

# Meaning Representation and Semantic Analysis

Ling 571  
Deep Processing Techniques for NLP  
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# Roadmap

- Meaning representation:
  - Event representations
  - Temporal representation
- Semantic Analysis
  - Compositionality and rule-to-rule
  - Semantic attachments
    - Basic
    - Refinements
  - Quantifier scope
  - Earley Parsing and Semantics

# FOL Syntax Summary

*Formula* → *AtomicFormula*  
| *Formula* *Connective* *Formula*  
| *Quantifier* *Variable*, ... *Formula*  
|  $\neg$  *Formula*  
| (*Formula*)  
*AtomicFormula* → *Predicate*(*Term*, ...)  
*Term* → *Function*(*Term*, ...)  
| *Constant*  
| *Variable*  
*Connective* →  $\wedge$  |  $\vee$  |  $\Rightarrow$   
*Quantifier* →  $\forall$  |  $\exists$   
*Constant* → *A* | *VegetarianFood* | *Maharani* ...  
*Variable* → *x* | *y* | ...  
*Predicate* → *Serves* | *Near* | ...  
*Function* → *LocationOf* | *CuisineOf* | ...

# Semantics of FOL

- Model-theoretic approach:
  - FOL terms (objects): denote elements in a domain
  - Atomic formulas are:
    - If properties, sets of domain elements
    - If relations, sets of tuples of elements
- Formulas based on logical operators:

$P$	$Q$	$\neg P$	$P \wedge Q$	$P \vee Q$	$P \Rightarrow Q$
<i>False</i>	<i>False</i>	<i>True</i>	<i>False</i>	<i>False</i>	<i>True</i>
<i>False</i>	<i>True</i>	<i>True</i>	<i>False</i>	<i>True</i>	<i>True</i>
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# Inference

- Standard AI-type logical inference procedures
  - Modus Ponens
  - Forward-chaining, Backward Chaining
  - Abduction
  - Resolution
  - Etc,...
- We'll assume we have a prover

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- Initially, single predicate with some arguments
  - Serves(Maharani,IndianFood)

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  - Serves(Maharani,IndianFood)
  - Assume # ags = # elements in subcategorization frame
- Example:
  - I ate.
  - I ate a turkey sandwich.
  - I ate a turkey sandwich at my desk.
  - I ate at my desk.
  - I ate lunch.
  - I ate a turkey sandwich for lunch.
  - I ate a turkey sandwich for lunch at my desk.



# Events

- Issues?

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  - Arity – how can we deal with different #s of arguments?
- One predicate per frame
  - Eating<sub>1</sub>(Speaker)
  - Eating<sub>2</sub>(Speaker,TS)
  - Eating<sub>3</sub>(Speaker,TS,Desk)
  - Eating<sub>4</sub>(Speaker,Desk)
  - Eating<sub>5</sub>(Speaker,TS,Lunch)
  - Eating<sub>6</sub>(Speaker,TS,Lunch,Desk)

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    - Can't directly associate with other predicates
- Could write rules to implement implications
  - But?
    - Intractable in the large
      - Like the subcat problem generally.

# Variabilizing

- Create predicate with maximum possible arguments
  - Include appropriate args
  - Maintains connections
    - $\exists w, x, y \text{Eating}(\text{Speaker}, w, x, y)$
    - $\exists w, x \text{Eating}(\text{Speaker}, TS, w, x)$
    - $\exists w \text{Eating}(\text{Speaker}, TS, w, \text{Desk})$
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- Better?
  - Yes, but
    - Too many commitments – assume all details show up
    - Can't individuate – don't know if same event

# Events - Finalized

- Neo-Davidsonian representation:
  - Distill event to single argument for event itself
  - Everything else is additional predication

$\exists e \text{Eating}(e) \wedge \text{Eater}(e, \text{Speaker}) \wedge \text{Eaten}(e, \text{TS}) \wedge \text{Meal}(e, \text{Lunch}) \wedge \text{Location}(e, \text{Desk})$

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- Pros:
  - No fixed argument structure
    - Dynamically add predicates as necessary
  - No extra roles
  - Logical connections can be derived

# Representing Time

- Temporal logic:
  - Includes tense logic to capture verb tense infor
- Basic notion:
  - Timeline:
    - From past to future
    - Events associated with points or intervals on line
      - Ordered by positioning on line
    - Current time
      - Relative order gives past/present/future

# Temporal Information

- I arrived in New York.
- I am arriving in New York.
- I will arrive in New York.
  - Same event, differ only in tense

$\exists e \text{Arriving}(e) \wedge \text{Arriver}(e, \text{Speaker}) \wedge \text{Destination}(e, \text{NY})$

- Create temporal representation based on verb tense
  - Add predication about event variable
  - Temporal variables represent:
    - Interval of event
    - End point of event
    - Predicates link end point to current time

# Temporal Representation

$\exists e, i, n, t \text{ Arriving}(e) \wedge \text{Arriver}(e, \text{Speaker}) \wedge \text{Destination}(e, \text{NY})$   
 $\wedge \text{IntervalOf}(e, i) \wedge \text{EndPoint}(i, e) \wedge \text{Precedes}(e, \text{Now})$

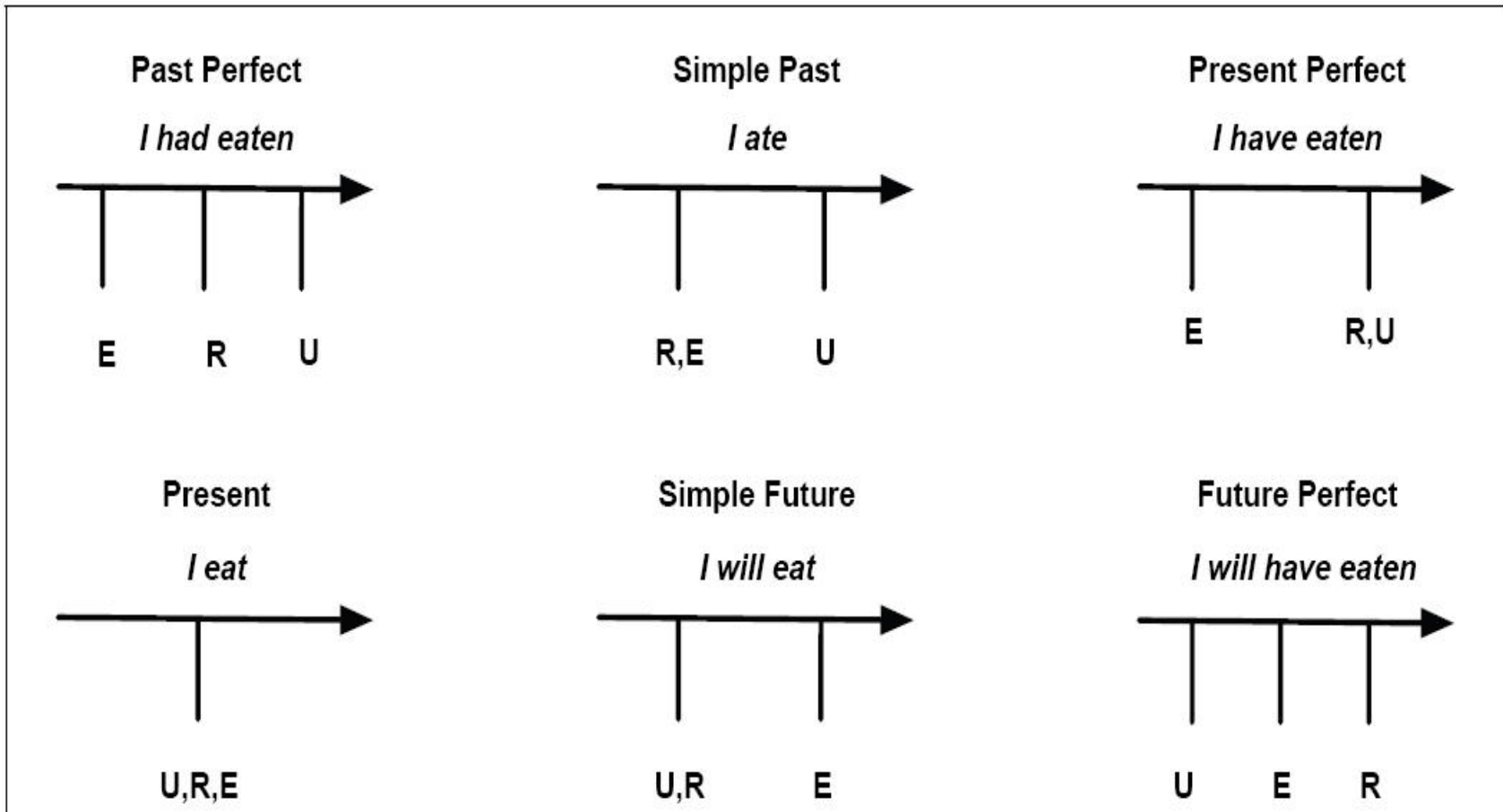
$\exists e, i, n, t \text{ Arriving}(e) \wedge \text{Arriver}(e, \text{Speaker}) \wedge \text{Destination}(e, \text{NY})$   
 $\wedge \text{IntervalOf}(e, i) \wedge \text{MemberOf}(i, \text{Now})$

$\exists e, i, n, t \text{ Arriving}(e) \wedge \text{Arriver}(e, \text{Speaker}) \wedge \text{Destination}(e, \text{NY})$   
 $\wedge \text{IntervalOf}(e, i) \wedge \text{EndPoint}(i, n) \wedge \text{Precedes}(\text{Now}, e)$

# More Temp Rep

- Flight 902 arrived late.
- Flight 902 had arrived late.
- Does the current model cover this?
  - Not really
  - Need additional notion:
    - Reference point
      - As well as current time, event time
        - Current model: current = utterance time = reference point

# Reichenbach's Tense Model



# Meaning Representation for Computational Semantics

- Requirements:
  - Verifiability, Unambiguous representation, Canonical Form, Inference, Variables, Expressiveness
- Solution:
  - First-Order Logic
    - Structure
    - Semantics
    - Event Representation
- Next: Semantic Analysis
  - Deriving a meaning representation for an input



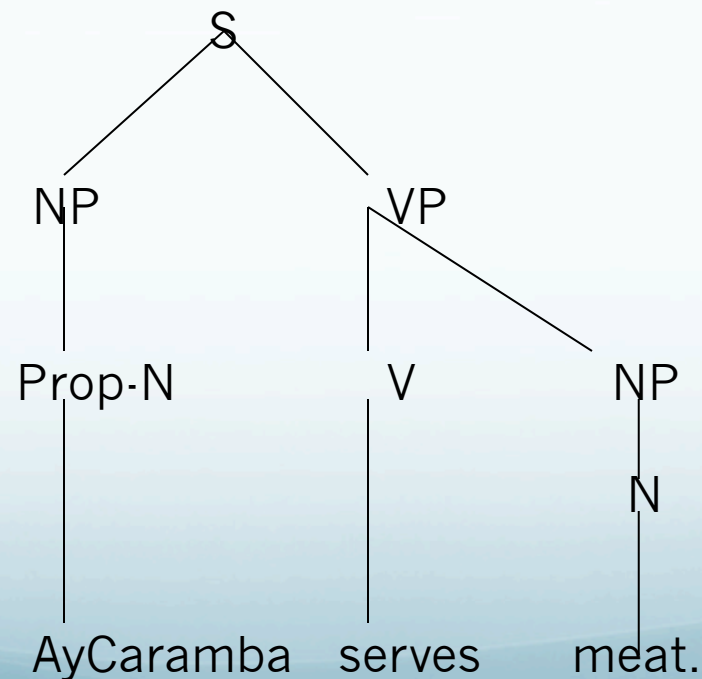
# Syntax-driven Semantic Analysis

- Key: Principle of Compositionality
  - Meaning of sentence from meanings of parts
    - E.g. groupings and relations from syntax
- Question: Integration?
- Solution 1: Pipeline
  - Feed parse tree and sentence to semantic unit
  - Sub-Q: Ambiguity:
    - Approach: Keep all analyses, later stages will select

# Simple Example

- AyCaramba serves meat.

$\exists e \text{ Isa}(e, \text{Serving}) \wedge \text{Server}(e, \text{AyCaramba}) \wedge \text{Served}(e, \text{Meat})$



# Rule-to-Rule

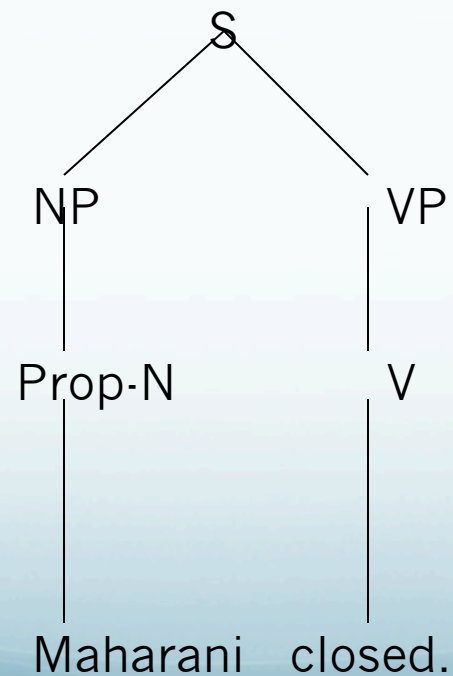
- Issue:
  - How do we know which pieces of the semantics link to what part of the analysis?
  - Need detailed information about sentence, parse tree
    - Infinitely many sentences & parse trees
    - Semantic mapping function per parse tree => intractable
- Solution:
  - Tie semantics to finite components of grammar
    - E.g. rules & lexicon
  - Augment grammar rules with semantic info
    - Aka “attachments”
      - Specify how RHS elements compose to LHS

# Semantic Attachments

- Basic structure:
  - $A \rightarrow a_1 \dots a_n \{f(a_j.\text{sem}, \dots a_k.\text{sem})\}$
  - $A.\text{sem}$
- Language for semantic attachments
  - Arbitrary programming language fragments?
    - Arbitrary power but hard to map to logical form
    - No obvious relation between syntactic, semantic elements
  - Lambda calculus
    - Extends First Order Predicate Calculus (FOPC) with function application
  - Feature-based model + unification
- Focus on lambda calculus approach

# Basic example

- Input: Maharani closed.
- Target output: Closed(Maharani)



# Semantic Analysis Example

- Semantic attachments:
  - Each CFG production gets semantic attachment
- Maharani
  - ProperNoun  $\rightarrow$  Maharani {Maharani}
    - FOL constant to refer to object
  - NP  $\rightarrow$  ProperNoun {ProperNoun.sem}
    - No additional semantic info added

# Semantic Attachment Example

- Phrase semantics is function of SA of children
- More complex functions are parameterized
  - E.g. Verb  $\rightarrow$  closed  $\{ \lambda x. \text{Closed}(x) \}$ 
    - Unary predicate:
      - 1 arg = subject, not yet specified
  - VP  $\rightarrow$  Verb  $\{ \text{Verb.sem} \}$ 
    - No added information
  - S  $\rightarrow$  NP VP  $\{ \text{VP.sem}(\text{NP.sem}) \}$ 
    - Application =  $\lambda x. \text{Closed}(x)(\text{Maharani}) = \text{Closed}(\text{Maharani})$

# Semantic Attachment

- General pattern:
  - Grammar rules mostly lambda reductions
    - Functor and arguments
- Most representation resides in lexicon



# Refining Representation

- Add
  - Neo-Davidsonian event-style model
  - Complex quantification
- Example II
  - Input: Every restaurant closed.
  - Target:

$$\forall x \text{Restaurant}(x) \Rightarrow \exists e \text{Closed}(e) \wedge \text{ClosedThing}(e, x)$$

# Refining Representation

- Idea:  $\forall x \text{Restaurant}(x)$ 
  - Good enough?
    - No: roughly ‘everything is a restaurant’
    - Saying something about all restaurants – nuclear scope
- Solution: Dummy predicate  
 $\forall x \text{Restaurant}(x) \Rightarrow Q(x)$ 
  - Good enough?
    - No: no way to get  $Q(x)$  from elsewhere in sentence
- Solution: Lambda  
 $\lambda Q. \forall x \text{Restaurant}(x) \Rightarrow Q(x)$

# Updating Attachments

- Noun -> restaurant  $\{ \lambda x. \text{Restaurant}(x) \}$
- Nominal -> Noun  $\{ \text{Noun.sem} \}$
- Det -> Every  $\{ \lambda P. \lambda Q. \forall x P(x) \Rightarrow Q(x) \}$
- NP -> Det Nominal  $\{ \text{Det.sem}(\text{Nom.sem}) \}$

$\lambda P. \lambda Q. \forall x P(x) \Rightarrow Q(x) (\lambda x. \text{Restaurant}(x))$

$\lambda P. \lambda Q. \forall x P(x) \Rightarrow Q(x) (\lambda y. \text{Restaurant}(y))$

$\lambda Q. \forall x \lambda y. \text{Restaurant}(y)(x) \Rightarrow Q(x)$

$\lambda Q. \forall x \text{Restaurant}(x) \Rightarrow Q(x)$

# Full Representation

- Verb  $\rightarrow$  close  $\{\lambda x.\exists e \text{Closed}(e) \wedge \text{ClosedThing}(e, x)\}$
- VP  $\rightarrow$  Verb  $\{\text{Verb.sem}\}$
- S  $\rightarrow$  NP VP  $\{\text{NP.sem}(\text{VP.sem})\}$

$\lambda Q.\forall x \text{Restaurant}(x) \Rightarrow Q(x)(\lambda y.\exists e \text{Closed}(e) \wedge \text{ClosedThing}(e, y))$

$\forall x \text{Restaurant}(x) \Rightarrow \lambda y.\exists e \text{Closed}(e) \wedge \text{ClosedThing}(e, y)(x)$

$\forall x \text{Restaurant}(x) \Rightarrow \exists e \text{Closed}(e) \wedge \text{ClosedThing}(e, x)$

# Generalizing Attachments

- ProperNoun -> Maharani {Maharani}
- Does this work in the new style?
  - No, we turned the NP/VP application around
- New style:  $\lambda x.x(\text{Maharani})$

# More

- Determiner

- Det  $\rightarrow$  a  $\{ \lambda P. \lambda Q. \exists x P(x) \wedge Q(x) \}$

- a restaurant  $\lambda Q. \exists x Restaurant(x) \wedge Q(x)$

- Transitive verb:

- VP  $\rightarrow$  Verb NP { Verb.sem(NP.sem) }

- Verb  $\rightarrow$  opened

$\lambda w. \lambda z. w(\lambda x. \exists e Opened(e) \wedge Opener(e, z) \wedge OpenedThing(e, w))$

# Strategy for Semantic Attachments

- General approach:
  - Create complex, lambda expressions with lexical items
    - Introduce quantifiers, predicates, terms
  - Percolate up semantics from child if non-branching
  - Apply semantics of one child to other through lambda
    - Combine elements, but don't introduce new



# Sample Attachments

<b>Grammar Rule</b>	<b>Semantic Attachment</b>
$S \rightarrow NP VP$	$\{NP.sem(VP.sem)\}$
$NP \rightarrow Det Nominal$	$\{Det.sem(Nominal.sem)\}$
$NP \rightarrow ProperNoun$	$\{ProperNoun.sem\}$
$Nominal \rightarrow Noun$	$\{Noun.sem\}$
$VP \rightarrow Verb$	$\{Verb.sem\}$
$VP \rightarrow Verb NP$	$\{Verb.sem(NP.sem)\}$
$Det \rightarrow every$	$\{\lambda P.\lambda Q.\forall xP(x) \Rightarrow Q(x)\}$
$Det \rightarrow a$	$\{\lambda P.\lambda Q.\exists xP(x) \wedge Q(x)\}$
$Noun \rightarrow restaurant$	$\{\lambda r.Restaurant(r)\}$
$ProperNoun \rightarrow Matthew$	$\{\lambda m.m(Matthew)\}$
$ProperNoun \rightarrow Franco$	$\{\lambda f.f(Franco)\}$
$ProperNoun \rightarrow Frasca$	$\{\lambda f.f(Frasca)\}$
$Verb \rightarrow closed$	$\{\lambda x.\exists eClosed(e) \wedge ClosedThing(e,x)\}$
$Verb \rightarrow opened$	$\{\lambda w.\lambda z.w(\lambda x.\exists eOpened(e) \wedge Opener(e,z) \wedge Opened(e,x))\}$

# Quantifier Scope

- Ambiguity:

- *Every restaurant has a menu*

$\forall x \text{Restaurant}(x) \Rightarrow \exists y(\text{Menu}(y) \wedge (\exists e \text{Having}(e) \wedge \text{Haver}(e, x) \wedge \text{Had}(e, y)))$

- Readings:
  - all have a menu;
  - all have same menu
- Only derived one

$\exists y \text{Menu}(y) \wedge \forall x(\text{Restaurant}(x) \Rightarrow \exists e \text{Having}(e) \wedge \text{Haver}(e, x) \wedge \text{Had}(e, y))$

- Potentially  $O(n!)$  scopings ( $n = \#$  quantifiers)
- There are approaches to describe ambiguity efficiently and recover all alternatives.

# Earley Parsing with Semantics

- Implement semantic analysis
  - In parallel with syntactic parsing
    - Enabled by compositional approach
- Required modifications
  - Augment grammar rules with semantic field
  - Augment chart states with meaning expression
  - Completer computes semantics – e.g. unifies
    - Can also fail to unify
      - Blocks semantically invalid parses
    - Can impose extra work

# Sidelight: Idioms

- Not purely compositional
  - E.g. kick the bucket = die
  - tip of the iceberg = beginning
- Handling:
  - Mix lexical items with constituents (word nps)
  - Create idiom-specific const. for productivity
  - Allow non-compositional semantic attachments
- Extremely complex: e.g. metaphor