# Distributional Semantics 

Ling571<br>Deep Processing Techniques for NLP<br>February 25, 2015

## Roadmap

- Distributional models
- Context
- Features
- Weighting
- Compression
- Integration
- Thesaurus-based similarity models
- Distance \& Similarity in a Thesaurus


## Distributional Similarity

- Represent 'company' of word such that similar words will have similar representations
- 'Company' = context


## Distributional Similarity

- Represent 'company' of word such that similar words will have similar representations
- 'Company' = context
- Word represented by context feature vector
- Many alternatives for vector


## Distributional Similarity

- Represent 'company' of word such that similar words will have similar representations
- 'Company' = context
- Word represented by context feature vector
- Many alternatives for vector
- Initial representation:
- 'Bag of words’ binary feature vector


## Distributional Similarity

- Represent 'company' of word such that similar words will have similar representations
- 'Company' = context
- Word represented by context feature vector
- Many alternatives for vector
- Initial representation:
- 'Bag of words’ binary feature vector
- Feature vector length $N$, where $N$ is size of vocabulary
- $f_{i}=1$ if word $_{i}$ within window of $w, 0$ o.w.


## Binary Feature Vector

|  | arts | boil | data | function | large | sugar | summarized | water |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| apricot | 0 | 1 | 0 | 0 | 1 | 1 | 0 | 1 |
| pineapple | 0 | 1 | 0 | 0 | 1 | 1 | 0 | 1 |
| digital | 0 | 0 | 1 | 1 | 1 | 0 | 1 | 0 |
| information | 0 | 0 | 1 | 1 | 1 | 0 | 1 | 0 |

## Distributional Similarity Questions

## Distributional Similarity Questions

- What is the right neighborhood?
- What is the context?


## Distributional Similarity Questions

- What is the right neighborhood?
- What is the context?
- How should we weight the features?


## Distributional Similarity Questions

- What is the right neighborhood?
- What is the context?
- How should we weight the features?
- How can we compute similarity between vectors?


## Feature Vector Design

- Window size:
- How many words in the neighborhood?
- Tradeoff:


## Feature Vector Design

- Window size:
- How many words in the neighborhood?
- Tradeoff:
- +/. 500 words


## Feature Vector Design

- Window size:
- How many words in the neighborhood?
- Tradeoff:
- +/. 500 words: 'topical context'


## Feature Vector Design

- Window size:
- How many words in the neighborhood?
- Tradeoff:
- +/. 500 words: 'topical context'
- +/. 1 or 2 words:


## Feature Vector Design

- Window size:
- How many words in the neighborhood?
- Tradeoff:
- +/. 500 words: 'topical context'
- +/- 1 or 2 words: collocations, predicate-argument


## Feature Vector Design

- Window size:
- How many words in the neighborhood?
- Tradeoff:
- +/. 500 words: 'topical context'
- +/. 1 or 2 words: collocations, predicate-argument
- Only words in some grammatical relation
- Parse text (dependency)
- Include subj-verb; verb-obj; adj-mod
- NxR vector: word x relation


## Context Windows

- Same corpus, different windows
- BNC
- Nearest neighbors of "dog"
- 2-word window:
- Cat, horse, fox, pet, rabbit, pig, animal, mongrel, sheep, pigeon
- 30-word window:
- Kennel, puppy, pet, terrier, Rottweiler, canine, cat, to bark, Alsatian


## Example Lin Relation Vector

|  | 0 0 0 0 0 0 0 0 $\vdots$ 3 $\vdots$ |  |  | ... | $\begin{aligned} & 0 \\ & \frac{0}{n} \\ & \vdots \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ | $\begin{aligned} & 0 \\ & : \\ & \hdashline \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ | ... |  |  |  | ... |  | $$ | $E$ 0 0 0 0 0 0 0 0 0 0 | $\begin{aligned} & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ | ... |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| cell | 1 | 1 | 1 |  | 16 | 30 |  | 3 | 8 | 1 |  | 6 | 11 | 3 | 2 |  | 3 | 2 | 2 |

## Document Context

- All models so far:
- Term x term (or term x relation)
- Alternatively:
- Term x document
- Vectors of occurrences (association) in "document"
- Document can be:
- Typically: article, essay, etc
- Also, utterance, dialog act
- Well-known term x document model:
- Latent Semantic Analysis (LSA)


## LSA Document Contexts

- (Deerwester et al, 1990)
- Titles of scientific articles
Example of text data: Titles of Some Technical Memos
c1: Human machine interface for ABC computer applications
c2: A survey of user opinion of computer system response time
c3: The EPS user interface management system
c4: System and human system engineering testing of EPS
c5: Relation of user perceived response time to error measurement
ml : The generation of random, binary, ordered trees
m2: The intersection graph of paths in trees
m3: Graph minors IV: Widths of trees and well-quasi-ordering
m4: Graph minors: A survey


## Document Context Representation

- Term x document:

|  | c1 | c2 | c3 | c4 | c5 | m1 | m2 | m3 | m4 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| human | 1 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 |
| interface | 1 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 |
| computer | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| user | 0 | 1 | 1 | 0 | 1 | 0 | 0 | 0 | 0 |
| system | 0 | 1 | 1 | 2 | 0 | 0 | 0 | 0 | 0 |
| response | 0 | 1 | 0 | 0 | 1 | 0 | 0 | 0 | 0 |
| time | 0 | 1 | 0 | 0 | 1 | 0 | 0 | 0 | 0 |
| EPS | 0 | 0 | 1 | 1 | 0 | 0 | 0 | 0 | 0 |
| survey | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 1 |
| trees | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 1 | 0 |
| graph | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 1 |
| minors | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 1 |

## Document Context Representation

- Term x document:
- $\operatorname{Corr}(h u m a n, u s e r)=-0.38 ; \operatorname{corr}(h u m a n, m i n o r s)=-0.29$

|  | c 1 | c2 | c3 | c4 | c5 | m1 | m2 | m3 | m4 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| human | 1 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 |
| interface | 1 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 |
| computer | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| user | 0 | 1 | 1 | 0 | 1 | 0 | 0 | 0 | 0 |
| system | 0 | 1 | 1 | 2 | 0 | 0 | 0 | 0 | 0 |
| response | 0 | 1 | 0 | 0 | 1 | 0 | 0 | 0 | 0 |
| time | 0 | 1 | 0 | 0 | 1 | 0 | 0 | 0 | 0 |
| EPS | 0 | 0 | 1 | 1 | 0 | 0 | 0 | 0 | 0 |
| survey | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 1 |
| trees | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 1 | 0 |
| graph | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 1 |
| minors | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 1 |

## Improved Representation

- Reduced dimension projection:
- Corr(human,user) $=0.98$; corr(human,minors)=-0.83

|  | c 1 | c 2 | c 3 | c 4 | c 5 | m 1 | m 2 | m 3 | m 4 |
| :--- | ---: | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| human | 0.16 | 0.40 | 0.38 | 0.47 | 0.18 | -0.05 | -0.12 | -0.16 | -0.09 |
| interface | 0.14 | 0.37 | 0.33 | 0.40 | 0.16 | -0.03 | -0.07 | -0.10 | -0.04 |
| computer | 0.15 | 0.51 | 0.36 | 0.41 | 0.24 | 0.02 | 0.06 | 0.09 | 0.12 |
| user | 0.26 | 0.84 | 0.61 | 0.70 | 0.39 | 0.03 | 0.08 | 0.12 | 0.19 |
| system | 0.45 | 1.23 | 1.05 | 1.27 | 0.56 | -0.07 | -0.15 | -0.21 | -0.05 |
| response | 0.16 | 0.58 | 0.38 | 0.42 | 0.28 | 0.06 | 0.13 | 0.19 | 0.22 |
| time | 0.16 | 0.58 | 0.38 | 0.42 | 0.28 | 0.06 | 0.13 | 0.19 | 0.22 |
| EPS | 0.22 | 0.55 | 0.51 | 0.63 | 0.24 | -0.07 | -0.14 | -0.20 | -0.11 |
| survey | 0.10 | 0.53 | 0.23 | 0.21 | 0.27 | 0.14 | 0.31 | 0.44 | 0.42 |
| trees | -0.06 | 0.23 | -0.14 | -0.27 | 0.14 | 0.24 | 0.55 | 0.77 | 0.66 |
| graph | -0.06 | 0.34 | -0.15 | -0.30 | 0.20 | 0.31 | 0.69 | 0.98 | 0.85 |
| minors | -0.04 | 0.25 | -0.10 | -0.21 | 0.15 | 0.22 | 0.50 | 0.71 | 0.62 |

## Weighting Features

- Baseline: Binary (0/1)


## Weighting Features

- Baseline: Binary (0/1)
- Minimally informative
- Can't capture intuition that frequent features informative


## Weighting Features

- Baseline: Binary (0/1)
- Minimally informative
- Can't capture intuition that frequent features informative
- Frequency or Probability:

$$
P(f \mid w)=\frac{\operatorname{count}(f, w)}{\operatorname{count}(w)}
$$

## Weighting Features

- Baseline: Binary (0/1)
- Minimally informative
- Can't capture intuition that frequent features informative
- Frequency or Probability:

$$
P(f \mid w)=\frac{\operatorname{count}(f, w)}{\operatorname{count}(w)}
$$

- Better but,


## Weighting Features

- Baseline: Binary (0/1)
- Minimally informative
- Can't capture intuition that frequent features informative
- Frequency or Probability:

$$
P(f \mid w)=\frac{\operatorname{count}(f, w)}{\operatorname{count}(w)}
$$

- Better but,
- Can overweight a priori frequent features
- Chance cooccurrence


## Pointwise Mutual Information <br> $\operatorname{assoc}_{P M I}(w, f)=\log _{2} \frac{P(w, f)}{P(w) P(f)}$

## PMI:

- Contrasts observed cooccurrence
- With that expected by chance (if independent)


## Pointwise Mutual Information <br> $\operatorname{assoc}_{P M I}(w, f)=\log _{2} \frac{P(w, f)}{P(w) P(f)}$

## PMI:

- Contrasts observed cooccurrence
- With that expected by chance (if independent)
- Generally only use positive values
- Negatives inaccurate unless corpus huge


## Lin Association

- Recall:
- Lin's vectors include:
- r: dependency relation
- w': other word in dependency relation
- Decomposes weights on that basis:

$$
\operatorname{assoc}_{\operatorname{Lin}}(w, f)=\log _{2} \frac{P(w, f)}{P(w) P(r \mid w) P\left(w^{\prime} \mid w\right)}
$$

## Vector Similarity

- Euclidean or Manhattan distances:


## Vector Similarity

- Euclidean or Manhattan distances:
- Too sensitive to extreme values


## Vector Similarity

- Euclidean or Manhattan distances:
- Too sensitive to extreme values
- Dot product: $\operatorname{sim}_{\text {dot-product }}(\vec{v}, \vec{w})=\vec{v} \bullet \vec{w}=\sum_{i=1}^{N} v_{i} \times w_{i}$


## Vector Similarity

- Euclidean or Manhattan distances:
- Too sensitive to extreme values
- Dot product: $\operatorname{sim}_{\text {dot-product }}(\vec{v}, \vec{w})=\vec{v} \bullet \vec{w}=\sum_{i=1}^{N} v_{i} \times w_{i}$
- More features or higher values


## Vector Similarity

- Euclidean or Manhattan distances:
- Too sensitive to extreme values
- Dot product: $\operatorname{sim}_{\text {dot-product }}(\vec{v}, \vec{w})=\vec{v} \bullet \vec{w}=\sum_{i=1}^{N} v_{i} \times w_{i}$
- More features or higher values

$$
\frac{\sum_{i=1}^{N} v_{i} \times w_{i}}{\sqrt{\sum_{i=1}^{N} v_{i}^{2}} \sqrt{\sum_{i=1}^{N} w_{i}^{2}}}
$$

- Cosine: $\operatorname{sim}_{\text {cosise }}(\vec{v}, \vec{w})=\frac{\sum_{i=1}}{\sqrt{\sum_{i=1}^{N}} v_{i}^{2}} \sqrt{\sum_{i=1}^{N} w_{i}^{2}}$


## Alternative Weighting Schemes

- Models have used alternate weights of computing similarity based on weighted overlap

$$
\begin{align*}
\operatorname{sim}_{\operatorname{cosine}}(\vec{v}, \vec{w}) & =\frac{\vec{v} \cdot \vec{w}}{|\vec{v}| \vec{w} \mid}=\frac{\sum_{i=1}^{N} v_{i} \times w_{i}}{\sqrt{\sum_{i=1}^{N} v_{i}^{2}} \sqrt{\sum_{i=1}^{N} w_{i}^{2}}}  \tag{20.47}\\
\operatorname{sim}_{\operatorname{Jaccard}}(\vec{v}, \vec{w}) & =\frac{\sum_{i=1}^{N} \min \left(v_{i}, w_{i}\right)}{\sum_{i=1}^{N} \max \left(v_{i}, w_{i}\right)}  \tag{20.48}\\
\operatorname{sim}_{\operatorname{Dice}}(\vec{v}, \vec{w}) & =\frac{2 \times \sum_{i=1}^{N} \min \left(v_{i}, w_{i}\right)}{\sum_{i=1}^{N}\left(v_{i}+w_{i}\right)} \tag{20.49}
\end{align*}
$$

## Results

- Based on Lin ${ }_{\text {assoc }}$
- Hope (N): optimism, chance, expectation, prospect, dream, desire, fear
- Hope (V): would like, wish, plan, say, believe, think
- Brief (N): legal brief, affidavit, filing, petition, document, argument, letter
- Brief (A): lengthy, hour-long, short, extended, frequent, recent, short-lived, prolonged, week-long


## Curse of Dimensionality

- Vector representations:
- Sparse
- Very high dimensional:
- \# words in vocabulary
- \# relations x \# words, etc


## Curse of Dimensionality

- Vector representations:
- Sparse
- Very high dimensional:
- \# words in vocabulary
- \# relations x \# words, etc
- Google1T5 corpus:
- 1M x 1M matrix


## Curse of Dimensionality

- Vector representations:
- Sparse
- Very high dimensional:
- \# words in vocabulary
- \# relations x \# words, etc
- Google1T5 corpus:
- $1 \mathrm{M} \times 1 \mathrm{M}$ matrix: $<0.05 \%$ non-zero values
- Computationally hard to manage
- Lots of zeroes
- Can miss underlying relations


## Reducing Dimensionality

- Feature selection:
- Desirable traits:


## Reducing Dimensionality

- Feature selection:
- Desirable traits:
- High frequency
- High variance


## Reducing Dimensionality

- Feature selection:
- Desirable traits:
- High frequency
- High variance
- Filtering:
- Can exclude terms with too few occurrences
- Can include only top X most frequent terms
- Chi-squared selection


## Reducing Dimensionality

- Feature selection:
- Desirable traits:
- High frequency
- High variance
- Filtering:
- Can exclude terms with too few occurrences
- Can include only top X most frequent terms
- Chi-squared selection
- Cautions:
- Feature correlations
- Joint feature selection complex, expensive


## Reducing Dimensionality

- Projection into lower dimensional space:
- Principal Components Analysis (PCA), Locality Preserving Projections (LPP), Singular Value Decomposition, etc
- Create new lower dimensional space that
- Preserves distances between data points
- Keep like with like
- Approaches differ on exactly what is preserved.


## SVD

- Enables creation of reduced dimension model
- Low rank approximation of original matrix
- Best-fit at that rank (in least-squares sense)


## SVD

- Enables creation of reduced dimension model
- Low rank approximation of original matrix
- Best-fit at that rank (in least-squares sense)
- Motivation:
- Original matrix: high dimensional, sparse
- Similarities missed due to word choice, etc
- Create new projected space
- More compact, better captures important variation
- Landauer et al argue identifies underlying "concepts"
- Across words with related meanings


## Diverse Applications

- Unsupervised POS tagging
- Word Sense Disambiguation
- Essay Scoring
- Document Retrieval
- Unsupervised Thesaurus Induction
- Ontology/Taxonomy Expansion
- Analogy tests, word tests
- Topic Segmentation


## Distributional Similarity for Word Sense Disambiguation

## Schutze's Word Space

- Build a co-occurrence matrix


## Schutze's Word Space

- Build a co-occurrence matrix
- Restrict Vocabulary to 4 letter sequences


## Schutze's Word Space

- Build a co-occurrence matrix
- Restrict Vocabulary to 4 letter sequences
- Similar effect to stemming
- Exclude Very Frequent - Articles, Affixes


## Schutze' s Word Space

- Build a co-occurrence matrix
- Restrict Vocabulary to 4 letter sequences
- Similar effect to stemming
- Exclude Very Frequent - Articles, Affixes
- Entries in 5000-5000 Matrix
- Apply Singular Value Decomposition (SVD)
- Reduce to 97 dimensions


## Schutze' s Word Space

- Build a co-occurrence matrix
- Restrict Vocabulary to 4 letter sequences
- Similar effect to stemming
- Exclude Very Frequent - Articles, Affixes
- Entries in 5000-5000 Matrix
- Apply Singular Value Decomposition (SVD)
- Reduce to 97 dimensions
- Word Context
- 4grams within 1001 Characters


## Word Representation

- $2^{\text {nd }}$ order representation:
- Identify words in context of w
- For each $x$ in context of $w$
- Compute x's vector representation
- Compute centroid of those $x$ vector representations


## Computing Word Senses

- Compute context vector for each occurrence of word in corpus
- Cluster these context vectors
- \# of clusters = \# number of senses
- Cluster centroid represents word sense
- Link to specific sense?


## Computing Word Senses

- Compute context vector for each occurrence of word in corpus
- Cluster these context vectors
- \# of clusters = \# number of senses
- Cluster centroid represents word sense
- Link to specific sense?
- Pure unsupervised: no sense tag, just $i^{\text {th }}$ sense
- Some supervision: hand label clusters, or tag training


## Disambiguating Instances

- To disambiguate an instance $t$ of $w$ :
- Compute context vector for the instance
- Retrieve all senses of $w$
- Assign w sense with closest centroid to $t$

There are more kinds of plants and animals in the rainforests than anywhere else on Earth. Over half of the millions of known species of plants and animals live in the rainforest. Many are found nowhere else. There are even plants and animals in the rainforest that we have not yet discovered.

## Biological Example

The Paulus company was founded in 1938. Since those days the product range has been the subject of constant expansions and is brought up continuously to correspond with the state of the art. We' re engineering, manufacturing and commissioning worldwide ready-to-run plants packed with our comprehensive knowhow. Our Product Range includes pneumatic conveying systems for carbon, carbide, sand, lime andmany others. We use reagent injection in molten metal for the...
Industrial Example
Label the First Use of "Plant"

## Example Sense Selection for Plant Data

- Build a Context Vector


## Example Sense Selection for Plant Data

- Build a Context Vector
- 1,001 character window - Whole Article


## Example Sense Selection for Plant Data

- Build a Context Vector
- 1,001 character window - Whole Article
- Compare Vector Distances to Sense Clusters


## Example Sense Selection for Plant Data

- Build a Context Vector
- 1,001 character window - Whole Article
- Compare Vector Distances to Sense Clusters
- Only 3 Content Words in Common
- Distant Context Vectors
- Clusters - Build Automatically, Label Manually


## Example Sense Selection for Plant Data

- Build a Context Vector
- 1,001 character window - Whole Article
- Compare Vector Distances to Sense Clusters
- Only 3 Content Words in Common
- Distant Context Vectors
- Clusters - Build Automatically, Label Manually
- Result: 2 Different, Correct Senses
- $92 \%$ on Pair-wise tasks


## Odd Cluster Examples

- The "Ste." Cluster:
- Dry Oyster Whisky Hot Float Ice


## Odd Cluster Examples

- The "Ste." Cluster:
- Dry Oyster Whisky Hot Float Ice
- Why? - River name


## Odd Cluster Examples

- The "Ste." Cluster:
- Dry Oyster Whisky Hot Float Ice
- Why? - River name
- Learning the Corpus, not the Sense
- Keeping cluster:
- Bring Hoping Wiping Could Should Some Them Rest


## Odd Cluster Examples

- The "Ste." Cluster:
- Dry Oyster Whisky Hot Float Ice
- Why? - River name
- Learning the Corpus, not the Sense
- Keeping cluster:
- Bring Hoping Wiping Could Should Some Them Rest
- Uninformative: Wide context misses verb sense


## Distributional Models

- Upsurge in distributional compositional models
- Neural network embeddings:
- Discriminatively trained, low dimensional reps
- E.g. word2vec
- Skipgrams etc over large corpora
- Composition:
- Methods for combining word vector models
- Capture phrasal, sentential meanings

Thesaurus-Based Similarity

## Thesaurus-based Techniques

- Key idea:
- Shorter path length in thesaurus, smaller semantic dist.


## Thesaurus-based Techniques

- Key idea:
- Shorter path length in thesaurus, smaller semantic dist.
- Words similar to parents, siblings in tree
- Further away, less similar


## Thesaurus-based Techniques

- Key idea:
- Shorter path length in thesaurus, smaller semantic dist.
- Words similar to parents, siblings in tree
- Further away, less similar
- Pathlength=\# edges in shortest route in graph b/t nodes


## Thesaurus-based Techniques

- Key idea:
- Shorter path length in thesaurus, smaller semantic dist.
- Words similar to parents, siblings in tree
- Further away, less similar
- Pathlength=\# edges in shortest route in graph b/t nodes
- $\operatorname{Sim}_{\text {path }}=-\log$ pathlen $\left(\mathrm{c}_{1}, \mathrm{c}_{2}\right)$ [Leacock \& Chodorow]


## Thesaurus-based Techniques

- Key idea:
- Shorter path length in thesaurus, smaller semantic dist.
- Words similar to parents, siblings in tree
- Further away, less similar
- Pathlength=\# edges in shortest route in graph b/t nodes
- $\operatorname{Sim}_{\text {path }}=-\log$ pathlen $\left(\mathrm{c}_{1}, \mathrm{c}_{2}\right)$ [Leacock \& Chodorow]
- Problem 1:


## Thesaurus-based Techniques

- Key idea:
- Shorter path length in thesaurus, smaller semantic dist.
- Words similar to parents, siblings in tree
- Further away, less similar
- Pathlength=\# edges in shortest route in graph b/t nodes
- $\operatorname{Sim}_{\text {path }}=-\log$ pathlen $\left(\mathrm{c}_{1}, \mathrm{c}_{2}\right)$ [Leacock \& Chodorow]
- Problem 1:
- Rarely know which sense, and thus which node


## Thesaurus-based Techniques

- Key idea:
- Shorter path length in thesaurus, smaller semantic dist.
- Words similar to parents, siblings in tree
- Further away, less similar
- Pathlength=\# edges in shortest route in graph b/t nodes
- $\operatorname{Sim}_{\text {path }}=-\log$ pathlen $\left(\mathrm{c}_{1}, \mathrm{c}_{2}\right)$ [Leacock \& Chodorow]
- Problem 1:
- Rarely know which sense, and thus which node
- Solution: assume most similar senses estimate


## Thesaurus-based Techniques

- Key idea:
- Shorter path length in thesaurus, smaller semantic dist.
- Words similar to parents, siblings in tree
- Further away, less similar
- Pathlength=\# edges in shortest route in graph b/t nodes
- $\operatorname{Sim}_{\text {path }}=-\log$ pathlen $\left(\mathrm{c}_{1}, \mathrm{c}_{2}\right)$ [Leacock \& Chodorow]
- Problem 1:
- Rarely know which sense, and thus which node
- Solution: assume most similar senses estimate
- Wordsim $\left(\mathrm{w}_{1}, \mathrm{w}_{2}\right)=\max \operatorname{sim}\left(\mathrm{c}_{1}, \mathrm{c}_{2}\right)$


## Path Length

- Path length problem:



## Path Length

- Path length problem:
- Links in WordNet not uniform
- Distance 5: Nickel->Money and Nickel->Standard



## Resnik's Similarity Measure

- Solution 1:


## Resnik's Similarity Measure

- Solution 1:
- Build position-specific similarity measure


## Resnik's Similarity Measure

- Solution 1:
- Build position-specific similarity measure
- Not general
- Solution 2 :


## Resnik's Similarity Measure

- Solution 1:
- Build position-specific similarity measure
- Not general
- Solution 2:
- Add corpus information: information-content measure
- P(c) : probability that a word is instance of concept c


## Resnik's Similarity Measure

- Solution 1:
- Build position-specific similarity measure
- Not general
- Solution 2:
- Add corpus information: information-content measure
- P(c) : probability that a word is instance of concept c
- Words(c) : words subsumed by concept c; N: words in corpus

$$
P(c)=\frac{\sum_{w \in w o r d s(c)} \operatorname{count}(w)}{N}
$$

## Resnik's Similarity Measure

- Information content of node:
- $\operatorname{IC}(\mathrm{c})=-\log P(c)$


## Resnik's Similarity Measure

- Information content of node:
- $\operatorname{IC}(\mathrm{c})=-\log \mathrm{P}(\mathrm{c})$
- Least common subsumer (LCS):
- Lowest node in hierarchy subsuming 2 nodes


## Resnik's Similarity Measure

- Information content of node:
- $\operatorname{IC}(\mathrm{c})=-\log \mathrm{P}(\mathrm{c})$
- Least common subsumer (LCS):
- Lowest node in hierarchy subsuming 2 nodes
- Similarity measure:
- $\operatorname{sim}_{\text {RESNIK }}\left(\mathrm{c}_{1}, \mathrm{c}_{2}\right)=\cdot \log \mathrm{P}\left(\operatorname{LCS}\left(\mathrm{c}_{1}, \mathrm{c}_{2}\right)\right)$


## Resnik's Similarity Measure

- Information content of node:
- $\operatorname{IC}(c)=-\log P(c)$
- Least common subsumer (LCS):
- Lowest node in hierarchy subsuming 2 nodes
- Similarity measure:
- $\operatorname{sim}_{\text {RESNIK }}\left(\mathrm{c}_{1}, \mathrm{c}_{2}\right)=\cdot \log \mathrm{P}\left(\operatorname{LCS}\left(\mathrm{c}_{1}, \mathrm{c}_{2}\right)\right)$
- Issue:


## IC Example



## Resnik's Similarity Measure

- Information content of node:
- $\operatorname{IC}(\mathrm{c})=-\log \mathrm{P}(\mathrm{c})$
- Least common subsumer (LCS):
- Lowest node in hierarchy subsuming 2 nodes
- Similarity measure:
- $\operatorname{sim}_{\text {RESNIK }}\left(\mathrm{C}_{1}, \mathrm{c}_{2}\right)=\cdot \log \mathrm{P}\left(\operatorname{LCS}\left(\mathrm{c}_{1}, \mathrm{c}_{2}\right)\right)$
- Issue:
- Not content, but difference between node \& LCS


## Resnik's Similarity Measure

- Information content of node:
- $\operatorname{IC}(c)=-\log P(c)$
- Least common subsumer (LCS):
- Lowest node in hierarchy subsuming 2 nodes
- Similarity measure:
- $\operatorname{sim}_{\text {RESNIK }}\left(\mathrm{c}_{1}, \mathrm{c}_{2}\right)=\cdot \log \mathrm{P}\left(\operatorname{LCS}\left(\mathrm{c}_{1}, \mathrm{c}_{2}\right)\right)$
- Issue:
- Not content, but difference between node \& LCS

$$
\operatorname{sim}_{\text {Lin }}\left(c_{1}, c_{2}\right)=\frac{2 \times \log P\left(L C S\left(c_{1}, c_{2}\right)\right)}{\log P\left(c_{1}\right)+\log P\left(c_{2}\right)}
$$

## Application to WSD

- Calculate Informativeness
- For Each Node in WordNet:


## Application to WSD

- Calculate Informativeness
- For Each Node in WordNet:
- Sum occurrences of concept and all children
- Compute IC


## Application to WSD

- Calculate Informativeness
- For Each Node in WordNet:
- Sum occurrences of concept and all children
- Compute IC
- Disambiguate with WordNet


## Application to WSD

- Calculate Informativeness
- For Each Node in WordNet:
- Sum occurrences of concept and all children
- Compute IC
- Disambiguate with WordNet
- Assume set of words in context
- E.g. \{plants, animals, rainforest, species\} from article


## Application to WSD

- Calculate Informativeness
- For Each Node in WordNet:
- Sum occurrences of concept and all children
- Compute IC
- Disambiguate with WordNet
- Assume set of words in context
- E.g. \{plants, animals, rainforest, species\} from article
- Find Most Informative Subsumer for each pair, I
- Find LCS for each pair of senses, pick highest similarity


## Application to WSD

- Calculate Informativeness
- For Each Node in WordNet:
- Sum occurrences of concept and all children
- Compute IC
- Disambiguate with WordNet
- Assume set of words in context
- E.g. \{plants, animals, rainforest, species\} from article
- Find Most Informative Subsumer for each pair, I
- Find LCS for each pair of senses, pick highest similarity
- For each subsumed sense, Vote += I


## Application to WSD

- Calculate Informativeness
- For Each Node in WordNet:
- Sum occurrences of concept and all children
- Compute IC
- Disambiguate with WordNet
- Assume set of words in context
- E.g. \{plants, animals, rainforest, species\} from article
- Find Most Informative Subsumer for each pair, I
- Find LCS for each pair of senses, pick highest similarity
- For each subsumed sense, Vote += I
- Select Sense with Highest Vote

There are more kinds of plants and animals in the rainforests than anywhere else on Earth. Over half of the millions of known species of plants and animals live in the rainforest. Many are found nowhere else. There are even plants and animals in the rainforest that we have not yet discovered.

## Biological Example

The Paulus company was founded in 1938. Since those days the product range has been the subject of constant expansions and is brought up continuously to correspond with the state of the art. We' re engineering, manufacturing and commissioning worldwide ready-to-run plants packed with our comprehensive knowhow. Our Product Range includes pneumatic conveying systems for carbon, carbide, sand, lime and many others. We use reagent injection in molten metal for the...
Industrial Example
Label the First Use of "Plant"

## Sense Labeling Under WordNet

- Use Local Content Words as Clusters
- Biology: Plants, Animals, Rainforests, species...
- Industry: Company, Products, Range, Systems...


## Sense Labeling Under WordNet

- Use Local Content Words as Clusters
- Biology: Plants, Animals, Rainforests, species...
- Industry: Company, Products, Range, Systems...
- Find Common Ancestors in WordNet


## Sense Labeling Under WordNet

- Use Local Content Words as Clusters
- Biology: Plants, Animals, Rainforests, species...
- Industry: Company, Products, Range, Systems...
- Find Common Ancestors in WordNet
- Biology: Plants \& Animals isa Living Thing


## Sense Labeling Under WordNet

- Use Local Content Words as Clusters
- Biology: Plants, Animals, Rainforests, species...
- Industry: Company, Products, Range, Systems...
- Find Common Ancestors in WordNet
- Biology: Plants \& Animals isa Living Thing
- Industry: Product \& Plant isa Artifact isa Entity


## Sense Labeling Under WordNet

- Use Local Content Words as Clusters
- Biology: Plants, Animals, Rainforests, species...
- Industry: Company, Products, Range, Systems...
- Find Common Ancestors in WordNet
- Biology: Plants \& Animals isa Living Thing
- Industry: Product \& Plant isa Artifact isa Entity
- Use Most Informative
- Result: Correct Selection


## Thesaurus Similarity Issues

## Thesaurus Similarity Issues

- Coverage:
- Few languages have large thesauri


## Thesaurus Similarity Issues

- Coverage:
- Few languages have large thesauri
- Few languages have large sense tagged corpora


## Thesaurus Similarity Issues

- Coverage:
- Few languages have large thesauri
- Few languages have large sense tagged corpora
- Thesaurus design:
- Works well for noun IS-A hierarchy


## Thesaurus Similarity Issues

- Coverage:
- Few languages have large thesauri
- Few languages have large sense tagged corpora
- Thesaurus design:
- Works well for noun IS-A hierarchy
- Verb hierarchy shallow, bushy, less informative


## Naïve Bayes’ Approach

- Supervised learning approach
- Input: feature vector X label


## Naïve Bayes’ Approach

- Supervised learning approach
- Input: feature vector X label
- Best sense = most probable sense given f

$$
\begin{aligned}
& \hat{s}=\underset{s \in S}{\arg \max } P(s \mid \vec{f}) \\
& \hat{s}=\underset{s \in S}{\arg \max } \frac{P(\vec{f} \mid s) P(s)}{P(\vec{f})}
\end{aligned}
$$

## Naïve Bayes’ Approach

- Issue:
- Data sparseness: full feature vector rarely seen


## Naïve Bayes’ Approach

- Issue:
- Data sparseness: full feature vector rarely seen
- "Naïve" assumption:
- Features independent given sense

$$
\begin{aligned}
& P(\vec{f} \mid s) \approx \prod_{j=1}^{n} P\left(f_{j} \mid s\right) \\
& \hat{s}=\underset{s \in S}{\operatorname{argmax}} P(s) \prod_{j=1}^{n} P\left(f_{j} \mid s\right)
\end{aligned}
$$

## Training NB Classifier

$\hat{s}=\underset{s \in S}{\operatorname{argmax}} P(s) \prod_{j=1}^{n} P\left(f_{j} \mid s\right)$

- Estimate P(s):
- Prior


## Training NB Classifier

$\hat{s}=\underset{s \in S}{\operatorname{argmax}} P(s) \prod_{j=1}^{n} P\left(f_{j} \mid s\right)$

- Prior

$$
P\left(s_{i}\right)=\frac{\operatorname{count}\left(s_{i}, w_{j}\right)}{\operatorname{count}\left(w_{j}\right)}
$$

## Training NB Classifier

$\hat{s}=\underset{s \in S}{\operatorname{argmax}} P(s) \prod_{j=1}^{n} P\left(f_{j} \mid s\right)$

- Prior

$$
P\left(s_{i}\right)=\frac{\operatorname{count}\left(s_{i}, w_{j}\right)}{\operatorname{count}\left(w_{j}\right)}
$$

- Estimate $P\left(f_{j} \mid s\right)$


## Training NB Classifier

$\hat{s}=\underset{s \in s}{\operatorname{argmax}} P(s) \prod_{j=1}^{n} P\left(f_{j} \mid s\right)$

- Estimate P(s):
- Prior

$$
P\left(s_{i}\right)=\frac{\operatorname{count}\left(s_{i}, w_{j}\right)}{\operatorname{count}\left(w_{j}\right)}
$$

- Estimate $\mathrm{P}\left(\mathrm{f}_{j} \mid \mathrm{s}\right) \quad P\left(f_{j} \mid s\right)=\frac{\operatorname{count}\left(f_{j}, s\right)}{\operatorname{count}(s)}$
- Issues:


## Training NB Classifier

$\hat{s}=\underset{s \in s}{\operatorname{argmax}} P(s) \prod_{j=1}^{n} P\left(f_{j} \mid s\right)$

- Estimate P(s):
- Prior

$$
P\left(s_{i}\right)=\frac{\operatorname{count}\left(s_{i}, w_{j}\right)}{\operatorname{count}\left(w_{j}\right)}
$$

- Estimate $\mathrm{P}\left(\mathrm{f}_{j} \mid \mathrm{s}\right) \quad P\left(f_{j} \mid s\right)=\frac{\operatorname{count}\left(f_{j}, s\right)}{\operatorname{count}(s)}$
- Issues:

$$
P\left(f_{j} \mid s\right)=\frac{\operatorname{count}\left(f_{j}, s\right)}{\operatorname{count}(s)}
$$

- Underflow => log prob


## Training NB Classifier

$\hat{s}=\underset{s \in s}{\operatorname{argmax}} P(s) \prod_{j=1}^{n} P\left(f_{j} \mid s\right)$

- Estimate P(s):
- Prior

$$
P\left(s_{i}\right)=\frac{\operatorname{count}\left(s_{i}, w_{j}\right)}{\operatorname{count}\left(w_{j}\right)}
$$

- Estimate $\mathrm{P}\left(\mathrm{f}_{j} \mid \mathrm{s}\right) \quad P\left(f_{j} \mid s\right)=\frac{\operatorname{count}\left(f_{j}, s\right)}{\operatorname{count}(s)}$
- Issues:
- Underflow => log prob
- Sparseness => smoothing

