

Features & Unification

Ling 571

Deep Processing Techniques for NLP

January 31, 2011

Roadmap

- Features: Motivation
 - Constraint & compactness
- Features
 - Definitions & representations
- Unification
- Application of features in the grammar
 - Agreement, subcategorization
- Parsing with features & unification
 - Augmenting the Earley parser, unification parsing
- Extensions: Types, inheritance, etc
- Conclusion

Constraints & Compactness

- Constraints in grammar
 - $S \rightarrow NP VP$
 - They run.
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- Violate agreement (number), subcategorization

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 - Explosive!, loses key generalizations

Features

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 - I, we; you; he, she, they
 - am, are, is

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- animacy: +/-
- etc

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 - Number, person, gender, etc
- Augment CF rules with feature constraints
 - Develop mechanism to enforce consistency
 - Elegant, compact, rich representation

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 - Features: atomic symbols from a finite set

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$\left(\begin{array}{cc} \text{NUMBER} & \text{PL} \end{array} \right)$

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PERSON	3

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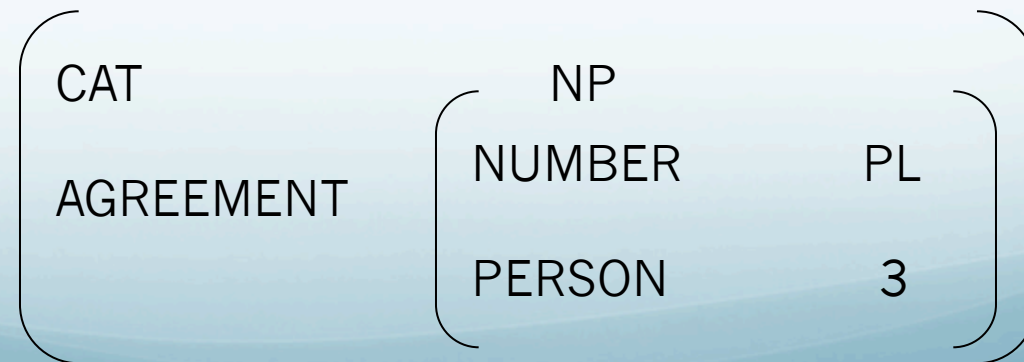
Attribute-value matrix (AVM)

NUMBER	PL
PERSON	3
NUMBER	PL
PERSON	3
CAT	NP
NUMBER	PL
PERSON	3

Feature Representations

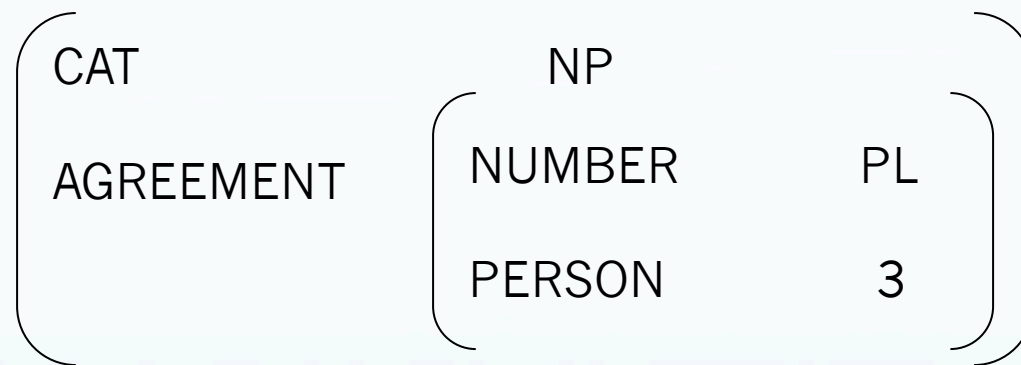
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 - Atomic symbols from a finite set
 - Values may also be feature structures themselves

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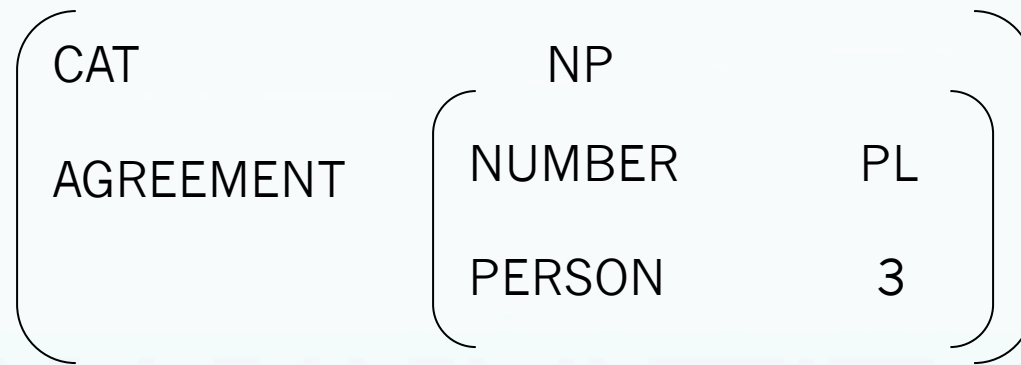
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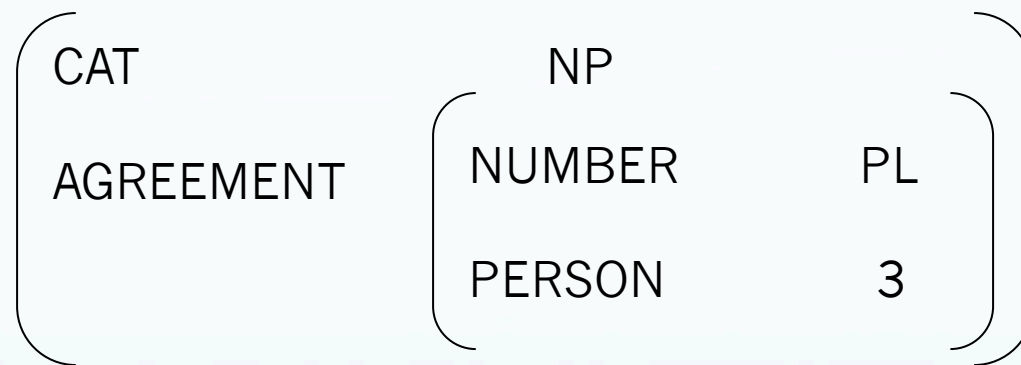
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<AGREEMENT NUMBER> -> PL

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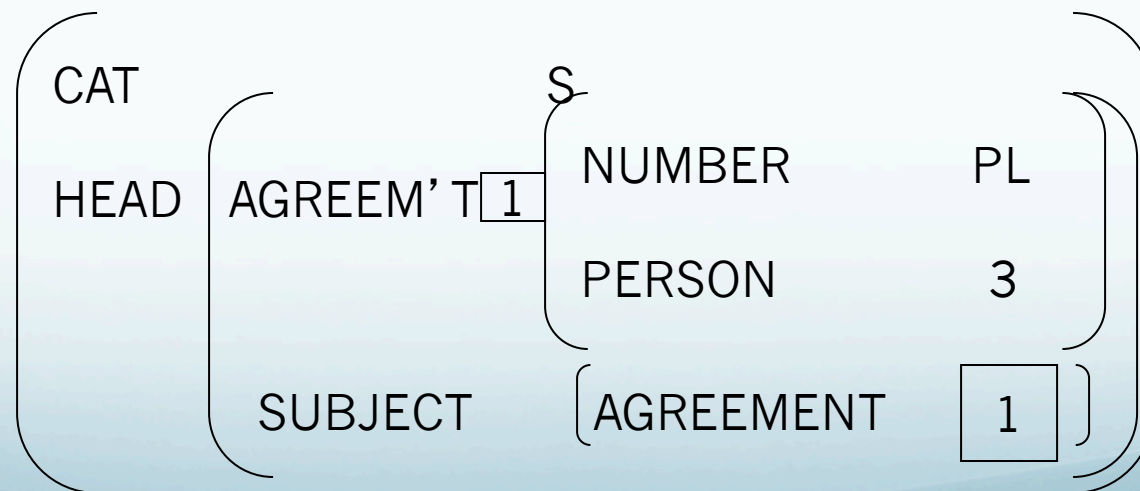
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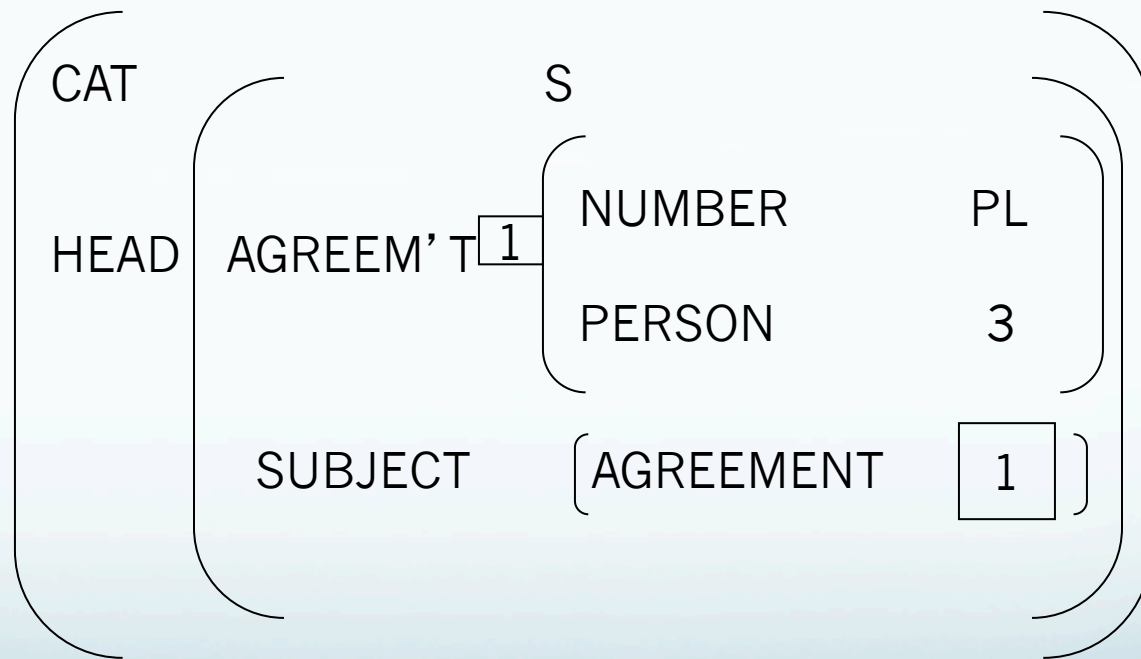
<AGREEMENT NUMBER> -> PL
<AGREEMENT PERSON> -> 3

Feature Representations

- Reentrant feature structures
 - Features share some feature structure as value
 - Not merely equal values
 - Shared substructure
 - Feature paths lead to same node

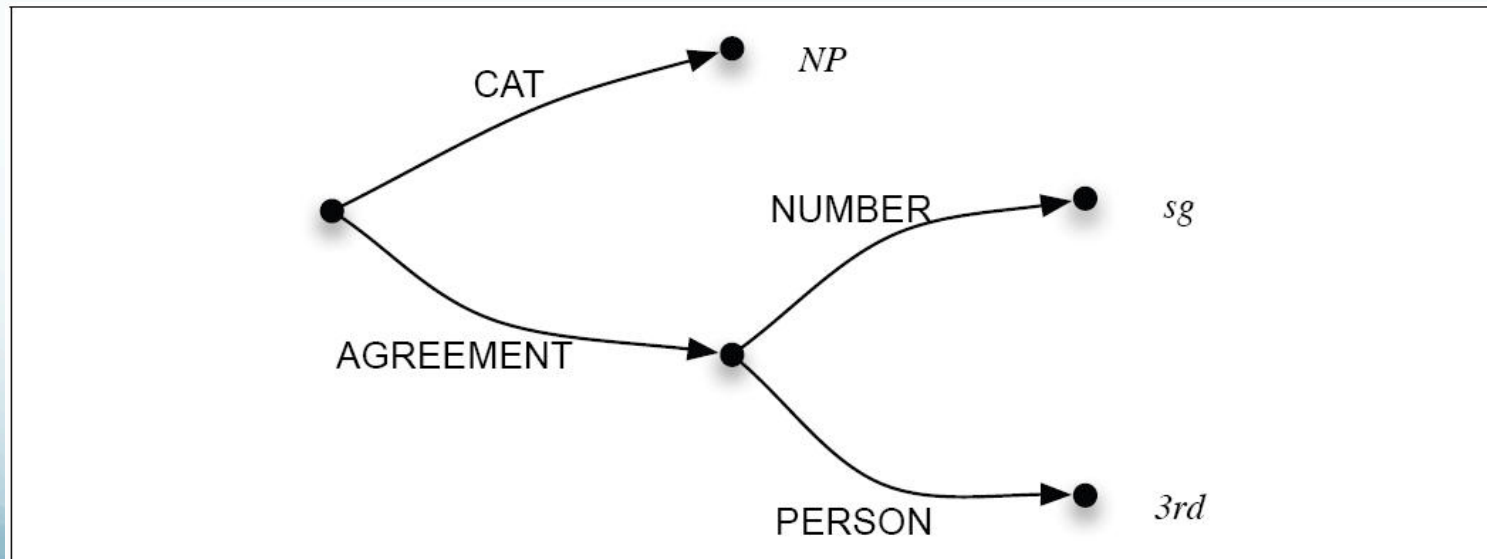


Head-Subject Agreement

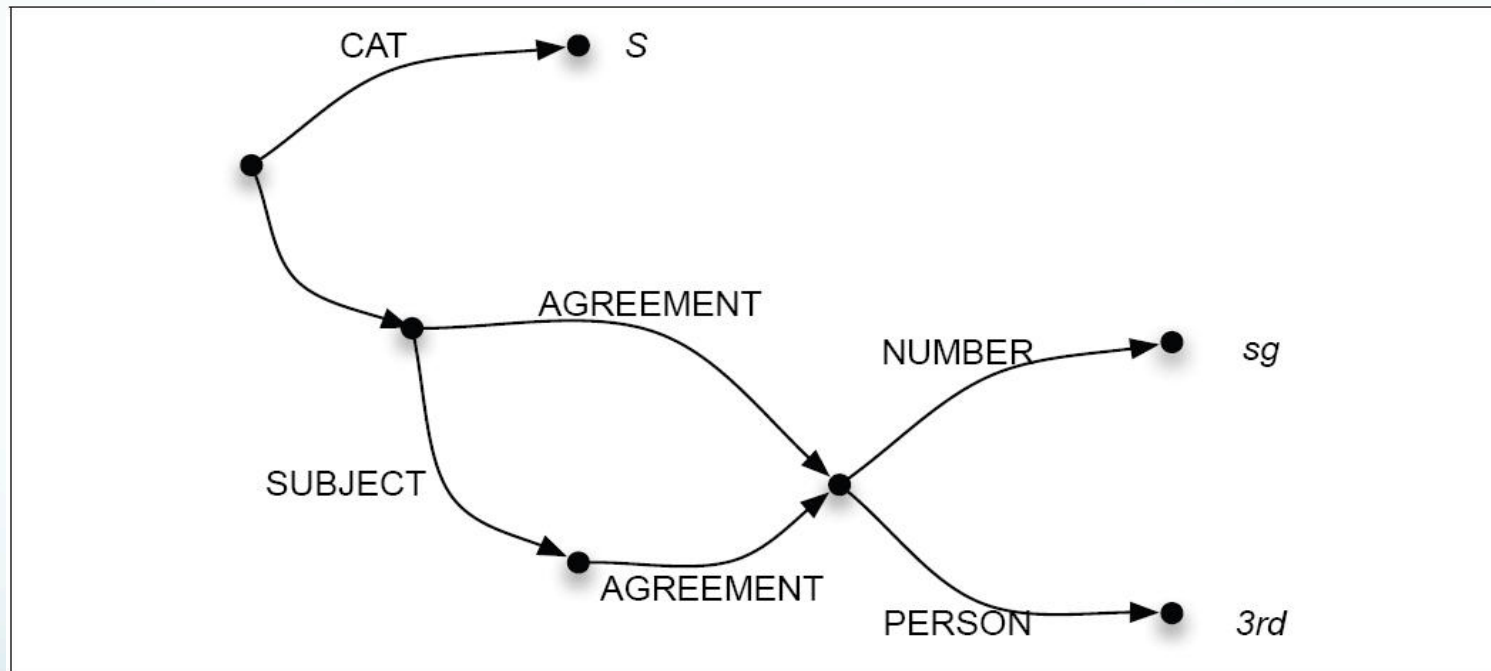


Feature representations

- Feature structures can also be represented as DAGs
 - Directed, acyclic graphs
 - Edges are features
 - Nodes values



Reentrant DAG



Unification

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Unification

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 - Feature structures match where both have values, differ in missing or underspecified
 - Resulting structure incorporates constraints of both

Subsumption

- Relation between feature structures
 - Less specific f.s. subsumes more specific f.s.
 - F.s. F subsumes f.s. G iff
 - For every feature x in F , $F(x)$ subsumes $G(x)$
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Unification Examples

- Identical
 - [Number SG] U [Number SG]

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 - $[\text{Person 3}]$
 - $[\text{Number SG}] \cup [\text{Number PL}]$

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- Different specification
 - $[\text{Number SG}] \cup [\text{Person 3}] = [\text{Number SG}]$
 - $[\text{Person 3}]$
- Mismatched
 - $[\text{Number SG}] \cup [\text{Number PL}] \rightarrow \text{Fails!}$

More Unification Examples

$$\left(\begin{array}{l} \text{AGREEMENT} \quad [1] \\ \text{SUBJECT} \quad \left(\text{AGREEMENT} [1] \right) \end{array} \right) \cup$$

$$\left(\begin{array}{l} \text{SUBJECT} \quad \left(\text{AGREEMENT} \quad \left(\begin{array}{l} \text{PERSON} \quad 3 \\ \text{NUMBER} \quad \text{SG} \end{array} \right) \right) \\ \text{AGREEMENT} \quad [1] \\ \text{SUBJECT} \quad \left(\text{AGREEMENT} [1] \quad \left(\begin{array}{l} \text{PERSON} \quad 3 \\ \text{NUMBER} \quad \text{SG} \end{array} \right) \right) \end{array} \right) =$$

Features in CFGs: Agreement

- Goal:
 - Support agreement of NP/VP, Det Nominal
- Approach:
 - Augment CFG rules with features
 - Employ head features
 - Each phrase: VP, NP has head
 - Head: child that provides features to phrase
 - Associates grammatical role with word
 - VP – V; NP – Nom, etc

Agreement with Heads and Features

VP -> Verb NP

<VP HEAD> = <Verb HEAD>

NP -> Det Nominal

<NP HEAD> = <Nominal HEAD>

<Det HEAD AGREEMENT> = <Nominal HEAD AGREEMENT>

Nominal -> Noun

<Nominal HEAD> = <Noun HEAD>

Noun -> flights

<Noun HEAD AGREEMENT NUMBER> = PL

Verb -> serves

<Verb HEAD AGREEMENT NUMBER> = SG

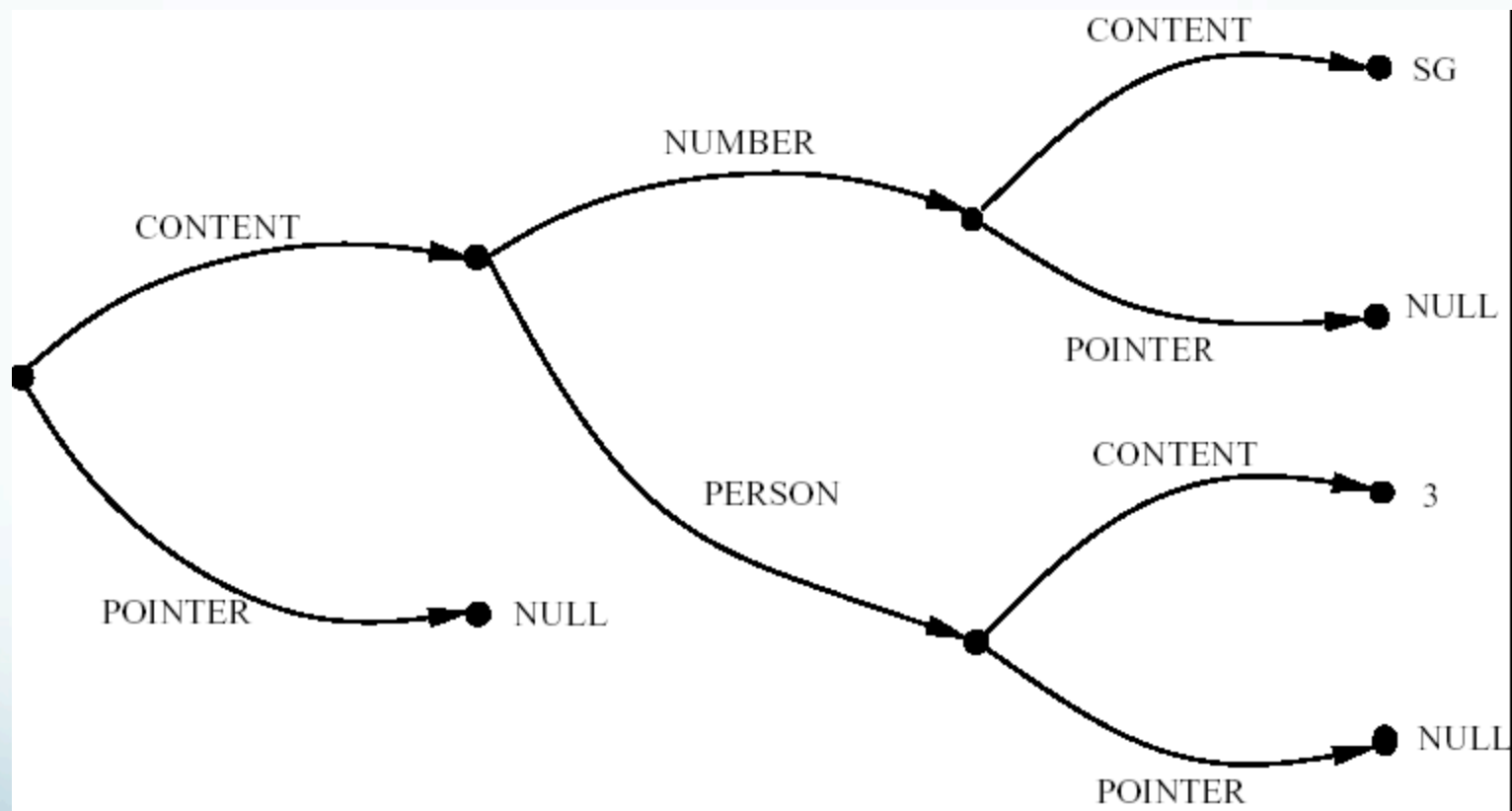
<Verb HEAD AGREEMENT PERSON> = 3

Feature Applications

- Subcategorization:
 - Verb-Argument constraints
 - Number, type, characteristics of args (e.g. animate)
 - Also adjectives, nouns
- Long distance dependencies
 - E.g. filler-gap relations in wh-questions, rel

Implementing Unification

- Data Structure:
 - Extension of the DAG representation
 - Each f.s. has a content field and a pointer field
 - If pointer field is null, content field has the f.s.
 - If pointer field is non-null, it points to actual f.s.



Implementing Unification: II

- Algorithm:
 - Operates on pairs of feature structures
 - Order independent, destructive
 - If fs1 is null, point to fs2
 - If fs2 is null, point to fs1
 - If both are identical, point fs1 to fs2, return fs2
 - Subsequent updates will update both
 - If non-identical atomic values, fail!

Implementing Unification: III

- If non-identical, complex structures
 - Recursively traverse all features of fs2
 - If feature in fs2 is missing in fs1
 - Add to fs1 with value null
 - If all unify, point fs2 to fs1 and return fs1

Unification

function UNIFY(*f1-orig*, *f2-orig*) **returns** f-structure or failure

f1 \leftarrow Dereferenced contents of *f1-orig*

f2 \leftarrow Dereferenced contents of *f2-orig*

if *f1* and *f2* are identical **then**

f1.pointer \leftarrow *f2*

return *f2*

else if *f1* is null **then**

f1.pointer \leftarrow *f2*

return *f2*

else if *f2* is null **then**

f2.pointer \leftarrow *f1*

return *f1*

else if both *f1* and *f2* are complex feature structures **then**

f2.pointer \leftarrow *f1*

for each *f2-feature* **in** *f2* **do**

f1-feature \leftarrow Find or create a corresponding feature in *f1*

if UNIFY(*f1-feature.value*, *f2-feature.value*) **returns** failure **then**

return failure

return *f1*

else return failure

Example

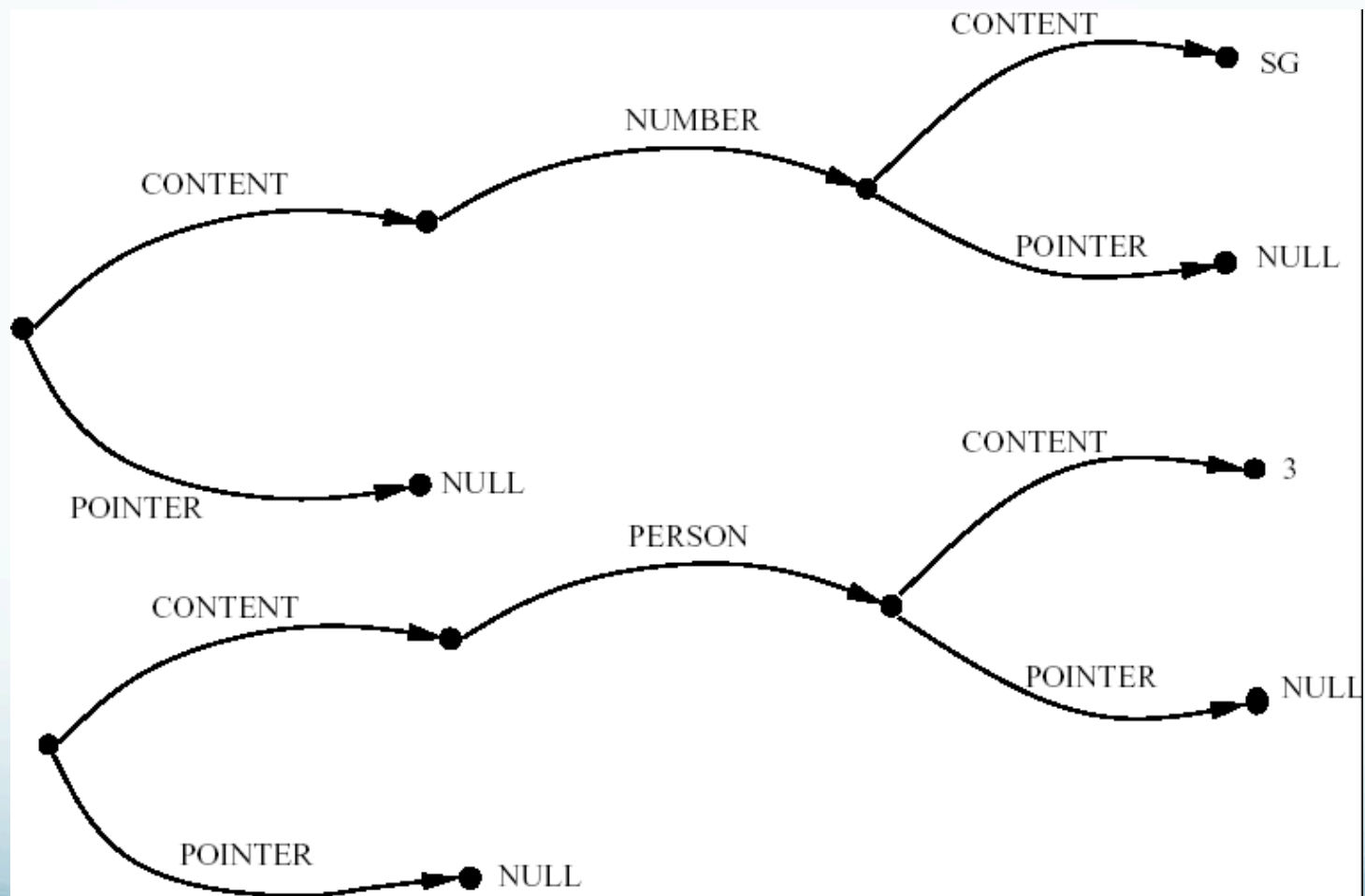
$$\left(\begin{array}{l} \text{AGREEMENT [1]} \\ \text{SUBJECT} \end{array} \left\{ \begin{array}{l} \text{NUMBER SG} \\ \text{AGREEMENT [1]} \end{array} \right\} \right) \cup$$

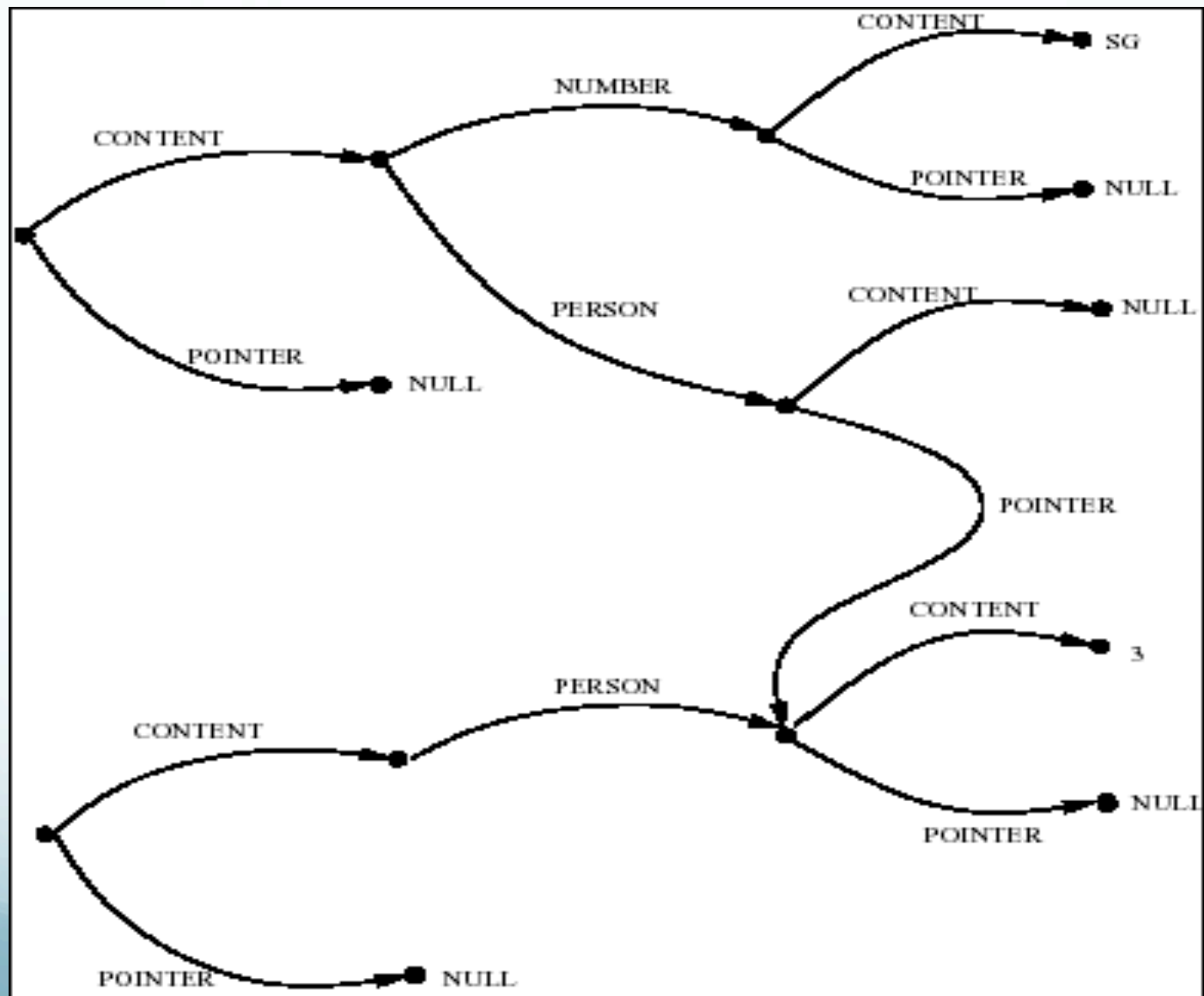
$$\left(\text{SUBJECT} \left(\text{AGREEMENT} \left(\text{PERSON 3} \right) \right) \right)$$

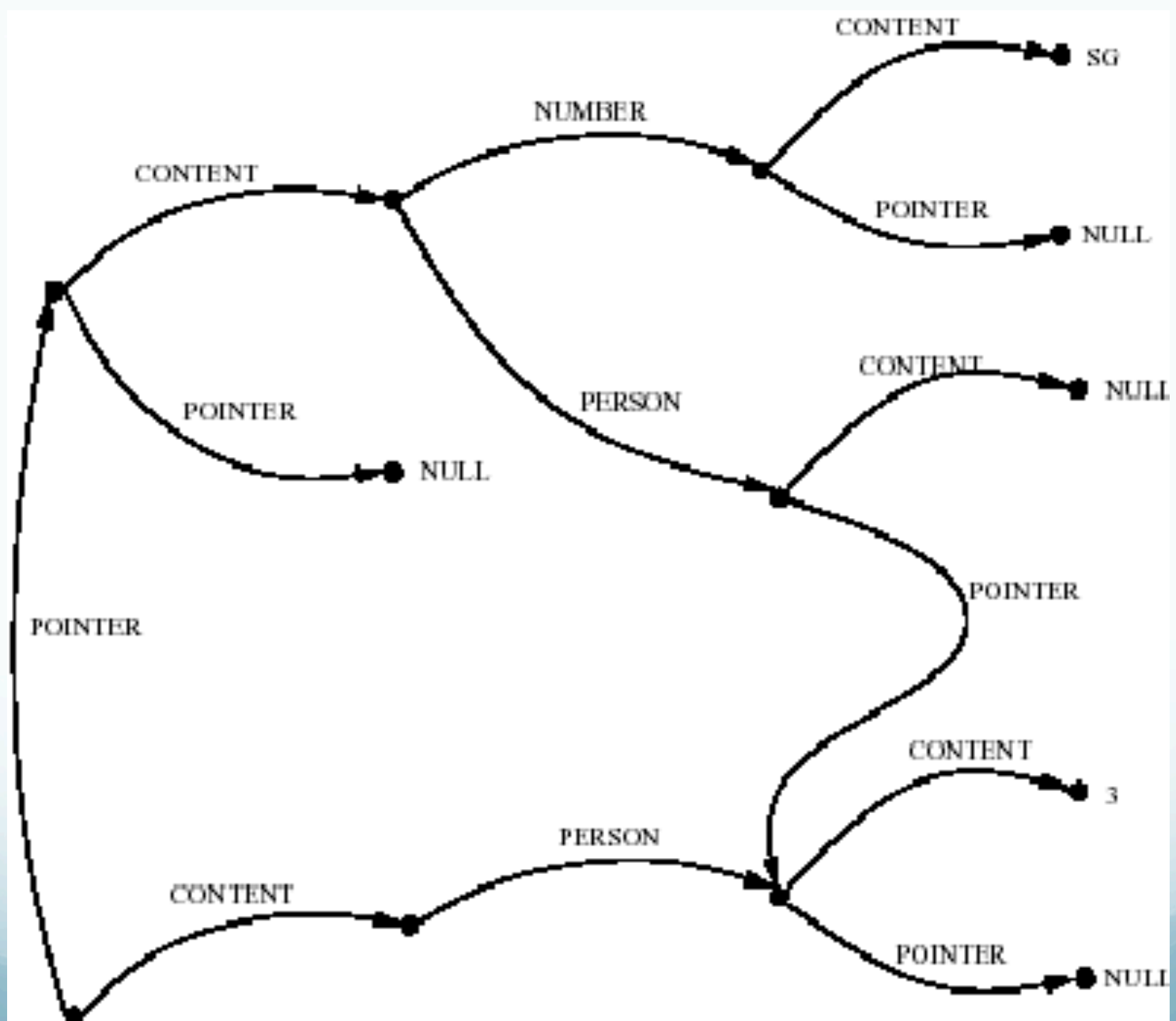
[AGREEMENT [1]] U [AGREEMENT [PERSON 3]]

[NUMBER SG] U [PERSON 3]

[NUMBER SG] U [PERSON 3]
[PERSON NULL]







Unification Example

cat	S
voice	active
agent	[1 [cat NP number 4]
process	[2 [cat VB number 4]
patient	[3 [cat NP]
pattern	[subject 1 verb 2 object 3]

Grammar entry for sentence

(From S.F., 2010)

Unification Example

cat	NP
spec	[1] [cat DT number [3] definite [4]]
head	[2] [cat NN number [3]]
number	[3]
definite	[4]
pattern	[first [1] second [2]]

Grammar entry for NP

Unification Example

cat	DT
definite	yes
number	SG
form	"the"

cat	DT
definite	yes
number	PL
form	"these"

Lexical entries

Unification Example

Unifying a noun phrase with a determiner

cat	NP								
spec	<table><tr><td>1</td><td><table><tr><td>cat</td><td>DT</td></tr><tr><td>number</td><td>3</td></tr><tr><td>definite</td><td>4</td></tr></table></td></tr></table>	1	<table><tr><td>cat</td><td>DT</td></tr><tr><td>number</td><td>3</td></tr><tr><td>definite</td><td>4</td></tr></table>	cat	DT	number	3	definite	4
1	<table><tr><td>cat</td><td>DT</td></tr><tr><td>number</td><td>3</td></tr><tr><td>definite</td><td>4</td></tr></table>	cat	DT	number	3	definite	4		
cat	DT								
number	3								
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head	<table><tr><td>2</td><td><table><tr><td>cat</td><td>NN</td></tr><tr><td>number</td><td>3</td></tr></table></td></tr></table>	2	<table><tr><td>cat</td><td>NN</td></tr><tr><td>number</td><td>3</td></tr></table>	cat	NN	number	3		
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cat	NN								
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first	1								
second	2								

 \sqcup

cat	DT
definite	yes
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(From S.F., 2010)

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Unifying NP with Determiner

(From S.F., 2010)

Unification Example

Result of unification

cat	NP										
spec	<table><tr><td>1</td><td><table><tr><td>cat</td><td>DT</td></tr><tr><td>number</td><td>PL</td></tr><tr><td>definite</td><td>yes</td></tr><tr><td>form</td><td>"these"</td></tr></table></td></tr></table>	1	<table><tr><td>cat</td><td>DT</td></tr><tr><td>number</td><td>PL</td></tr><tr><td>definite</td><td>yes</td></tr><tr><td>form</td><td>"these"</td></tr></table>	cat	DT	number	PL	definite	yes	form	"these"
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(From S.F., 2010)

Unification and the Earley Parser

- Employ constraints to restrict addition to chart
- Actually pretty straightforward
 - Augment rules with feature structure
 - Augment state (chart entries) with DAG
 - Prediction adds DAG from rule
 - Completion applies unification (on copies)
 - Adds entry only if current DAG is NOT subsumed

Parsing with Features

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- One strategy:
 - Parse as usual
 - Test completed parses for unification constraints
- Pros:
 - Simple, requires little modification
- Cons:
 - Wasted effort
 - Builds many partial parses that can't unify
- Integrate unification in parse construction

Parsing, Unification, & Earley

- Augment existing Earley parser for unification
 - Fairly straightforward
- Modify representations:
 - Augment CFG rules with constraints
 - Use constraints to create feature structure as DAG
 - Add DAG to state representation
 - E.g., $S \rightarrow \bullet NP VP, [0,0], [], Dag$

Integrating Unification

- Main change: Completer
 - Advances • in rules where next constituent matches a just-completed constituent
 - Now, unifies Dag from completed constituent with the part of the feature structure in rules advanced
 - If fails, no new entry in chart
- Second change:
 - Only add state if NOT subsumed by states in chart

function EARLEY-PARSE(*words*, *grammar*) **returns** *chart*

 ADDTOCHART($(\gamma \rightarrow \bullet S, [0,0], dag_\gamma)$, *chart*[0])

for $i \leftarrow$ **from** 0 **to** LENGTH(*words*) **do**

for each *state* **in** *chart*[*i*] **do**

if INCOMPLETE?(*state*) **and**

 NEXT-CAT(*state*) is not a part of speech **then**

 PREDICTOR(*state*)

elseif INCOMPLETE?(*state*) **and**

 NEXT-CAT(*state*) is a part of speech **then**

 SCANNER(*state*)

else

 COMPLETER(*state*)

end

end

return(*chart*)

```

procedure PREDICTOR( $(A \rightarrow \alpha \bullet B \beta, [i, j], dag_A)$ )
  for each  $(B \rightarrow \gamma)$  in GRAMMAR-RULES-FOR( $B, grammar$ ) do
    ADDTOCHART( $(B \rightarrow \bullet \gamma, [j, j], dag_B), chart[j]$ )
  end

procedure SCANNER( $(A \rightarrow \alpha \bullet B \beta, [i, j], dag_A)$ )
  if  $B \in \text{PARTS-OF-SPEECH}(word[j])$  then
    ADDTOCHART( $(B \rightarrow word[j] \bullet, [j, j+1], dag_B), chart[j+1]$ )

procedure COMPLETER( $(B \rightarrow \gamma \bullet, [j, k], dag_B)$ )
  for each  $(A \rightarrow \alpha \bullet B \beta, [i, j], dag_A)$  in  $chart[j]$  do
    if  $new-dag \leftarrow \text{UNIFY-STATES}(dag_B, dag_A, B) \neq \text{Fails!}$ 
      ADDTOCHART( $(A \rightarrow \alpha B \bullet \beta, [i, k], new-dag), chart[k]$ )
  end

procedure UNIFY-STATES( $dag1, dag2, cat$ )
   $dag1-cp \leftarrow \text{COPYDAG}(dag1)$ 
   $dag2-cp \leftarrow \text{COPYDAG}(dag2)$ 
  UNIFY( $\text{FOLLOW-PATH}(cat, dag1-cp), \text{FOLLOW-PATH}(cat, dag2-cp)$ )

procedure ADDTOCHART( $state, chart-entry$ )
  if  $state$  is not subsumed by a state in  $chart-entry$  then
    PUSH-ON-END( $state, chart-entry$ )
  end

```


Unification Parsing

- Abstracts over categories
 - $S \rightarrow NP VP \Rightarrow$
 - $X_0 \rightarrow X_1 X_2; \langle X_0 \text{ cat} \rangle = S; \langle X_1 \text{ cat} \rangle = NP;$
 - $\langle X_2 \text{ cat} \rangle = VP$
 - Conjunction:
 - $X_0 \rightarrow X_1 \text{ and } X_2; \langle X_1 \text{ cat} \rangle = \langle X_2 \text{ cat} \rangle;$
 - $\langle X_0 \text{ cat} \rangle = \langle X_1 \text{ cat} \rangle$
- Issue: Completer depends on categories
- Solution: Completer looks for DAGs which unify with the just-completed state's DAG

Extensions

- Types and inheritance
 - Issue: generalization across feature structures
 - E.g. many variants of agreement
 - More or less specific: 3rd vs sg vs 3rdsg
 - Approach: Type hierarchy
 - Simple atomic types match literally
 - Multiple inheritance hierarchy
 - Unification of subtypes is most general type that is more specific than two input types
 - Complex types encode legal features, etc

Conclusion

- Features allow encoding of constraints
 - Enables compact representation of rules
 - Supports natural generalizations
- Unification ensures compatibility of features
 - Integrates easily with existing parsing mech.
- Many unification-based grammatical theories