CKY Algorithm, Chomsky Normal Form

Scott Farrar CLMA, University of Washington

January 13, 2010

Today's lecture

- Brief review
- 2 CKY algorithm
- 3 Chomsky Normal Form (CNF)
- 4 Homework2

• Name one reason why bottom-up parsing is inefficient?

Name one reason why bottom-up parsing is inefficient?
 The [search for Spock] was successful.

- Name one reason why bottom-up parsing is inefficient?
 The [search for Spock] was successful.
- And for top-down?

- Name one reason why bottom-up parsing is inefficient?
 The [search for Spock] was successful.
- And for top-down?
 Which would you like?
 That one.

- Name one reason why bottom-up parsing is inefficient?
 The [search for Spock] was successful.
- And for top-down?
 Which would you like?
 That one.
- And what makes naive search so inefficient?

- Name one reason why bottom-up parsing is inefficient?
 The [search for Spock] was successful.
- And for top-down?
 Which would you like?
 That one.
- And what makes naive search so inefficient?
 There's no way to store intermediate solutions.

Cocke-Kasami-Younger (CKY) algorithm: a fast bottom-up parsing algorithm that avoids some of the inefficiency associated with purely naive search with the same bottom-up strategy.

• Intermediate solutions are stored.

- Intermediate solutions are stored.
- Only intermediate solutions that contribute to a full parse are further pursued.

- Intermediate solutions are stored.
- Only intermediate solutions that contribute to a full parse are further pursued.
- The CKY is picky about what type of grammar it accepts.

- Intermediate solutions are stored.
- Only intermediate solutions that contribute to a full parse are further pursued.
- The CKY is picky about what type of grammar it accepts.
- We require that our grammar be in a special form, known as Chomsky Normal Form (CNF).

- Intermediate solutions are stored.
- Only intermediate solutions that contribute to a full parse are further pursued.
- The CKY is picky about what type of grammar it accepts.
- We require that our grammar be in a special form, known as Chomsky Normal Form (CNF).
- The rationale is to fill in a chart with the solutions to the subproblems encountered in the bottom-up parsing process.

Dynamic programming

Definition

Dynamic programming: a method of reducing the runtime of algorithms by discovering solutions to subproblems along the way to the solution of the main problem; to optimally plan a multi-stage process

- good for problems with overlapping subproblems
- generally involves the caching of partial results in a table for later retrieval
- many application (outside of NLP)

What are the subproblems for the parsing task?



Well-formed substring table (WFST)

Definition

A well-formed substring table is a data structure containing partial constituency structures. It may be represented as either a chart or a graph.

Well-formed substring table (WFST)

Example

the brown dog

 $NP \rightarrow DT$ Nom, Nom \rightarrow JJ NN, $DT \rightarrow the$, etc.

the	brown	dog
DT_1		NP_5
	JJ_2	Nom ₄
		NN_3

Numbers indicate order in which symbol was enterred into table.

Setting up the CKY algorithm

- For an input of length=n, create a matrix $(n + 1 \times n + 1)$, indexed from 0 to n.
- 2 Each cell in the matrix [i,j] is the set of all categories of constituents spanning from position i to j.
- The algorithm forces you to fill in the table in the most efficient way.
- Process cells left to right (across columns), bottom to top (backwards across rows).

Well-formed substring table (WFST)

Example

the brown dog

 $NP \rightarrow DT$ Nom, Nom \rightarrow JJ NN, $DT \rightarrow the$, etc.

the	brown	dog
DT_1		NP_5
	JJ_2	Nom ₄
		NN_3

Numbers indicate order in which symbol was enterred into table.

CKY: assumptions

Critical observation: any portion of the input string spanning i to j can be split at k, and structure can then be built using sub-solutions spanning i to k and sub-solutions spanning k to j.

Example

- \bullet_0 the \bullet_1 brown \bullet_2 dog \bullet_3
 - k = 1: possible constituents are [0,1] and [1,3]
 - k = 2: possible constituents are [0,2] and [2,3]

Simple grammar

```
S \rightarrow NP \ VBZ
                            DT \rightarrow the
S \rightarrow NP VP
                            NN \rightarrow chef
VP \rightarrow VP PP
                            NNS \rightarrow fish
VP \rightarrow VBZ NP
                            NNS → chopsticks
VP \rightarrow VB7 PP
                            VBP \rightarrow fish
VP \rightarrow VBZ NNS
                           VBZ \rightarrow eats
VP \rightarrow VBZ VP
                            IN \rightarrow with
VP \rightarrow VBP NP
VP \rightarrow VBP PP
NP \rightarrow DT NN
NP \rightarrow DT NNS
PP \rightarrow IN NP
```

 $[\]bullet_0$ the \bullet_1 chef \bullet_2 eats \bullet_3 fish \bullet_4 with \bullet_5 the \bullet_6 chopsticks \bullet_7

0	1	2	3	4	5	6	7
0							
1							
2							
3							
4							
5							
6							

Build an $n+1 \times n+1$ matrix, where n = number of words in input

	the	chef	eats	fish	with	the	chopsticks
0	1	2	3	4	5	6	7
0	[0,1]						
1		[1,2]					
2			[2,3]				
3				[3,4]			
4					[4,5]		
5						[5,6]	
6							[6,7]

Illustrate the numbering of cells: [i,j]'s represent spans.

	the	chef	eats	fish	with	the	chopsticks
0	1	2	3	4	5	6	7
0							
1		[1,2]					
2							
3							
4							
5							
6							

Notice how the spans (e.g, [1,2]) differ from the word indices (e.g, 'chef', 2).

	the	chef	eats	fish	with	the	chopsticks
0	1	2	3	4	5	6	7
0	DT						
	[0,1]						
1		[1,2]					
2			[2,3]				
3				[3,4]			
					[4,5]		
5						[5,6]	
6							[6,7]

^{&#}x27;the' is labelled DT

	the	chef	eats	fish	with	the	chopsticks
0	1	2	3	4	5	6	7
0	DT						
	[0,1]						
1		NN [1,2]					
2			[2,3]				
3				[3,4]			
4					[4,5]		
5						[5,6]	
6							[6,7]

^{&#}x27;chef' is labelled NN

	the	chef	eats	fish	with	the	chopsticks
0	1	2	3	4	5	6	7
0	DT [0,1]	NP [0,2]					
1		NN [1,2]					
2			[2,3]				
3				[3,4]			
4					[4,5]		
5						[5,6]	
6							[6,7]

Found an NP: [0,1], [1,2]

	the	chef	eats	fish	with	the	chopsticks
0	1	2	3	4	5	6	7
0	DT	NP [0,2]					
	[0,1]						
1		NN [1,2]					
2			VBZ				
			[2,3]				
3				[3,4]			
4					[4,5]		
5						[5,6]	
6							[6,7]

^{&#}x27;eats' is labelled VBZ

	the	chef	eats	fish	with	the	chopsticks
0	1	2	3	4	5	6	7
0	DT [0,1]	NP [0,2]	S [0,3]				
1		NN [1,2]					
2			VBZ				
			[2,3]				
3				[3,4]			
4					[4,5]		
5						[5,6]	
6							[6,7]

Found an S: [0,2],[2,3]

	the	chef	eats	fish	with	the	chopsticks
0	1	2	3	4	5	6	7
0	DT	NP [0,2]	S [0,3]				
	[0,1]						
1		NN [1,2]					
2			VBZ				
			[2,3]				
3				NNS			
				[3,4]			
4					[4,5]		
5						[5,6]	
6							[6,7]

^{&#}x27;fish' is labelled NNS

	the	chef	eats	fish	with	the	chopsticks
0	1	2	3	4	5	6	7
0	DT	NP [0,2]	S [0,3]				
	[0,1]						
1		NN [1,2]					
2			VBZ				
			[2,3]				
3				NNS,VBP			
				[3,4]			
4					[4,5]		
5						[5,6]	
6							[6,7]

^{&#}x27;fish' is labelled VBP

	the	chef	eats	fish	with	the	chopsticks
0	1	2	3	4	5	6	7
0	DT [0,1]	NP [0,2]	S [0,3]				
1		NN [1,2]					
2			VBZ [2,3]	VP [2,4]			
3				NNS,VBP [3,4]			
4					[4,5]		
5						[5,6]	
6							[6,7]

Found a VP: [2,3], [3,4]

	the	chef	eats	fish	with	the	chopsticks
0	1	2	3	4	5	6	7
0	DT [0,1]	NP [0,2]	S [0,3]	S [0,4]			
1		NN [1,2]					
2			VBZ [2,3]	VP [2,4]			
3				NNS,VBP [3,4]			
4					[4,5]		
5						[5,6]	
6							[6,7]

Found an S: [0,2],[2,4]

	the	chef	eats	fish	with	the	chopsticks
0	1	2	3	4	5	6	7
0	DT	NP [0,2]	S [0,3]	S [0,4]			
	[0,1]						
1		NN [1,2]					
2			VBZ	VP [2,4]			
			[2,3]				
3				NNS,VBP			
				[3,4]			
4					IN [4,5]		
5						[5,6]	
6							[6,7]

^{&#}x27;with' is labelled IN

	the	chef	eats	fish	with	the	chopsticks
0	1	2	3	4	5	6	7
0	DT	NP [0,2]	S [0,3]	S [0,4]			
	[0,1]						
1		NN [1,2]					
2			VBZ	VP [2,4]			
			[2,3]				
3				NNS,VBP			
				[3,4]			
4					IN [4,5]		
5						DT [5,6]	
6							[6,7]

^{&#}x27;the' is labelled DT

	the	chef	eats	fish	with	the	chopsticks
0	1	2	3	4	5	6	7
0	DT [0,1]	NP [0,2]	S [0,3]	S [0,4]			
1		NN [1,2]					
2			VBZ [2,3]	VP [2,4]			
3				NNS,VBP [3,4]			
4					IN [4,5]		
5						DT [5,6]	
6							NNS [6,7]

^{&#}x27;chopsticks' is labelled NNS

the	chef	eats	fish	with	the	chopsticks
1	2	3	4	5	6	7
DT	NP [0,2]	S [0,3]	S [0,4]			
[0,1]						
	NN [1,2]					
		VBZ	VP [2,4]			
		[2,3]				
			NNS,VBP			
			[3,4]			
				IN [4,5]		
					DT [F 6]	ND [F 7]
					[5,6] וע	NP [5,7]
						NNS
						[6,7]
	1 DT	1 2 DT NP [0,2] [0,1]	1 2 3 DT NP [0,2] S [0,3] [0,1] NN [1,2] VBZ	1 2 3 4 DT NP [0,2] S [0,3] S [0,4] [0,1] NN [1,2] VBZ [2,3] VP [2,4] NNS,VBP	1 2 3 4 5 DT NP [0,2] S [0,3] S [0,4] [0,1] NN [1,2] VBZ [2,3] VP [2,4] NNS,VBP [3,4]	1 2 3 4 5 6 DT NP [0,2] S [0,3] S [0,4] [0,1] NN [1,2] VBZ [2,3] VP [2,4] NNS,VBP [3,4]

Found an NP: [5,6], [6,7]

	the	chef	eats	fish	with	the	chopsticks
0	1	2	3	4	5	6	7
0	DT	NP [0,2]	S [0,3]	S [0,4]			
	[0,1]						
1		NN [1,2]					
2			VBZ	VP [2,4]			
			[2,3]				
3				NNS,VBP			
				[3,4]			
4					INI [4 E]		DD [4 7]
					IN [4,5]		PP [4,7]
5						DT [5,6]	NP [5,7]
6							NNS
O							
		[1 <u>-1</u> _1					[6,7]

Found a PP: [4,5],[5,7]

	the	chef	eats	fish	with	the	chopsticks
0	1	2	3	4	5	6	7
0	DT	NP [0,2]	S [0,3]	S [0,4]			
	[0,1]						
1		NN [1,2]					
2			VBZ	VP [2,4]			
			[2,3]				
3				NNS, VBP			\/D [2 7]
				[3,4]			VP [3,7]
4					IN [4,5]		DD [4 7]
							PP [4,7]
5						DT [5,6]	NP [5,7]
6							NNS
							[6,7]

Found a VP: [3,4], [4,7]

	the	chef	eats	fish	with	the	chopsticks
0	1	2	3	4	5	6	7
0	DT [0,1]	NP [0,2]	S [0,3]	S [0,4]			
1		NN [1,2]					
2			VBZ [2,3]	VP [2,4]			VP [2,7]
3				NNS,VBP [3,4]			VP [3,7]
4					IN [4,5]		PP [4,7]
5						DT [5,6]	NP [5,7]
6							NNS [6,7]

Found a VP: [2,3],[3,7]

	the	chef	eats	fish	with	the	chopsticks
0	1	2	3	4	5	6	7
0	DT	NP [0,2]	S [0,3]	S [0,4]			
	[0,1]						
1		NN [1,2]					
2			VBZ	\/D [0.4]			VP_1 , VP_2
			[2,3]	VP [2,4]			[2,7]
3				NNS,VBP			VP [3,7]
				[3,4]			
4					IN [4,5]		DD [4 7]
							PP [4,7]
5						DT [5,6]	NP [5,7]
6							NNS
							[6,7]

Found another VP: [2,4],[4,7]

	the	chef	eats	fish	with	the	chopsticks
0	1	2	3	4	5	6	7
0	DT [0,1]	NP [0,2]	S [0,3]	S [0,4]			S [0,7]
1		NN [1,2]					
2			VBZ [2,3]	VP [2,4]			VP ₁ , VP ₂ [2,7]
3				NNS,VBP [3,4]			VP [3,7]
4					IN [4,5]		PP [4,7]
5						DT [5,6]	NP [5,7]
6							NNS [6,7]

Found an S node: [0,2] [2,7]

	the	chef	eats	fish	with	the	chopsticks
0	1	2	3	4	5	6	7
0	DT [0,1]	NP [0,2]	S [0,3]	S [0,4]			S ₁ , S ₂ [0,7]
1		NN [1,2]					
2			VBZ	VP [2,4]			VP_1 , VP_2
			[2,3]				[2,7]
3				NNS,VBP			VP [3,7]
				[3,4]			
4					IN [4,5]		PP [4,7]
5						DT [5,6]	NP [5,7]
6							NNS
							[6,7]

Found a second S node: also [0,2] [2,7]

	the	chef	eats	fish	with	the	chopsticks
0	1	2	3	4	5	6	7
0	DT [0,1]	NP [0,2]	S [0,3]	S [0,4]			S ₁ , S ₂ [0,7]
1		NN [1,2]					
2			VBZ	VP [2,4]			VP_1 , VP_2
			[2,3]				[2,7]
3				NNS,VBP			VP [3,7]
				[3,4]			
4					IN [4,5]		PP [4,7]
5						DT [5,6]	NP [5,7]
6							NNS
							[6,7]

Found a second S node: also [0,2] [2,7]

Recognition algorithm returns True when a root node is found in [0,n]



The CKY Algorithm (recognition)

```
function CKY-Parse (words, grammar) returns table
          for j \leftarrow 1 to length(words) do: (loop over columns)
               table[i-1,i] \leftarrow \{A|A \rightarrow words[i] \in grammar\} \text{ (add POS)}
               for i \leftarrow j-2 downto 0 do: (loop over rows, backwards)
                   for k \leftarrow i+1 to j-1 do: (loop over contents of cell)
                   table[i,i] \leftarrow table[i,i] \cup
                              \{A|A \rightarrow B \ C \in grammar.
                              B \in table[i,k]
                              C \in table[k,i]
```

CKY recognition vs. parsing

- Returning the full parse requires storing more in a cell than just a node label.
- We also require back-pointers to constituents of that node.
- We could also store whole trees, but less space efficient.
- For parsing, we must add an extra step to the algorithm:

CKY recognition vs. parsing

- Returning the full parse requires storing more in a cell than just a node label.
- We also require back-pointers to constituents of that node.
- We could also store whole trees, but less space efficient.
- For parsing, we must add an extra step to the algorithm: follow pointers and return the parse

The CKY Algorithm (parsing)

```
function CKY-Parse (words, grammar) returns parses
          for i \leftarrow 1 to length(words) do: (loop over columns)
              table[j-1,j] \leftarrow for all \{A|A \rightarrow words[j] \in grammar\} \text{ (add all POS)}
              for i \leftarrow j-2 downto 0 do: (loop over rows, backwards)
                  for k \leftarrow i+1 to i-1 do: (loop over contents of cell)
                      for all \{A|A \rightarrow B \ C\}: (all productions)
                      back[i,j,A] \leftarrow \{ k,B,C \}  (add back pointer)
          return buildtree(back[1, length(words,S]), table[1,LENGTH(words),S]
          (follow back pointer)
```

Issues with CKY

Efficiency

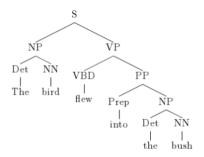
- The CKY can be performed in cubic time: $O(n^3)$, where n=number of words in sentence.
- The complexity of the inner most loop is bounded by the square of the number of non-terminals.
- The more rules, the less efficient; but this increases at a constant rate $L = r^2$ where r is the number of non-terminals.

Issues with CKY

Grammar requirements

- The basic algoritm requires a binary grammar, in fact a grammar in Chomsky Normal Form.
- Basic algorithm can be extended to account for arbitrary CFGs.
- However, transforming a grammar into a CNF grammar is easier and more efficient than parsing with an arbitrary grammar.
- Later, we'll look at the Earley Algorithm for parsing arbitrary CFGs.

Binary tree



Chomsky Normal Form grammar

Definition

CNF grammar: a context-free grammar where the RHS of each production rule is restricted to be either two non-terminals or one terminal, and no empty productions are allowed.

There can be:

- no mixed rules (NP → the NN)
- no unit productions ($NP \rightarrow NNP$), except for $NN \rightarrow dog$
- no right hand sides of more than two non-terminals $(VP \rightarrow VBZ \ NP \ PP)$.

Grammar equivalence

Any CFG can be converted to a weakly equivalent grammar in CNF.

Grammar equivalence

Any CFG can be converted to a weakly equivalent grammar in CNF.

Definition

Weak equivalence: Two grammars are weakly equivalent if they generate the same set of strings (sentences). Transforming a grammar to CNF results in a new grammar that is weakly equivalent.

Grammar equivalence

Any CFG can be converted to a weakly equivalent grammar in CNF.

Definition

Weak equivalence: Two grammars are weakly equivalent if they generate the same set of strings (sentences). Transforming a grammar to CNF results in a new grammar that is weakly equivalent.

Definition

Strong equivalence: Two grammars are strongly equivalent if they generate the same set of strings AND the same structures over those strings. If only the variable names are diff. then the grammar are said to be *isomorphic*.

Symbol naming conventions

- Use new symbols (binarization): X1, X2, ..., Y3 $S \rightarrow NP \ VP \ PUNC$ becomes: $S \rightarrow NP \ X1, X1 \rightarrow VP \ PUNC$
- Delete a symbol (unary collapsing): $SBAR \rightarrow S$, $S \rightarrow NP \ VP$ becomes $SBAR \rightarrow NP \ VP$

CNF conversion algorithm

- Removing unit-productions (unary collapsing):
 - while there is a unit-production $A \rightarrow B$,
 - Remove $A \rightarrow B$.
 - foreach $B \rightarrow u$, add $A \rightarrow u$.

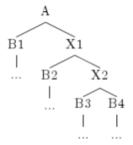
CNF conversion algorithm

- Removing unit-productions (unary collapsing):
 - while there is a unit-production $A \rightarrow B$,
 - Remove $A \rightarrow B$.
 - foreach $B \rightarrow u$, add $A \rightarrow u$.
- 2 Remove terminals from mixed rules
 - **foreach** production $A \rightarrow B_1 \ B_2...B_k$, containing a terminal x
 - Add new non-terminal/production $X1 \rightarrow x$ (unless it has already been added)
 - Replace every $B_i = x$ with X1

CNF conversion algorithm

- Removing unit-productions (unary collapsing):
 - while there is a unit-production $A \rightarrow B$,
 - Remove $A \rightarrow B$.
 - foreach $B \rightarrow u$, add $A \rightarrow u$.
- 2 Remove terminals from mixed rules
 - **foreach** production $A \rightarrow B_1 \ B_2 ... B_k$, containing a terminal x
 - Add new non-terminal/production $X1 \rightarrow x$ (unless it has already been added)
 - Replace every $B_i = x$ with X1
- Remove rules with more than two nonterminals on the RHS (binarization)
 - **foreach** rule *p* of form $A \rightarrow B_1 \ B_2...B_k$
 - replace p with $A \rightarrow B_1 X1$, $X1 \rightarrow B_2 X2$, $X2 \rightarrow B_3 X3$, ..., $X(k-2) \rightarrow B_{k-1} B_k$ (Xi's are new variables.)

Binarization



 $S \rightarrow NP \ VP \ PUNC$

 $S \rightarrow NP \ VP \ PUNC \ (non-binary)$

$$S \rightarrow NP \ VP \ PUNC$$
 (non-binary)
 $S \rightarrow S \ and \ S$

```
S \rightarrow NP \ VP \ PUNC  (non-binary)

S \rightarrow S \ and \ S  (mixed)

NP \rightarrow DT \ NP
```

```
S \rightarrow NP \ VP \ PUNC \ (non-binary) S \rightarrow S \ and \ S \ (mixed) NP \rightarrow DT \ NP \ (OK)
```

$$S \rightarrow NP \ VP \ PUNC$$
 (non-binary)
 $S \rightarrow S \ and \ S$ (mixed)
 $NP \rightarrow DT \ NP$ (OK)
 $NP \rightarrow NN$

```
S 	o NP \ VP \ PUNC \ (non-binary)

S 	o S \ and \ S \ (mixed)

NP 	o DT \ NP \ (OK)

NP 	o NN \ (unit production)
```

```
S 	o NP \ VP \ PUNC \quad \text{(non-binary)} S 	o S \ and \ S \quad \text{(mixed)} NP 	o DT \ NP \quad \text{(OK)} NP 	o NN \quad \text{(unit production)} NN 	o dog
```

```
S \rightarrow NP \ VP \ PUNC \quad \text{(non-binary)}
S \rightarrow S \ and \ S \quad \text{(mixed)}
NP \rightarrow DT \ NP \quad \text{(OK)}
NP \rightarrow NN \quad \text{(unit production)}
NN \rightarrow dog \quad \text{(OK)}
```

```
S \rightarrow NP \ VP \ PUNC \ (non-binary)

S \rightarrow S \ and \ S \ (mixed)

NP \rightarrow DT \ NP \ (OK)

NP \rightarrow NN \ (unit production)

NN \rightarrow dog \ (OK)

NN \rightarrow cat
```

```
S \rightarrow NP \ VP \ PUNC \ (non-binary)

S \rightarrow S \ and \ S \ (mixed)

NP \rightarrow DT \ NP \ (OK)

NP \rightarrow NN \ (unit production)

NN \rightarrow dog \ (OK)

NN \rightarrow cat \ (OK)

VP \rightarrow VBZ \ NP \ (OK)

VP \rightarrow VBZ
```

```
S 	o NP \ VP \ PUNC \ (non-binary)
S 	o S \ and \ S \ (mixed)
NP 	o DT \ NP \ (OK)
NP 	o NN \ (unit production)
NN 	o dog \ (OK)
NN 	o cat \ (OK)
VP 	o VBZ \ NP \ (UNIT production)
VBZ 	o sleeps
```

```
S \rightarrow NP \ VP \ PUNC \ (non-binary)

S \rightarrow S \ and \ S \ (mixed)

NP \rightarrow DT \ NP \ (OK)

NP \rightarrow NN \ (unit production)

NN \rightarrow dog \ (OK)

NN \rightarrow cat \ (OK)

VP \rightarrow VBZ \ NP \ (OK)

VP \rightarrow VBZ \rightarrow sleeps \ (OK)
```

```
S 
ightarrow NP \ VP \ PUNC \ (non-binary)
S 
ightarrow S \ and \ S \ (mixed)
NP 
ightarrow DT \ NP \ (OK)
NP 
ightarrow NN \ (unit production)
NN 
ightarrow dog \ (OK)
NN 
ightarrow cat \ (OK)
VP 
ightarrow VBZ \ NP \ (OK)
VP 
ightarrow VBZ \ ounit production)
VBZ 
ightarrow sleeps \ (OK)
VBZ 
ightarrow eats
```

```
S \rightarrow NP \ VP \ PUNC \ (non-binary)

S \rightarrow S \ and \ S \ (mixed)

NP \rightarrow DT \ NP \ (OK)

NP \rightarrow NN \ (unit production)

NN \rightarrow dog \ (OK)

NN \rightarrow cat \ (OK)

VP \rightarrow VBZ \ NP \ (OK)

VP \rightarrow VBZ \ (unit production)

VBZ \rightarrow sleeps \ (OK)

VBZ \rightarrow eats \ (OK)
```

```
S 
ightarrow NP \ VP \ PUNC \ (non-binary)
S 
ightarrow S \ and \ S \ (mixed)
NP 
ightarrow DT \ NP \ (OK)
NP 
ightarrow NN \ (unit production)
NN 
ightarrow dog \ (OK)
NN 
ightarrow cat \ (OK)
VP 
ightarrow VBZ \ NP \ (OK)
VP 
ightarrow VBZ \ (unit production)
VBZ 
ightarrow sleeps \ (OK)
VBZ 
ightarrow eats
DT 
ightarrow the
```

```
S 
ightarrow NP \ VP \ PUNC \ (non-binary)
S 
ightarrow S \ and \ S \ (mixed)
NP 
ightarrow DT \ NP \ (OK)
NP 
ightarrow NN \ (unit production)
NN 
ightarrow dog \ (OK)
NN 
ightarrow cat \ (OK)
VP 
ightarrow VBZ \ NP \ (OK)
VP 
ightarrow VBZ \ (unit production)
VBZ 
ightarrow sleeps \ (OK)
VBZ 
ightarrow eats \ (OK)
DT 
ightarrow the \ (OK)
```

Non-CNF grammar | CNF grammar | Action |

 $\begin{array}{c|c} \text{Non-CNF grammar} & \text{CNF grammar} & \text{Action} \\ \hline NP \rightarrow \textit{NN} & & & & & \\ \end{array}$

Non-CNF grammar	CNF grammar	Action
$NP \rightarrow NN$ $NN \rightarrow dog$		

Non-CNF grammar	CNF grammar	Action
$NP \rightarrow NN$		
NN o dog		
NN o cat		

Non-CNF grammar	CNF grammar	Action
$NP \rightarrow NN$ $NN \rightarrow dog$		
$NN \rightarrow dog$ $NN \rightarrow cat$		
	$NP \rightarrow dog$	(collapse rule)

Non-CNF grammar	CNF grammar	Action
$NP \rightarrow NN$ $NN \rightarrow dog$ $NN \rightarrow cat$		
	$egin{aligned} extstyle extstyle NP & ightarrow extstyle cat \end{aligned}$	(collapse rule) (collapse rule)

Non-CNF grammar	CNF grammar	Action
$NP \rightarrow NN$		
NN o dog		
NN o cat		
	$egin{aligned} extstyle extstyle NP & ightarrow extstyle cat \end{aligned}$	(collapse rule)
	NP ightarrow cat	(collapse rule)
VP o VBZ		

Non-CNF grammar	CNF grammar	Action
A/D A/A/		
$egin{aligned} NP & ightarrow NN \ NN & ightarrow dog \end{aligned}$		
$NN \rightarrow cat$		
	$egin{aligned} extstyle extstyle NP & ightarrow extstyle dog \ extstyle NP & ightarrow extstyle cat \end{aligned}$	(collapse rule)
	NP ightarrow cat	(collapse rule)
$VP \rightarrow VBZ$		
VBZ ightarrow sleeps		

Non-CNF grammar	CNF grammar	Action
NP o NN $NN o dog$ $NN o cat$		
VP ightarrow VBZ $VBZ ightarrow sleeps$ $VBZ ightarrow eats$	NP o dog NP o cat	(collapse rule) (collapse rule)

Non-CNF grammar	CNF grammar	Action
$NP \rightarrow NN$ $NN \rightarrow dog$		
NN o cat $VP o VBZ$	$egin{aligned} extstyle NP & ightarrow extstyle dog \ extstyle NP & ightarrow extstyle ex$	(collapse rule) (collapse rule)
VBZ ightarrow sleeps VBZ ightarrow eats		
	$VP ightarrow sleeps \ VP ightarrow eats$	(collapse rule) (collapse rule)

Non-CNF grammar | CNF grammar | Action |

Non-CNF grammar	CNF grammar	Action
$S \rightarrow S$ and S		
	$S \rightarrow S X1$	(new symbol)

Non-CNF grammar	CNF grammar	Action
$S \rightarrow S$ and S	$ \begin{array}{c} S \to S X1 \\ X1 \to X2 S \end{array} $	(new symbol)

Non-CNF grammar	CNF grammar	Action
$S \rightarrow S$ and S		
	$\begin{array}{c} S \rightarrow S X1 \\ X1 \rightarrow X2 S \\ X2 \rightarrow and \end{array}$	(new symbol) (new symbol)
	X2 → and	()

Non-CNF grammar CNF grammar Action

Action

Non-CNF grammar	CNF grammar	Action
$S \rightarrow NP \ VP \ PUNC$		
	$S \rightarrow NP X3$	(new symbol)

Non-CNF grammar	CNF grammar	Action
$S \rightarrow NP \ VP \ PUNC$	$S \rightarrow NP X3$ $X3 \rightarrow VP PUNC$	(new symbol)

Non-CNF grammar	CNF grammar	Action
$S \rightarrow NP \ VP \ PUNC$	$S \rightarrow NP X3$	(new symbol)
$NP o DT \ NP$	$\begin{array}{c} S \rightarrow NP X3 \\ X3 \rightarrow VP PUNC \end{array}$	

Non-CNF grammar	CNF grammar	Action
$S \rightarrow NP \ VP \ PUNC$		
	$S \rightarrow NP X3$ $X3 \rightarrow VP PUNC$ $NP \rightarrow DT NP$	(new symbol)
$NP \rightarrow DT \ NP$	$NP \rightarrow DT NP$	(carry over)

Non-CNF grammar	CNF grammar	Action
$S \rightarrow NP \ VP \ PUNC$		
	$S \rightarrow NP X3$ $X3 \rightarrow VP PUNC$ $NP \rightarrow DT NP$	(new symbol)
$egin{aligned} NP & ightarrow DT & NP \ VP & ightarrow VBZ & NP \end{aligned}$	$NP \rightarrow DT NP$	(carry over)

Non-CNF grammar	CNF grammar	Action
$S \rightarrow NP \ VP \ PUNC$		
	$S \rightarrow NP X3$	(new symbol)
	$X3 \rightarrow VP PUNC$	
$NP \rightarrow DT NP$	$NP \rightarrow DT NP$	(carry over)
$VP \rightarrow VBZ NP$	$VP \rightarrow VBZ NP$	(carry over)

Non-CNF grammar	CNF grammar	Action
$S \rightarrow NP \ VP \ PUNC$		
	$S \rightarrow NP X3$ $X3 \rightarrow VP PUNC$	(new symbol)
$NP \rightarrow DT NP$ $VP \rightarrow VBZ NP$	$NP \rightarrow DT NP$ $VP \rightarrow VBZ NP$	(carry over) (carry over)
DT ightarrow the		

Non-CNF grammar	CNF grammar	Action
$S \rightarrow NP \ VP \ PUNC$		
	$S \rightarrow NP X3$ $X3 \rightarrow VP PUNC$	(new symbol)
$NP \rightarrow DT \ NP$ $VP \rightarrow VBZ \ NP$ $DT \rightarrow the$	$egin{aligned} NP & ightarrow DT & NP \ VP & ightarrow VBZ & NP \ DT & ightarrow the \end{aligned}$	(carry over) (carry over) (carry over)

CFG in CNF

Homework 2 discussion

Homework: CKY and toCNF

Symbol naming conventions

Refer to NLTK treetransforms module

- Create new symbols from old (binarization):
 - $S \rightarrow NP \ VP \ PUNC$ becomes:
 - $S \rightarrow NP \quad S|\langle VP\text{-PUNC} \rangle, \, S|\langle VP\text{-PUNC} \rangle \rightarrow VP \quad PUNC$
- Create new symbols from old (unary collapsing):
 - $SBAR \rightarrow S$, $S \rightarrow NP$ VP becomes
 - $SBAR+S \rightarrow NP VP$