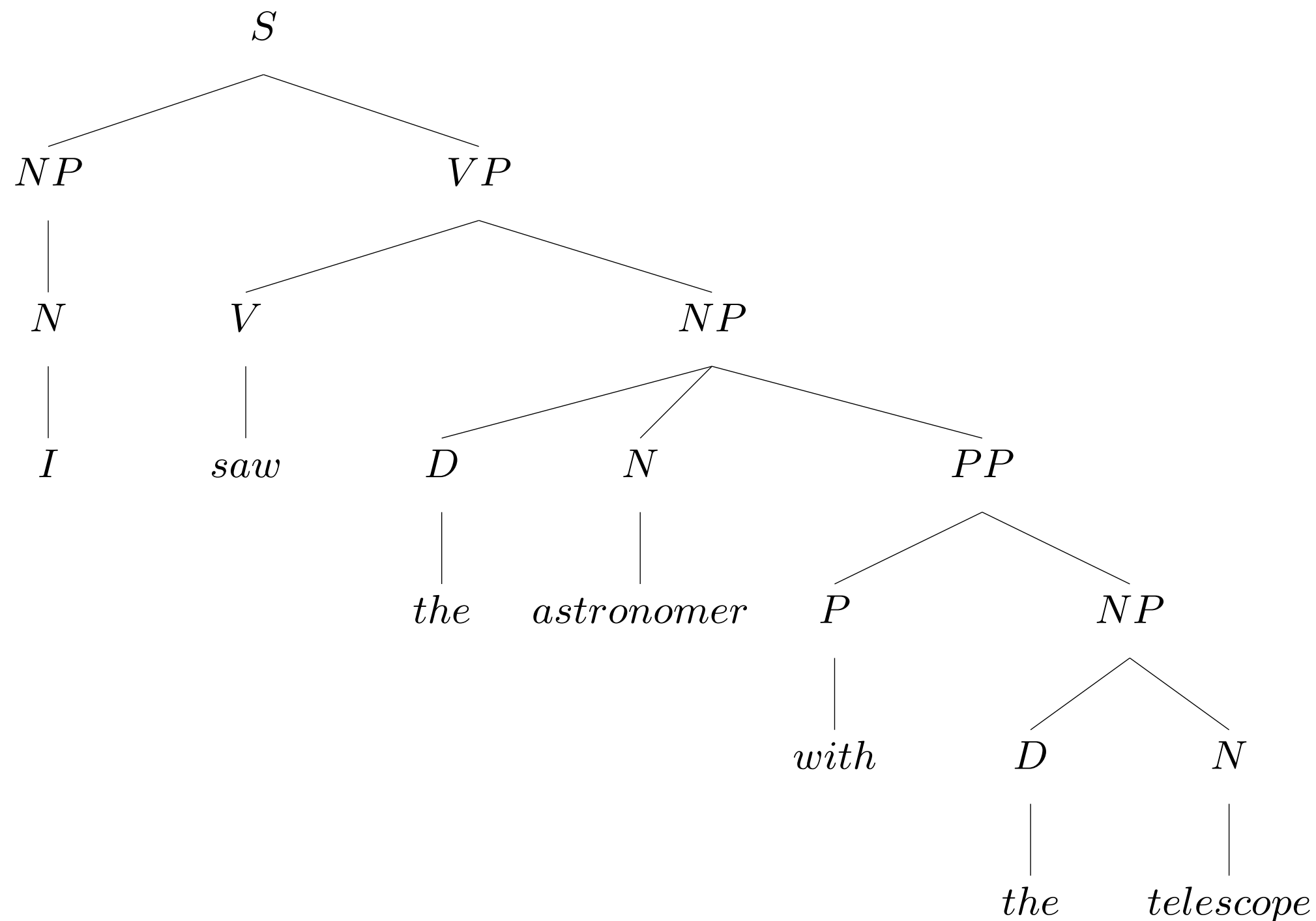
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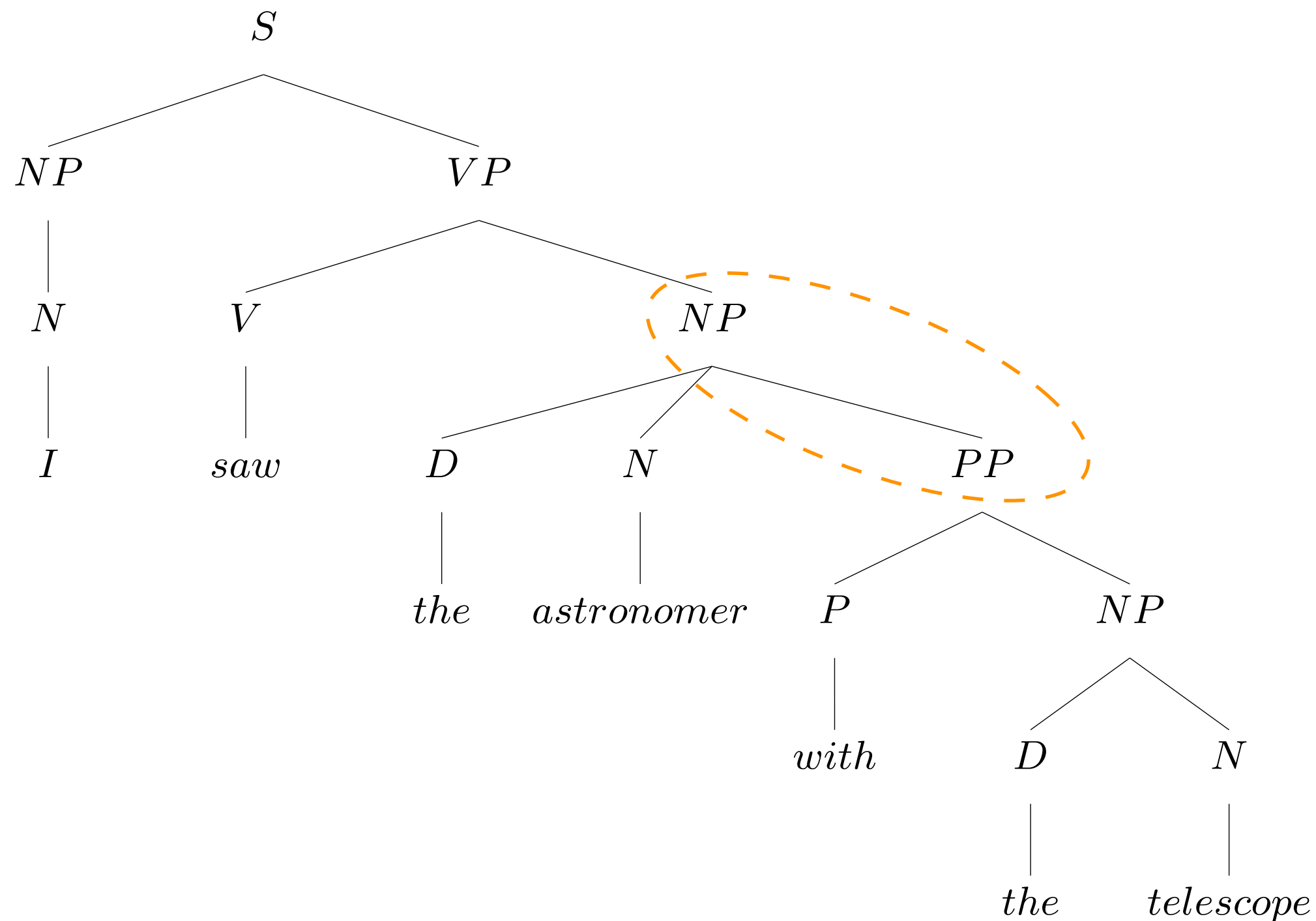


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- Cleft sentences

*It was a book about syntax they were reading.*

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... but they don't always agree.



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3. Two phrases are either disjoint or one fully contains the other (no partially overlapping constituents).
4. What a phrase can consist of depends only on what kind of a phrase it is (that is, the label on its top node), not on what appears around it.

- Claims 1-3 characterize what is called ‘phrase structure grammar’
- Claim 4 (that the internal structure of a phrase depends only on what type of phrase it is, not on where it appears) is what makes it ‘context-free’.
- There is another kind of phrase structure grammar called ‘context-sensitive grammar’ (CSG) that gives up 4. That is, it allows the applicability of a grammar rule to depend on what is in the neighboring environment. So rules can have the form  $A \rightarrow X$ , in the context of  $Y\_Z$ .

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*A technician arrived who could solve the problem.*

- To Claim 3 (no overlapping constituents):

*I read what was written about me.*

- To Claim 4 (context independence):

- *He arrives this morning.*
- *\*He arrive this morning.*
- *\*They arrives this morning.*
- *They arrive this morning.*

# A Trivial CFG

$S \rightarrow NP \ VP$

$NP \rightarrow D \ N$

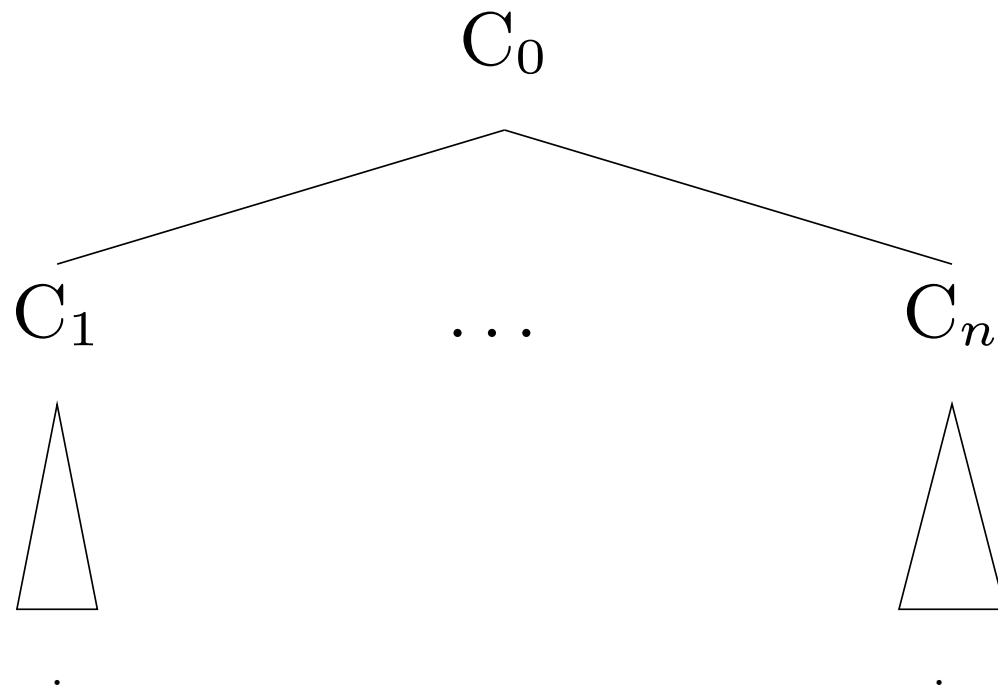
$VP \rightarrow V \ NP$

D: *the*

V: *chased*

N: *dog, cat*

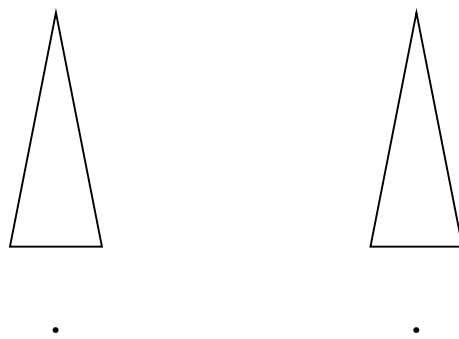
# Trees and Rules



is a well-formed nonlexical tree if (and only if)

$C_n, \dots, C_n$

are well-formed trees, and



$C_0 \rightarrow C_1 \dots C_n$

is a grammar rule.

# Bottom-up Tree Construction

D: *the*

V: *chased*

N: *dog, cat*

D

|

the

V

|

chased

N

|

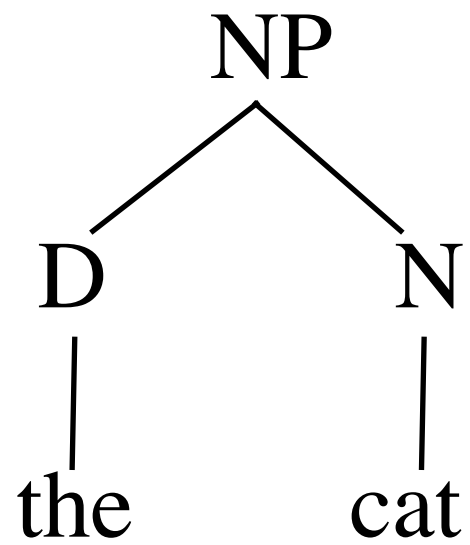
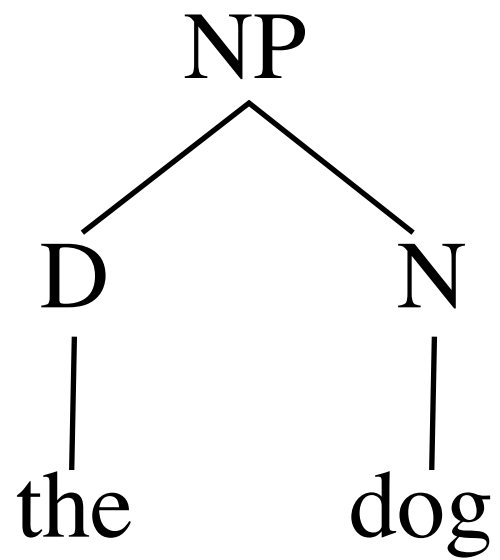
dog

N

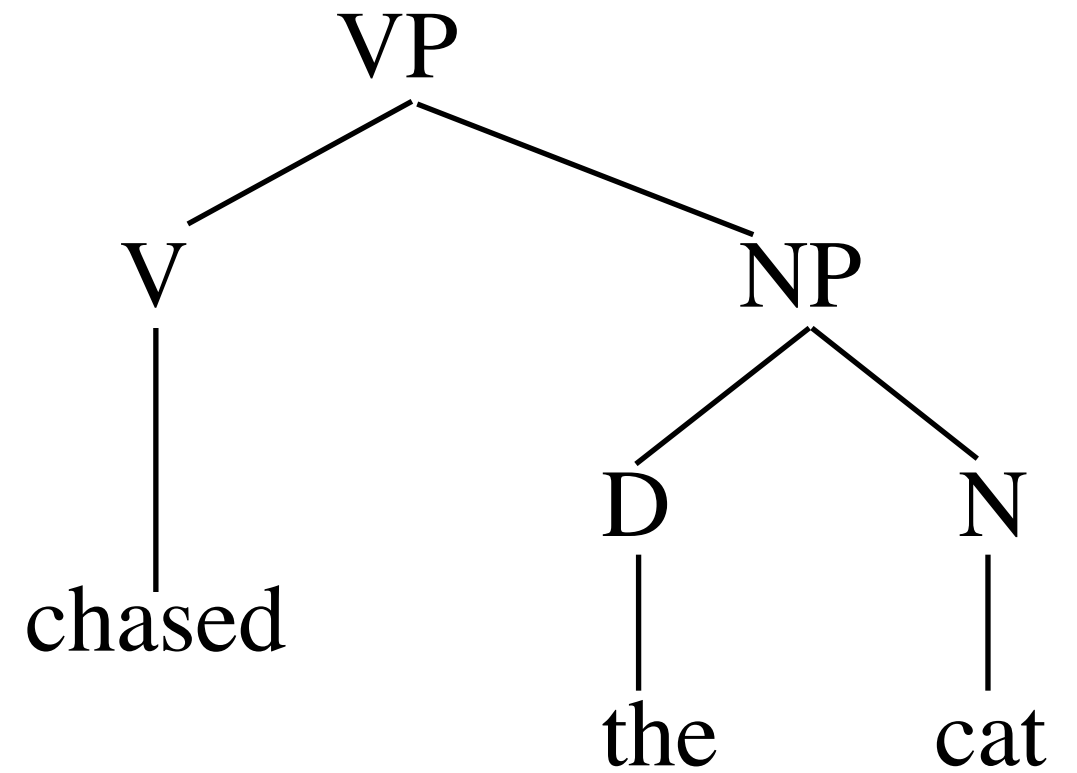
|

cat

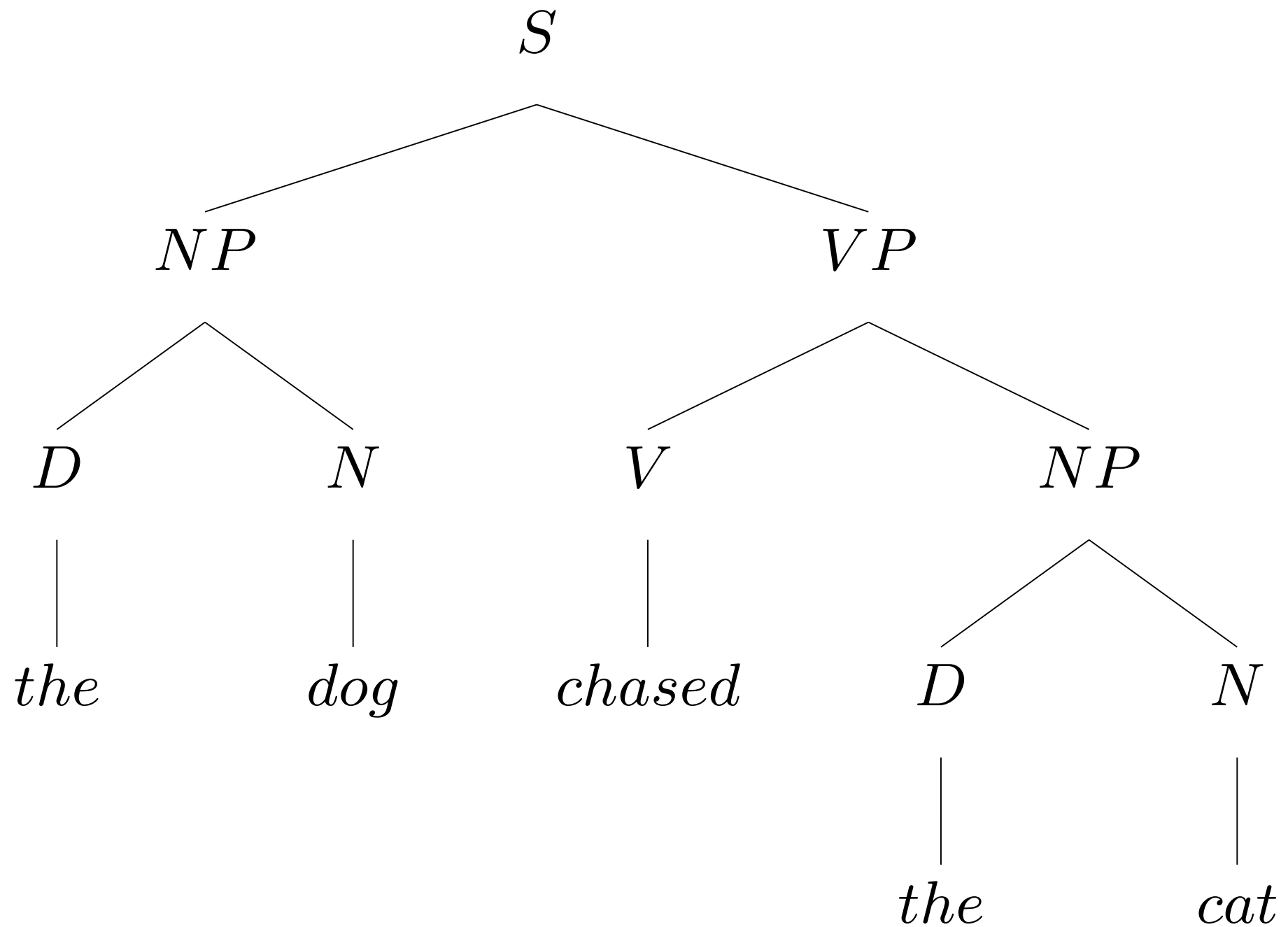
$NP \longrightarrow D \ N$



$VP \longrightarrow V \ NP$

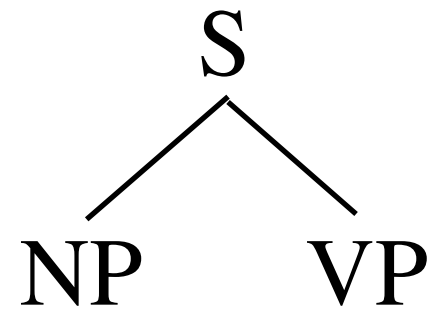


$S \rightarrow NP VP$

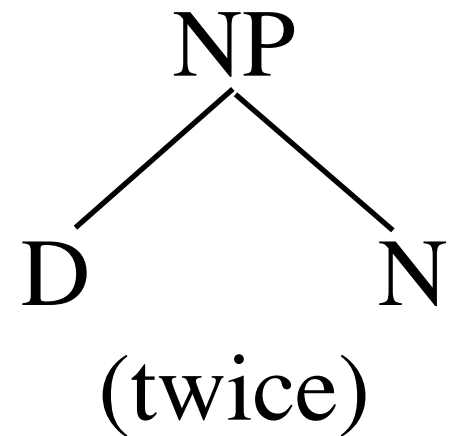


# Top-down Tree Construction

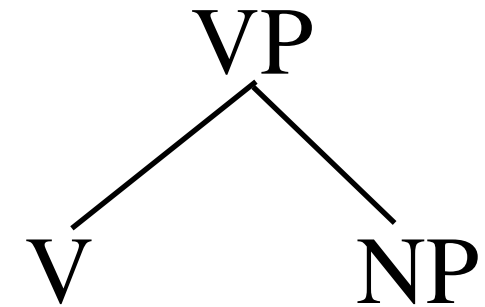
$S \longrightarrow NP \ VP$



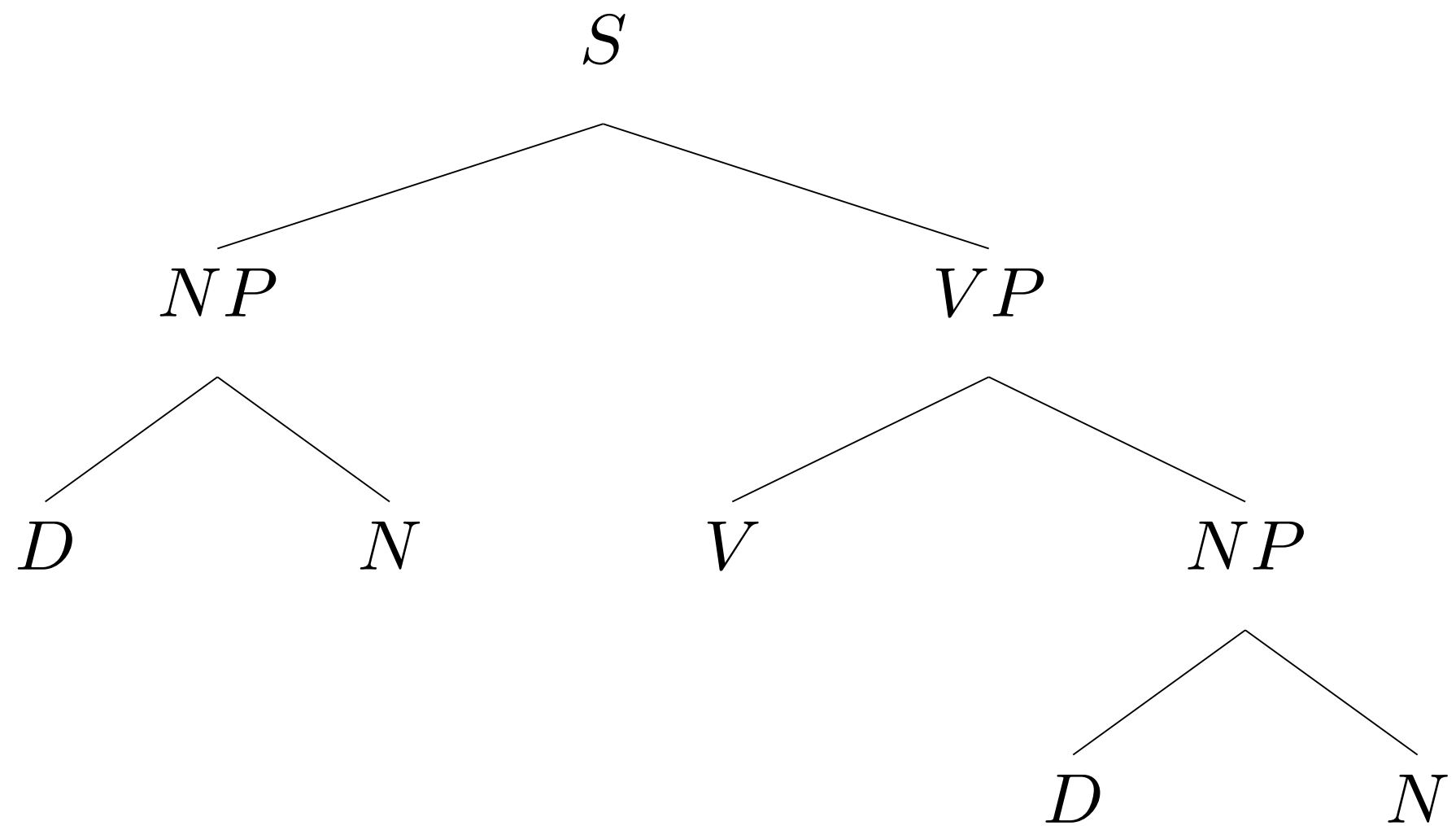
$NP \longrightarrow D \ N$



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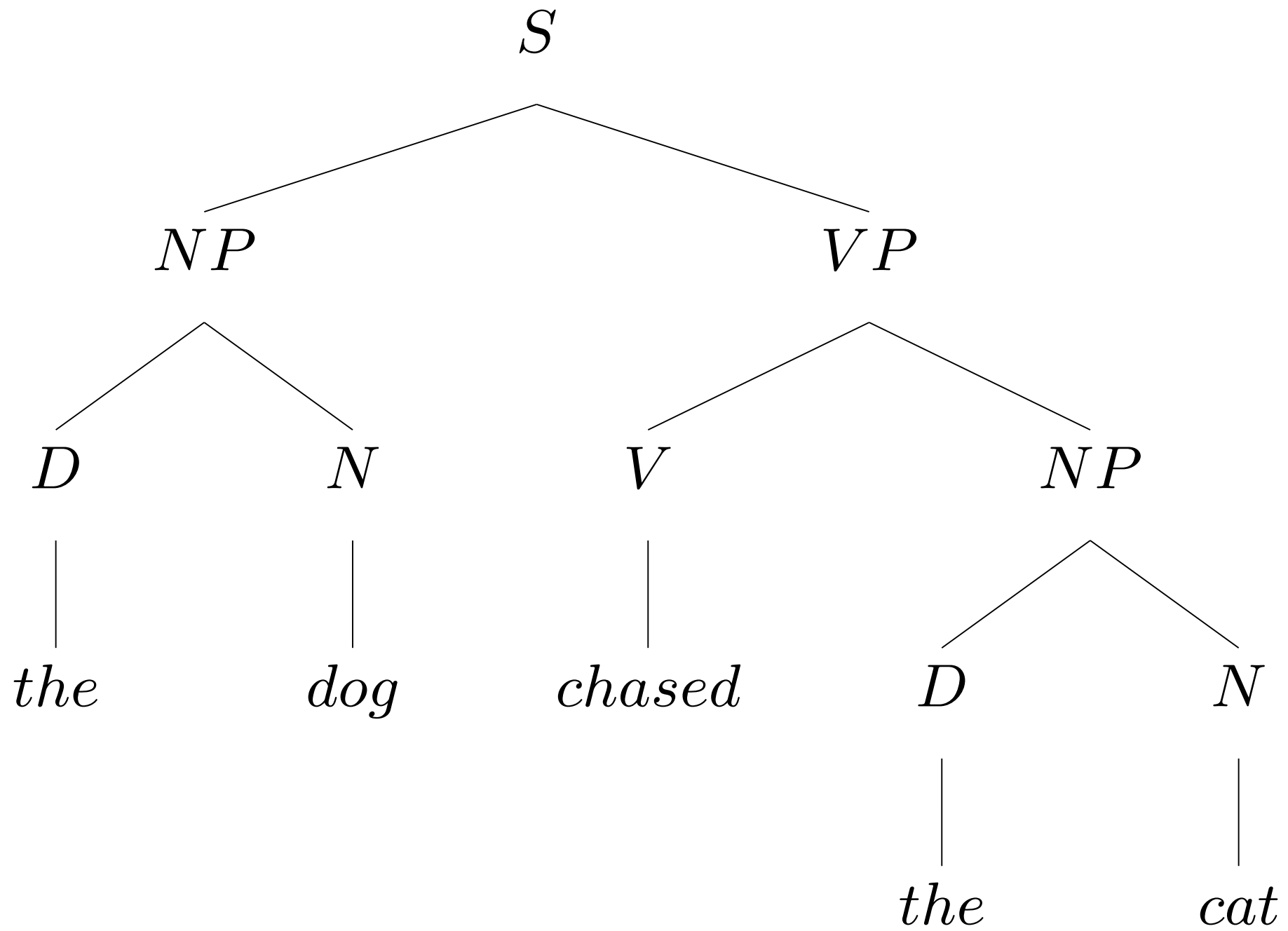


D  
|  
the

V  
|  
chased

N  
|  
dog

N  
|  
cat



Bottom-up and top-down approaches are equivalent for CFG,  
but can differ for more complex types of grammars

### Rules

$S \longrightarrow A \ B$

$A \longrightarrow C \ D$ , in the environment  $\_\_E$ .

$B \longrightarrow E \ F$ , in the environment  $D\_\_$ .

### Lexicon

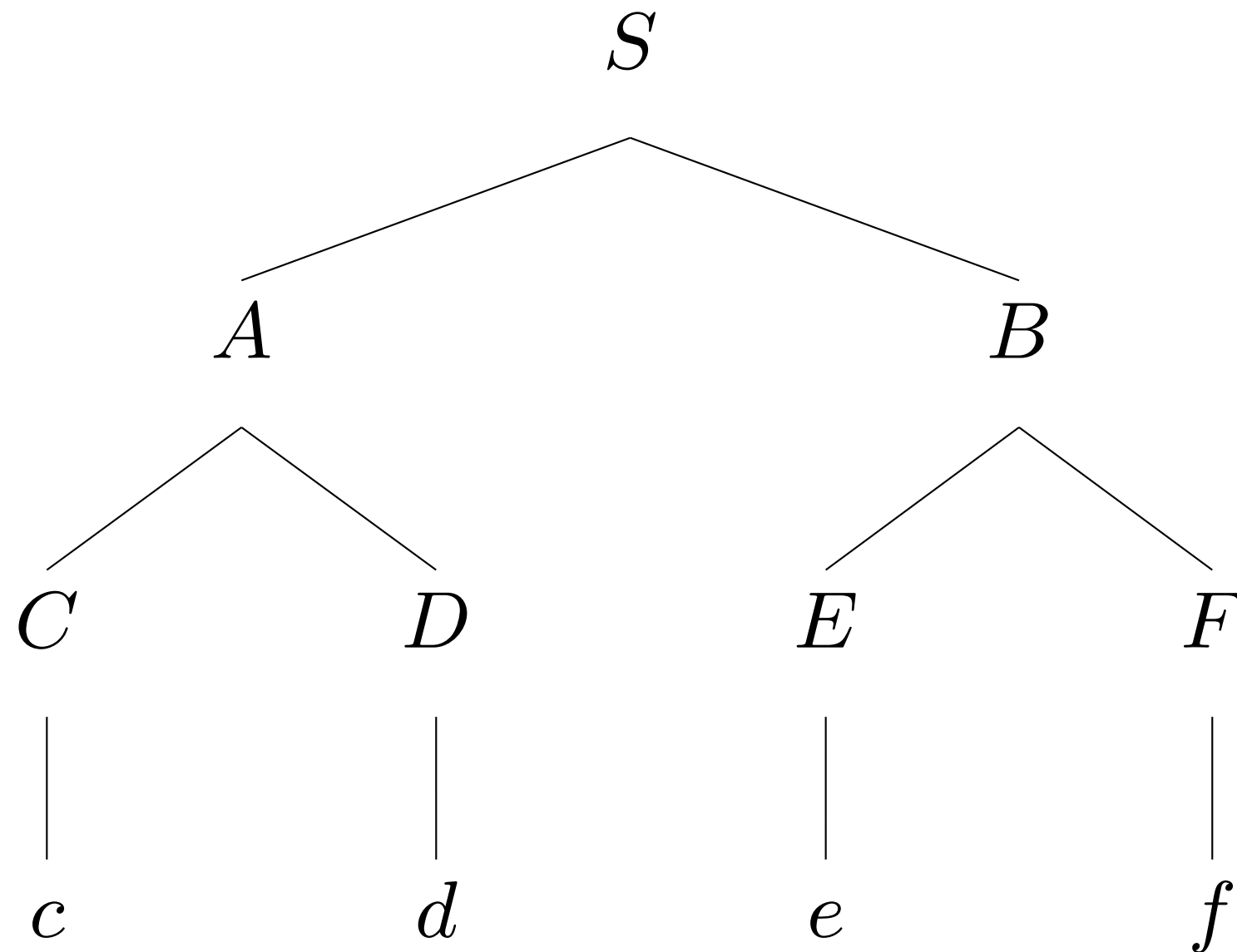
C: c

D: d

E: e

F: f

This tree is licensed bottom-up,  
but not top-down



# Weaknesses of CFG

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$VP \rightarrow P \ NP$

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- Rules get very cumbersome once we try to deal with things like agreement and transitivity.
- It has been argued that certain languages (notably Swiss German and Bambara) contain constructions that are provably beyond the descriptive capacity of CFG.

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- Linguistic constructions that are beyond the descriptive power of CFG are rare.
- It's computationally tractable and techniques for processing CFGs are well understood.

# So....

- CFG has been the starting point for most types of generative grammar.
- The theory we develop in this course is an extension of CFG.

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- Next time: Feature structures