

From NL to FOL

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February 17, 2010

Today's lecture

- 1 Review
- 2 From NL to Logic
- 3 Semantics and the NLTK

From NL to FOL

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Review

From NL to Logic

Semantics and the
NLTK

What is/are:

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What is/are:

- the **three main problems** associated with computational semantics?

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- a **logical sentence**?
- the **logical connectives** of sentential logical?
- a logical **argument**?
- a **tautology**?

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What is meaning, really?

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An example:

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An example:

- 1 English: *Horatio bakes me a cake* **or** *Horatio bakes you a cake.*

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Intuitive approach to meaning

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- Intuitively we say that (1)'s meaning depends on whether Horatio bakes a cake, and whether it's for you or me.

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Intuitive approach to meaning

- Intuitively we say that (1)'s meaning depends on whether Horatio bakes a cake, and whether it's for you or me.
- That is, depending on the state of the world.
- Not very satisfying!

Slightly more formal account

What about assigning a value to meaning?

Something like the meaning of *Horatio bakes me a cake.* is:

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Slightly more formal account

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What about assigning a value to meaning?

Something like the meaning of *Horatio bakes me a cake.* is:

- **True**

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What about assigning a value to meaning?

Something like the meaning of *Horatio bakes me a cake.* is:

- **True**
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Slightly more formal account

What about assigning a value to meaning?

Something like the meaning of *Horatio bakes me a cake.* is:

- **True**
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Truth values

In fact, we can say that the atomic sentences of our logic P , Q , ..., X can either be **True** or **False** depending on the state of the world. This is called a **truth functional logic**.

Slightly more formal account

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Complex sentences

What about $P \vee Q$? When is it **True** or **False**?

Truth table for 'inclusive or', \vee

P	Q	$P \vee Q$
T	T	T
T	F	T
F	T	T
F	F	F

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Truth table for 'exclusive or', \oplus

P	Q	$P \oplus Q$
T	T	F
T	F	T
F	T	T
F	F	F

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Methodology

Semantic analysis is the mapping of NL utterances onto some logic. In traditional logic classes, the mapping is usually done from logic to NL:

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Example

$\exists x (dog(x) \wedge disappear(x))$

At least one entity is a dog and disappeared.

Some dog disappeared.

A dog disappeared.

Semantic analysis is the mapping of NL utterances onto some logic. In traditional logic classes, the mapping is usually done from logic to NL:

Example

$\exists x (dog(x) \wedge disappear(x))$

At least one entity is a dog and disappeared.

Some dog disappeared.

A dog disappeared.

Our methodology: start with structures in NL and find appropriate logical formulas. This makes the logic work for NL, not the other way around.

Mapping NL to FOL: Nouns

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What do **nouns** usually denote?

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Mapping NL to FOL: Nouns

What do **nouns** usually denote?

- **physical objects**, ones that exist in time and space
 - **abstract objects**, ones that may persist in time, but not space
-
- fish, dogs, hat, leg
 - value, politics, mathematics, scorn

Mapping NL to FOL: Nouns

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What do **nouns** usually denote?

- **physical objects**, ones that exist in time and space
- **abstract objects**, ones that may persist in time, but not space
- **events**, ones that exist in time and space, but not as long as objects

- fish, dogs, hat, leg
- value, politics, mathematics, scorn
- destruction, creation, movement

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Mapping NL to FOL: Nouns

Unary predicates, those with a single argument, are often used to represent the semantics of nouns.

fish(FLIPPER), *dog(FRITZ)*, *hat(HAT234)*
value(V1), *politics(P1)*, *scorn(S1)*
destroyingEvent(D1), *movementEvent(M1)*

In fact the unary predicate is naming the **type** of whatever the argument may be. There can be many, many types wrt the semantics of natural language.

NL semantics and ontology

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Definition

Our FOL approach requires a rich **ontology**, or a theory of existence and how the elements of the world relate.

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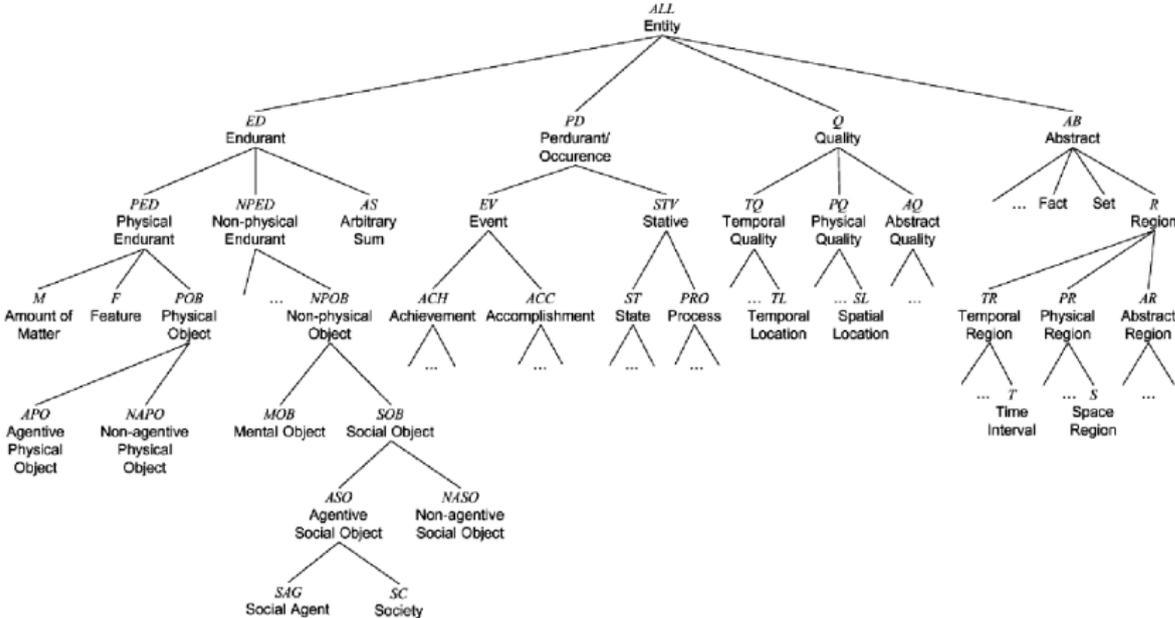
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Definition

Our FOL approach requires a rich **ontology**, or a theory of existence and how the elements of the world relate.

Modeling NL meaning is an exercise in ‘natural language’ metaphysics.

DOLCE upper categories



Mapping NL to FOL: PNs

Constants are used to represent the semantics of proper nouns.

- Queen Elizabeth II, *ELIZII*
- Barack Obama, *BARACK*
- John, *JOHN432*

Mapping NL to FOL: NPs

A modified NP is an NP of the form: $NP \rightarrow X NN$, where X can be one of a number of syntactic categories: determiner, quantity, adjective, etc.

- a dog, some dog
- all cats
- 3 fish
- several elephants
- a bunch of rats

Mapping NL to FOL: Quantificational modifiers

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Quantificational modifiers of the type **a** or **some** are modeled using the existential quantifier, \exists .

- a dog, $\exists x \text{ dog}(x)$
- some person, $\exists x \text{ person}(x)$

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And the quantificational modifier of the type **all**, **every**, etc. can be modeled using the universal \forall :

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- all fish, $\forall f \text{ fish}(f)$

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- every man, $\forall m \text{ man}(m)$

Mapping NL to FOL: Quantificational modifiers

And the quantificational modifier of the type **all**, **every**, etc. can be modeled using the universal \forall :

- all fish, $\forall f \text{ fish}(f)$
- every man, $\forall m \text{ man}(m)$
- each and every member, $\forall m \text{ member}(m)$

Mapping NL to FOL: Quantificational modifiers

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In reality quantification in languages is often difficult to describe given the standard logical machinery of FOL: \exists and \forall .

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Semanticists are often forced to come up with new logical quantifiers to discuss natural language quantification.

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- Just **a few** biscuits please, with **a lot** of gravy!
- He'll take **several** doses to be cured.

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- A **couple** of slices.
- Simply **scads** of weapons of mass destruction.

Mapping NL to FOL: Adjectives

Just as with nouns, adjectives say something about the type of entity being referred to; accordingly, they can be modeled as unary predicates at the semantic level.

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- red rooster, $red(y) \wedge rooster(y)$
- jagged white pill, $jagged(z) \wedge white(z) \wedge pill(z)$

Mapping NL to FOL: Adjectives

Just as with nouns, adjectives say something about the type of entity being referred to; accordingly, they can be modeled as unary predicates at the semantic level.

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- red rooster, $red(y) \wedge rooster(y)$
- jagged white pill, $jagged(z) \wedge white(z) \wedge pill(z)$

Some adjectives are more problematic and require more elaborate semantic machinery: *small solar system*, *large mouse*, *grande latte*

Mapping NL to FOL: Conjunctions

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Conjunctions such as **and**, **as well as**, **or**, **either...or...** are mapped to logical connectives.

Mapping NL to FOL: Conjunctions

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- ham as well as eggs, $ham(h) \wedge egg(e)$
- coffee or tea, $coffee(c) \vee tea(t)$
- either red or green, $red(x) \oplus green(x)$ (XOR)

Mapping NL to FOL: misc

Negative markers are mapped to formulas with the negation symbol.

not pumpkin, $\neg \text{pumpkin}(p)$

Mapping NL to FOL: misc

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Some prepositions are mapped to binary predicates.

Joe is in Seattle, $\text{in}(\text{JOE}, \text{SEATTLE})$

Mapping NL to FOL: misc

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Copulas (certain occurrences of *be*) are mapped to equality.

Fred is the killer, $\text{FRED} = \text{KILLER123}$

Mapping NL to FOL: Verbs

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give(x, y, z)

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But there's a problem.

Mapping NL to FOL: VPs

- John buttered the toast.
Butter(*JOHN*, *TOAST*)

Mapping NL to FOL: VPs

- John buttered the toast.
Butter(*JOHN*, *TOAST*)
- John buttered the toast at midnight.
Butter(*JOHN*, *TOAST*, *MIDNIGHT*)

Mapping NL to FOL: VPs

- John buttered the toast.
Butter(*JOHN*, *TOAST*)
- John buttered the toast at midnight.
Butter(*JOHN*, *TOAST*, *MIDNIGHT*)
- John buttered the toast at midnight with a knife.
Butter(*JOHN*, *TOAST*, *MIDNIGHT*, *KNIFE*)

Mapping NL to FOL: VPs

- John buttered the toast.
Butter(*JOHN*, *TOAST*)
- John buttered the toast at midnight.
Butter(*JOHN*, *TOAST*, *MIDNIGHT*)
- John buttered the toast at midnight with a knife.
Butter(*JOHN*, *TOAST*, *MIDNIGHT*, *KNIFE*)
- John buttered the toast at midnight with a knife before he went to bed.
Butter(*JOHN*, *TOAST*, *MIDNIGHT*, *KNIFE*, ...)

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Review

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- `nltk.sem.logic`: A version of first order logic, built on top of the untyped lambda calculus.
- `nltk.sem.logic.Expression` is the base class for all kinds of logical formulas.
- `nltk.sem.LogicParser`: A parser that reads semantic representations and creates logic objects.
- `nltk.sem.util`: Utility functions for batch-processing sentences: parsing and extraction of the semantic representation of the root node of the the syntax tree, followed by evaluation of the semantic representation in a first-order model.
- `Prover9`: a supplemental theorem prover callable from the NLTK

The `nltk.sem.logic` package contains the tools necessary for representing FOL.

Boolean operators:

negation	-	(the hyphen)
conjunction	&	
disjunction		
implication	->	
equivalence	<->	

Equality predicates:

equality	=
inequality	!=

Quantifiers:

existential	exists
universal	all
lambda	\

Review

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