

# CKY example

a 1	pilot 2	likes 3	flying 4	planes 5

$S \rightarrow NP VP$   
 $VP \rightarrow VBG NNS$   
 $VP \rightarrow VBZ VP$   
 $VP \rightarrow VBZ NP$   
 $NP \rightarrow DT NN$   
 $NP \rightarrow JJ NNS$   
 $DT \rightarrow a$   
 $NN \rightarrow pilot$   
 $VBZ \rightarrow likes$   
 $VBG \rightarrow flying$   
 $JJ \rightarrow flying$   
 $NNS \rightarrow planes$

# CKY example

a 1	pilot 2	likes 3	flying 4	planes 5
DT				

$S \rightarrow NP VP$   
 $VP \rightarrow VBG NNS$   
 $VP \rightarrow VBZ VP$   
 $VP \rightarrow VBZ NP$   
 $NP \rightarrow DT NN$   
 $NP \rightarrow JJ NNS$   
#  $DT \rightarrow a$   
 $NN \rightarrow pilot$   
 $VBZ \rightarrow likes$   
 $VBG \rightarrow flying$   
 $JJ \rightarrow flying$   
 $NNS \rightarrow planes$

# CKY example

a 1	<b>pilot</b> 2	likes 3	flying 4	planes 5
DT				
	NN			

$S \rightarrow NP VP$   
 $VP \rightarrow VBG NNS$   
 $VP \rightarrow VBZ VP$   
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# CKY example

a 1	<b>pilot</b> 2	likes 3	flying 4	planes 5
DT	NP			
	NN			

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$S \rightarrow NP VP$   
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	NN			
		VBZ		

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# CKY example

a 1	pilot 2	likes 3	flying 4	planes 5
DT	NP			
	NN	-		
		VBZ		

$S \rightarrow NP VP$   
 $VP \rightarrow VBG NNS$   
 $VP \rightarrow VBZ VP$   
 $VP \rightarrow VBZ NP$   
 $NP \rightarrow DT NN$   
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 $VBG \rightarrow flying$   
 $JJ \rightarrow flying$   
 $NNS \rightarrow planes$

# CKY example

a 1	pilot 2	likes 3	flying 4	planes 5
DT	NP	-		
	NN	-		
		VBZ		

*S* → *NP VP*  
*VP* → *VBG NNS*  
*VP* → *VBZ VP*  
*VP* → *VBZ NP*  
*NP* → *DT NN*  
*NP* → *JJ NNS*  
*DT* → *a*  
*NN* → *pilot*  
*VBZ* → *likes*  
*VBG* → *flying*  
*JJ* → *flying*  
*NNS* → *planes*

# CKY example

a 1	pilot 2	likes 3	flying 4	planes 5
DT	NP	-		
	NN	-		
		VBZ		
			JJ	

$S \rightarrow NP VP$   
 $VP \rightarrow VBG NNS$   
 $VP \rightarrow VBZ VP$   
 $VP \rightarrow VBZ NP$   
 $NP \rightarrow DT NN$   
 $NP \rightarrow JJ NNS$   
 $DT \rightarrow a$   
 $NN \rightarrow pilot$   
 $VBZ \rightarrow likes$   
 $VBG \rightarrow flying$   
 $JJ \rightarrow flying$   
 $NNS \rightarrow planes$

#

# CKY example

a 1	pilot 2	likes 3	flying 4	planes 5
DT	NP	-		
	NN	-		
		VBZ		
			JJ VBG	

$S \rightarrow NP VP$   
 $VP \rightarrow VBG NNS$   
 $VP \rightarrow VBZ VP$   
 $VP \rightarrow VBZ NP$   
 $NP \rightarrow DT NN$   
 $NP \rightarrow JJ NNS$   
 $DT \rightarrow a$   
 $NN \rightarrow pilot$   
 $VBZ \rightarrow likes$   
 $VBG \rightarrow flying$   
 $JJ \rightarrow flying$   
 $NNS \rightarrow planes$

#

# CKY example

a 1	pilot 2	likes 3	flying 4	planes 5
DT	NP	-		
	NN	-		
		VBZ	-	
			JJ VBG	

*S* → *NP VP*  
*VP* → *VBG NNS*  
*VP* → *VBZ VP*  
*VP* → *VBZ NP*  
*NP* → *DT NN*  
*NP* → *JJ NNS*  
*DT* → *a*  
*NN* → *pilot*  
*VBZ* → *likes*  
*VBG* → *flying*  
*JJ* → *flying*  
*NNS* → *planes*

# CKY example

a 1	pilot 2	likes 3	flying 4	planes 5
DT	NP	-		
	NN	-	-	
		VBZ	-	
			JJ VBG	

$S \rightarrow NP VP$   
 $VP \rightarrow VBG NNS$   
 $VP \rightarrow VBZ VP$   
 $VP \rightarrow VBZ NP$   
 $NP \rightarrow DT NN$   
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 $DT \rightarrow a$   
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# CKY example

a 1	pilot 2	likes 3	flying 4	planes 5
DT	NP	-	-	
	NN	-	-	
		VBZ	-	
			JJ VBG	

$S \rightarrow NP VP$   
 $VP \rightarrow VBG NNS$   
 $VP \rightarrow VBZ VP$   
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# CKY example

a 1	pilot 2	likes 3	flying 4	planes 5
DT	NP	-	-	
	NN	-	-	
		VBZ	-	
			JJ VBG	
				NNS

$S \rightarrow NP VP$   
 $VP \rightarrow VBG NNS$   
 $VP \rightarrow VBZ VP$   
 $VP \rightarrow VBZ NP$   
 $NP \rightarrow DT NN$   
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# CKY example

a 1	pilot 2	likes 3	flying 4	planes 5
DT	NP	-	-	
	NN	-	-	
		VBZ	-	
			JJ VBG	NP
				NNS

#

- $S \rightarrow NP VP$
- $VP \rightarrow VBG NNS$
- $VP \rightarrow VBZ VP$
- $VP \rightarrow VBZ NP$
- $NP \rightarrow DT NN$
- $NP \rightarrow JJ NNS$
- $DT \rightarrow a$
- $NN \rightarrow pilot$
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# CKY example

a 1	pilot 2	likes 3	flying 4	planes 5
DT	NP	-	-	
	NN	-	-	
		VBZ	-	
			JJ VBG	NP VP
				NNS

#

$S \rightarrow NP VP$   
 $VP \rightarrow VBG NNS$   
 $VP \rightarrow VBZ VP$   
 $VP \rightarrow VBZ NP$   
 $NP \rightarrow DT NN$   
 $NP \rightarrow JJ NNS$   
 $DT \rightarrow a$   
 $NN \rightarrow pilot$   
 $VBZ \rightarrow likes$   
 $VBG \rightarrow flying$   
 $JJ \rightarrow flying$   
 $NNS \rightarrow planes$

# CKY example

a 1	pilot 2	likes 3	flying 4	planes 5
DT	NP	-	-	
	NN	-	-	
		VBZ	-	VP
			JJ VBG	NP VP
				NNS

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$S \rightarrow NP VP$   
 $VP \rightarrow VBG NNS$   
 $VP \rightarrow VBZ VP$   
 $VP \rightarrow VBZ NP$   
 $NP \rightarrow DT NN$   
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 $NN \rightarrow pilot$   
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 $VBG \rightarrow flying$   
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 $NNS \rightarrow planes$

# CKY example

a 1	pilot 2	likes 3	flying 4	planes 5
DT	NP	-	-	
	NN	-	-	
		VBZ	-	VP VP
			JJ VBG	NP VP
				NNS

#

$S \rightarrow NP VP$   
 $VP \rightarrow VBG NNS$   
 $VP \rightarrow VBZ VP$   
 $VP \rightarrow VBZ NP$   
 $NP \rightarrow DT NN$   
 $NP \rightarrow JJ NNS$   
 $DT \rightarrow a$   
 $NN \rightarrow pilot$   
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# CKY example

a 1	pilot 2	likes 3	flying 4	planes 5
DT	NP	-	-	
	NN	-	-	-
		VBZ	-	VP VP
			JJ VBG	NP VP
				NNS

$S \rightarrow NP VP$   
 $VP \rightarrow VBG NNS$   
 $VP \rightarrow VBZ VP$   
 $VP \rightarrow VBZ NP$   
 $NP \rightarrow DT NN$   
 $NP \rightarrow JJ NNS$   
 $DT \rightarrow a$   
 $NN \rightarrow pilot$   
 $VBZ \rightarrow likes$   
 $VBG \rightarrow flying$   
 $JJ \rightarrow flying$   
 $NNS \rightarrow planes$

# CKY example

a 1	pilot 2	likes 3	flying 4	planes 5
DT	NP	-	-	S
	NN	-	-	-
		VBZ	-	VP VP
			JJ VBG	NP VP
				NNS

#

- $S \rightarrow NP VP$
- $VP \rightarrow VBG NNS$
- $VP \rightarrow VBZ VP$
- $VP \rightarrow VBZ NP$
- $NP \rightarrow DT NN$
- $NP \rightarrow JJ NNS$
- $DT \rightarrow a$
- $NN \rightarrow pilot$
- $VBZ \rightarrow likes$
- $VBG \rightarrow flying$
- $JJ \rightarrow flying$
- $NNS \rightarrow planes$

# CKY example

a 1	pilot 2	likes 3	flying 4	planes 5
DT	NP	-	-	S S
	NN	-	-	-
		VBZ	-	VP VP
			JJ VBG	NP VP
				NNS

$S \rightarrow NP VP$   
 $VP \rightarrow VBG NNS$   
 $VP \rightarrow VBZ VP$   
 $VP \rightarrow VBZ NP$   
 $NP \rightarrow DT NN$   
 $NP \rightarrow JJ NNS$   
 $DT \rightarrow a$   
 $NN \rightarrow pilot$   
 $VBZ \rightarrow likes$   
 $VBG \rightarrow flying$   
 $JJ \rightarrow flying$   
 $NNS \rightarrow planes$

# Probabilistic CKY: all parses

a 1	pilot 2	likes 3	flying 4	planes 5

$S \rightarrow NP VP$  [1.0]  
 $VP \rightarrow VBG NNS$  [0.1]  
 $VP \rightarrow VBZ VP$  [0.1]  
 $VP \rightarrow VBZ NP$  [0.3]  
 $NP \rightarrow DT NN$  [0.3]  
 $NP \rightarrow JJ NNS$  [0.4]  
 $DT \rightarrow a$  [0.3]  
 $NN \rightarrow pilot$  [0.1]  
 $VBZ \rightarrow likes$  [0.4]  
 $VBG \rightarrow flying$  [0.5]  
 $JJ \rightarrow flying$  [0.1]  
 $NNS \rightarrow planes$  [.34]

# Probabilistic CKY: all parses

a 1	pilot 2	likes 3	flying 4	planes 5
DT [0.3]				

#

- $S \rightarrow NP VP$  [1.0]
- $VP \rightarrow VBG NNS$  [0.1]
- $VP \rightarrow VBZ VP$  [0.1]
- $VP \rightarrow VBZ NP$  [0.3]
- $NP \rightarrow DT NN$  [0.3]
- $NP \rightarrow JJ NNS$  [0.4]
- $DT \rightarrow a$  [0.3]
- $NN \rightarrow pilot$  [0.1]
- $VBZ \rightarrow likes$  [0.4]
- $VBG \rightarrow flying$  [0.5]
- $JJ \rightarrow flying$  [0.1]
- $NNS \rightarrow planes$  [.34]

# Probabilistic CKY: all parses

a 1	<b>pilot</b> 2	likes 3	flying 4	planes 5
DT [0.3]				
	NN [0.1]			

#

$S \rightarrow NP VP$  [1.0]  
 $VP \rightarrow VBG NNS$  [0.1]  
 $VP \rightarrow VBZ VP$  [0.1]  
 $VP \rightarrow VBZ NP$  [0.3]  
 $NP \rightarrow DT NN$  [0.3]  
 $NP \rightarrow JJ NNS$  [0.4]  
 $DT \rightarrow a$  [0.3]  
 $NN \rightarrow pilot$  [0.1]  
 $VBZ \rightarrow likes$  [0.4]  
 $VBG \rightarrow flying$  [0.5]  
 $JJ \rightarrow flying$  [0.1]  
 $NNS \rightarrow planes$  [.34]

# Probabilistic CKY: all parses

a 1	<b>pilot</b> 2	likes 3	flying 4	planes 5
DT [0.3]	NP [.009]			
	NN [0.1]			

#

$S \rightarrow NP VP$  [1.0]  
 $VP \rightarrow VBG NNS$  [0.1]  
 $VP \rightarrow VBZ VP$  [0.1]  
 $VP \rightarrow VBZ NP$  [0.3]  
 $NP \rightarrow DT NN$  [0.3]  
 $NP \rightarrow JJ NNS$  [0.4]  
 $DT \rightarrow a$  [0.3]  
 $NN \rightarrow pilot$  [0.1]  
 $VBZ \rightarrow likes$  [0.4]  
 $VBG \rightarrow flying$  [0.5]  
 $JJ \rightarrow flying$  [0.1]  
 $NNS \rightarrow planes$  [.34]

$$0.3 \times 0.1 \times 0.3 = 0.009$$

# Probabilistic CKY: all parses

a 1	pilot 2	likes 3	flying 4	planes 5
DT [0.3]	NP [.009]			
	NN [0.1]			
		VBZ [0.4]		

#

$S \rightarrow NP VP$  [1.0]  
 $VP \rightarrow VBG NNS$  [0.1]  
 $VP \rightarrow VBZ VP$  [0.1]  
 $VP \rightarrow VBZ NP$  [0.3]  
 $NP \rightarrow DT NN$  [0.3]  
 $NP \rightarrow JJ NNS$  [0.4]  
 $DT \rightarrow a$  [0.3]  
 $NN \rightarrow pilot$  [0.1]  
 $VBZ \rightarrow likes$  [0.4]  
 $VBG \rightarrow flying$  [0.5]  
 $JJ \rightarrow flying$  [0.1]  
 $NNS \rightarrow planes$  [.34]

# Probabilistic CKY: all parses

a 1	pilot 2	likes 3	flying 4	planes 5
DT [0.3]	NP [.009]			
	NN [0.1]	-		
		VBZ [0.4]		

$S \rightarrow NP VP$  [1.0]  
 $VP \rightarrow VBG NNS$  [0.1]  
 $VP \rightarrow VBZ VP$  [0.1]  
 $VP \rightarrow VBZ NP$  [0.3]  
 $NP \rightarrow DT NN$  [0.3]  
 $NP \rightarrow JJ NNS$  [0.4]  
 $DT \rightarrow a$  [0.3]  
 $NN \rightarrow pilot$  [0.1]  
 $VBZ \rightarrow likes$  [0.4]  
 $VBG \rightarrow flying$  [0.5]  
 $JJ \rightarrow flying$  [0.1]  
 $NNS \rightarrow planes$  [.34]

# Probabilistic CKY: all parses

a 1	pilot 2	likes 3	flying 4	planes 5
DT [0.3]	NP [.009]	-		
	NN [0.1]	-		
		VBZ [0.4]		

$S \rightarrow NP VP$  [1.0]  
 $VP \rightarrow VBG NNS$  [0.1]  
 $VP \rightarrow VBZ VP$  [0.1]  
 $VP \rightarrow VBZ NP$  [0.3]  
 $NP \rightarrow DT NN$  [0.3]  
 $NP \rightarrow JJ NNS$  [0.4]  
 $DT \rightarrow a$  [0.3]  
 $NN \rightarrow pilot$  [0.1]  
 $VBZ \rightarrow likes$  [0.4]  
 $VBG \rightarrow flying$  [0.5]  
 $JJ \rightarrow flying$  [0.1]  
 $NNS \rightarrow planes$  [.34]

# Probabilistic CKY: all parses

a 1	pilot 2	likes 3	flying 4	planes 5
DT [0.3]	NP [.009]	-		
	NN [0.1]	-		
		VBZ [0.4]		
			JJ [0.1]	

#

- $S \rightarrow NP VP$  [1.0]
- $VP \rightarrow VBG NNS$  [0.1]
- $VP \rightarrow VBZ VP$  [0.1]
- $VP \rightarrow VBZ NP$  [0.3]
- $NP \rightarrow DT NN$  [0.3]
- $NP \rightarrow JJ NNS$  [0.4]
- $DT \rightarrow a$  [0.3]
- $NN \rightarrow pilot$  [0.1]
- $VBZ \rightarrow likes$  [0.4]
- $VBG \rightarrow flying$  [0.5]
- $JJ \rightarrow flying$  [0.1]
- $NNS \rightarrow planes$  [.34]

# Probabilistic CKY: all parses

a 1	pilot 2	likes 3	flying 4	planes 5
DT [0.3]	NP [.009]	-		
	NN [0.1]	-		
		VBZ [0.4]		
			JJ [0.1] VBG [0.5]	

$S \rightarrow NP VP$  [1.0]  
 $VP \rightarrow VBG NNS$  [0.1]  
 $VP \rightarrow VBZ VP$  [0.1]  
 $VP \rightarrow VBZ NP$  [0.3]  
 $NP \rightarrow DT NN$  [0.3]  
 $NP \rightarrow JJ NNS$  [0.4]  
 $DT \rightarrow a$  [0.3]  
 $NN \rightarrow pilot$  [0.1]  
 $VBZ \rightarrow likes$  [0.4]  
 $VBG \rightarrow flying$  [0.5]  
 $JJ \rightarrow flying$  [0.1]  
 $NNS \rightarrow planes$  [.34]

#

# Probabilistic CKY: all parses

a 1	pilot 2	likes 3	flying 4	planes 5
DT [0.3]	NP [.009]	-		
	NN [0.1]	-		
		VBZ [0.4]	-	
			JJ [0.1] VBG [0.5]	

*S* → *NP VP* [1.0]  
*VP* → *VBG NNS* [0.1]  
*VP* → *VBZ VP* [0.1]  
*VP* → *VBZ NP* [0.3]  
*NP* → *DT NN* [0.3]  
*NP* → *JJ NNS* [0.4]  
*DT* → *a* [0.3]  
*NN* → *pilot* [0.1]  
*VBZ* → *likes* [0.4]  
*VBG* → *flying* [0.5]  
*JJ* → *flying* [0.1]  
*NNS* → *planes* [.34]

# Probabilistic CKY: all parses

a 1	pilot 2	likes 3	flying 4	planes 5
DT [0.3]	NP [.009]	-		
	NN [0.1]	-	-	
		VBZ [0.4]	-	
			JJ [0.1] VBG [0.5]	

*S* → *NP VP* [1.0]  
*VP* → *VBG NNS* [0.1]  
*VP* → *VBZ VP* [0.1]  
*VP* → *VBZ NP* [0.3]  
*NP* → *DT NN* [0.3]  
*NP* → *JJ NNS* [0.4]  
*DT* → *a* [0.3]  
*NN* → *pilot* [0.1]  
*VBZ* → *likes* [0.4]  
*VBG* → *flying* [0.5]  
*JJ* → *flying* [0.1]  
*NNS* → *planes* [.34]

# Probabilistic CKY: all parses

a 1	pilot 2	likes 3	flying 4	planes 5
DT [0.3]	NP [.009]	-	-	
	NN [0.1]	-	-	
		VBZ [0.4]	-	
			JJ [0.1] VBG [0.5]	

*S* → *NP VP* [1.0]  
*VP* → *VBG NNS* [0.1]  
*VP* → *VBZ VP* [0.1]  
*VP* → *VBZ NP* [0.3]  
*NP* → *DT NN* [0.3]  
*NP* → *JJ NNS* [0.4]  
*DT* → *a* [0.3]  
*NN* → *pilot* [0.1]  
*VBZ* → *likes* [0.4]  
*VBG* → *flying* [0.5]  
*JJ* → *flying* [0.1]  
*NNS* → *planes* [.34]

# Probabilistic CKY: all parses

a 1	pilot 2	likes 3	flying 4	planes 5
DT [0.3]	NP [.009]	-	-	
	NN [0.1]	-	-	
		VBZ [0.4]	-	
			JJ [0.1] VBG [0.5]	
				NNS [.34]

*S* → *NP VP* [1.0]  
*VP* → *VBG NNS* [0.1]  
*VP* → *VBZ VP* [0.1]  
*VP* → *VBZ NP* [0.3]  
*NP* → *DT NN* [0.3]  
*NP* → *JJ NNS* [0.4]  
*DT* → *a* [0.3]  
*NN* → *pilot* [0.1]  
*VBZ* → *likes* [0.4]  
*VBG* → *flying* [0.5]  
*JJ* → *flying* [0.1]  
*NNS* → *planes* [.34]

#

# Probabilistic CKY: all parses

a 1	pilot 2	likes 3	flying 4	planes 5
DT [0.3]	NP [.009]	-	-	
	NN [0.1]	-	-	
		VBZ [0.4]	-	
			JJ [0.1] VBG [0.5]	NP [.0136]
				NNS [.34]

#

- $S \rightarrow NP VP$  [1.0]
- $VP \rightarrow VBG NNS$  [0.1]
- $VP \rightarrow VBZ VP$  [0.1]
- $VP \rightarrow VBZ NP$  [0.3]
- $NP \rightarrow DT NN$  [0.3]
- $NP \rightarrow JJ NNS$  [0.4]
- $DT \rightarrow a$  [0.3]
- $NN \rightarrow pilot$  [0.1]
- $VBZ \rightarrow likes$  [0.4]
- $VBG \rightarrow flying$  [0.5]
- $JJ \rightarrow flying$  [0.1]
- $NNS \rightarrow planes$  [.34]

$$0.1 \times 0.34 \times 0.4 = 0.0136$$

# Probabilistic CKY: all parses

a 1	pilot 2	likes 3	flying 4	planes 5
DT [0.3]	NP [.009]	-	-	
	NN [0.1]	-	-	
		VBZ [0.4]	-	
			JJ [0.1] VBG [0.5]	NP [.0136] VP [.017]
				NNS [.34]

#	$S \rightarrow NP VP$	[1.0]
	$VP \rightarrow VBG NNS$	[0.1]
	$VP \rightarrow VBZ VP$	[0.1]
	$VP \rightarrow VBZ NP$	[0.3]
	$NP \rightarrow DT NN$	[0.3]
	$NP \rightarrow JJ NNS$	[0.4]
	$DT \rightarrow a$	[0.3]
	$NN \rightarrow pilot$	[0.1]
	$VBZ \rightarrow likes$	[0.4]
	$VBG \rightarrow flying$	[0.5]
	$JJ \rightarrow flying$	[0.1]
	$NNS \rightarrow planes$	[.34]

$$0.5 \times 0.34 \times 0.1 = 0.017$$

# Probabilistic CKY: all parses

a 1	pilot 2	likes 3	flying 4	planes 5
DT [0.3]	NP [.009]	-	-	
	NN [0.1]	-	-	
		VBZ [0.4]	-	VP [.001632]
			JJ [0.1] VBG [0.5]	NP [.0136] VP [.017]
				NNS [.34]

<i>S</i> → <i>NP VP</i>	[1.0]
<i>VP</i> → <i>VBG NNS</i>	[0.1]
<i>VP</i> → <i>VBZ VP</i>	[0.1]
<i>VP</i> → <i>VBZ NP</i>	[0.3]
<i>NP</i> → <i>DT NN</i>	[0.3]
<i>NP</i> → <i>JJ NNS</i>	[0.4]
<i>DT</i> → <i>a</i>	[0.3]
<i>NN</i> → <i>pilot</i>	[0.1]
<i>VBZ</i> → <i>likes</i>	[0.4]
<i>VBG</i> → <i>flying</i>	[0.5]
<i>JJ</i> → <i>flying</i>	[0.1]
<i>NNS</i> → <i>planes</i>	[.34]

$$0.4 \times 0.0136 \times 0.3 = 0.001632$$

# Probabilistic CKY: all parses

a 1	pilot 2	likes 3	flying 4	planes 5
DT [0.3]	NP [.009]	-	-	
	NN [0.1]	-	-	
		VBZ [0.4]	-	VP [.001632] VP [.00068]
			JJ [0.1] VBG [0.5]	NP [.0136] VP [.017]
				NNS [.34]

#

- $S \rightarrow NP VP$  [1.0]
- $VP \rightarrow VBG NNS$  [0.1]
- $VP \rightarrow VBZ VP$  [0.1]
- $VP \rightarrow VBZ NP$  [0.3]
- $NP \rightarrow DT NN$  [0.3]
- $NP \rightarrow JJ NNS$  [0.4]
- $DT \rightarrow a$  [0.3]
- $NN \rightarrow pilot$  [0.1]
- $VBZ \rightarrow likes$  [0.4]
- $VBG \rightarrow flying$  [0.5]
- $JJ \rightarrow flying$  [0.1]
- $NNS \rightarrow planes$  [.34]

$$0.4 \times 0.017 \times 0.1 = 0.00068$$

# Probabilistic CKY: all parses

a 1	pilot 2	likes 3	flying 4	planes 5
DT [0.3]	NP [.009]	-	-	
	NN [0.1]	-	-	-
		VBZ [0.4]	-	VP [.001632] VP [.00068]
			JJ [0.1] VBG [0.5]	NP [.0136] VP [.017]
				NNS [.34]

*S* → *NP VP* [1.0]  
*VP* → *VBG NNS* [0.1]  
*VP* → *VBZ VP* [0.1]  
*VP* → *VBZ NP* [0.3]  
*NP* → *DT NN* [0.3]  
*NP* → *JJ NNS* [0.4]  
*DT* → *a* [0.3]  
*NN* → *pilot* [0.1]  
*VBZ* → *likes* [0.4]  
*VBG* → *flying* [0.5]  
*JJ* → *flying* [0.1]  
*NNS* → *planes* [.34]

# Probabilistic CKY: all parses

a 1	pilot 2	likes 3	flying 4	planes 5
DT [0.3]	NP [.009]	-	-	S [1.4688x10 <sup>-5</sup> ]
	NN [0.1]	-	-	-
		VBZ [0.4]	-	VP [.001632] VP [.00068]
			JJ [0.1] VBG [0.5]	NP [.0136] VP [.017]
				NNS [.34]

#	<i>S</i> → <i>NP VP</i>	[1.0]
	<i>VP</i> → <i>VBG NNS</i>	[0.1]
	<i>VP</i> → <i>VBZ VP</i>	[0.1]
	<i>VP</i> → <i>VBZ NP</i>	[0.3]
	<i>NP</i> → <i>DT NN</i>	[0.3]
	<i>NP</i> → <i>JJ NNS</i>	[0.4]
	<i>DT</i> → <i>a</i>	[0.3]
	<i>NN</i> → <i>pilot</i>	[0.1]
	<i>VBZ</i> → <i>likes</i>	[0.4]
	<i>VBG</i> → <i>flying</i>	[0.5]
	<i>JJ</i> → <i>flying</i>	[0.1]
	<i>NNS</i> → <i>planes</i>	[.34]

$$0.009 \times 0.001632 \times 1.0 = 1.4688 \times 10^{-5}$$

# Probabilistic CKY: all parses

a 1	pilot 2	likes 3	flying 4	planes 5
DT [0.3]	NP [.009]	-	-	S [ $1.4688 \times 10^{-5}$ ] S [ $6.12 \times 10^{-6}$ ]
	NN [0.1]	-	-	-
		VBZ [0.4]	-	VP [.001632] VP [.00068]
			JJ [0.1] VBG [0.5]	NP [.0136] VP [.017]
				NNS [.34]

*S* → *NP VP* [1.0]  
*VP* → *VBG NNS* [0.1]  
*VP* → *VBZ VP* [0.1]  
*VP* → *VBZ NP* [0.3]  
*NP* → *DT NN* [0.3]  
*NP* → *JJ NNS* [0.4]  
*DT* → *a* [0.3]  
*NN* → *pilot* [0.1]  
*VBZ* → *likes* [0.4]  
*VBG* → *flying* [0.5]  
*JJ* → *flying* [0.1]  
*NNS* → *planes* [.34]

$$0.009 \times 0.00068 \times 1.0 = 6.12 \times 10^{-6}$$

# Probabilistic CKY: best parse

a 1	pilot 2	likes 3	flying 4	planes 5

$S \rightarrow NP VP$  [1.0]  
 $VP \rightarrow VBG NNS$  [0.1]  
 $VP \rightarrow VBZ VP$  [0.1]  
 $VP \rightarrow VBZ NP$  [0.3]  
 $NP \rightarrow DT NN$  [0.3]  
 $NP \rightarrow JJ NNS$  [0.4]  
 $DT \rightarrow a$  [0.3]  
 $NN \rightarrow pilot$  [0.1]  
 $VBZ \rightarrow likes$  [0.4]  
 $VBG \rightarrow flying$  [0.5]  
 $JJ \rightarrow flying$  [0.1]  
 $NNS \rightarrow planes$  [.34]

# Probabilistic CKY: best parse

a 1	pilot 2	likes 3	flying 4	planes 5
DT [0.3]				

	$S \rightarrow NP VP$	[1.0]
	$VP \rightarrow VBG NNS$	[0.1]
	$VP \rightarrow VBZ VP$	[0.1]
	$VP \rightarrow VBZ NP$	[0.3]
	$NP \rightarrow DT NN$	[0.3]
	$NP \rightarrow JJ NNS$	[0.4]
#	$DT \rightarrow a$	[0.3]
	$NN \rightarrow pilot$	[0.1]
	$VBZ \rightarrow likes$	[0.4]
	$VBG \rightarrow flying$	[0.5]
	$JJ \rightarrow flying$	[0.1]
	$NNS \rightarrow planes$	[.34]

# Probabilistic CKY: best parse

a 1	<b>pilot</b> 2	likes 3	flying 4	planes 5
DT [0.3]				
	NN [0.1]			

#

- $S \rightarrow NP VP$  [1.0]
- $VP \rightarrow VBG NNS$  [0.1]
- $VP \rightarrow VBZ VP$  [0.1]
- $VP \rightarrow VBZ NP$  [0.3]
- $NP \rightarrow DT NN$  [0.3]
- $NP \rightarrow JJ NNS$  [0.4]
- $DT \rightarrow a$  [0.3]
- $NN \rightarrow pilot$  [0.1]
- $VBZ \rightarrow likes$  [0.4]
- $VBG \rightarrow flying$  [0.5]
- $JJ \rightarrow flying$  [0.1]
- $NNS \rightarrow planes$  [.34]

# Probabilistic CKY: best parse

a 1	<b>pilot</b> 2	likes 3	flying 4	planes 5
DT [0.3]	NP [.009]			
	NN [0.1]			

	$S \rightarrow NP VP$	[1.0]
	$VP \rightarrow VBG NNS$	[0.1]
	$VP \rightarrow VBZ VP$	[0.1]
	$VP \rightarrow VBZ NP$	[0.3]
#	$NP \rightarrow DT NN$	[0.3]
	$NP \rightarrow JJ NNS$	[0.4]
	$DT \rightarrow a$	[0.3]
	$NN \rightarrow pilot$	[0.1]
	$VBZ \rightarrow likes$	[0.4]
	$VBG \rightarrow flying$	[0.5]
	$JJ \rightarrow flying$	[0.1]
	$NNS \rightarrow planes$	[.34]
	$0.3 \times 0.1 \times 0.3 =$	
	0.009	

# Probabilistic CKY: best parse

a 1	pilot 2	likes 3	flying 4	planes 5
DT [0.3]	NP [.009]			
	NN [0.1]			
		VBZ [0.4]		

	$S \rightarrow NP VP$	[1.0]
	$VP \rightarrow VBG NNS$	[0.1]
	$VP \rightarrow VBZ VP$	[0.1]
	$VP \rightarrow VBZ NP$	[0.3]
	$NP \rightarrow DT NN$	[0.3]
	$NP \rightarrow JJ NNS$	[0.4]
	$DT \rightarrow a$	[0.3]
	$NN \rightarrow pilot$	[0.1]
#	$VBZ \rightarrow likes$	[0.4]
	$VBG \rightarrow flying$	[0.5]
	$JJ \rightarrow flying$	[0.1]
	$NNS \rightarrow planes$	[.34]

# Probabilistic CKY: best parse

a 1	pilot 2	likes 3	flying 4	planes 5
DT [0.3]	NP [.009]			
	NN [0.1]	-		
		VBZ [0.4]		

$S \rightarrow NP VP$  [1.0]  
 $VP \rightarrow VBG NNS$  [0.1]  
 $VP \rightarrow VBZ VP$  [0.1]  
 $VP \rightarrow VBZ NP$  [0.3]  
 $NP \rightarrow DT NN$  [0.3]  
 $NP \rightarrow JJ NNS$  [0.4]  
 $DT \rightarrow a$  [0.3]  
 $NN \rightarrow pilot$  [0.1]  
 $VBZ \rightarrow likes$  [0.4]  
 $VBG \rightarrow flying$  [0.5]  
 $JJ \rightarrow flying$  [0.1]  
 $NNS \rightarrow planes$  [.34]

# Probabilistic CKY: best parse

a 1	pilot 2	likes 3	flying 4	planes 5
DT [0.3]	NP [.009]	-		
	NN [0.1]	-		
		VBZ [0.4]		

$S \rightarrow NP VP$  [1.0]  
 $VP \rightarrow VBG NNS$  [0.1]  
 $VP \rightarrow VBZ VP$  [0.1]  
 $VP \rightarrow VBZ NP$  [0.3]  
 $NP \rightarrow DT NN$  [0.3]  
 $NP \rightarrow JJ NNS$  [0.4]  
 $DT \rightarrow a$  [0.3]  
 $NN \rightarrow pilot$  [0.1]  
 $VBZ \rightarrow likes$  [0.4]  
 $VBG \rightarrow flying$  [0.5]  
 $JJ \rightarrow flying$  [0.1]  
 $NNS \rightarrow planes$  [.34]

# Probabilistic CKY: best parse

a 1	pilot 2	likes 3	flying 4	planes 5
DT [0.3]	NP [.009]	-		
	NN [0.1]	-		
		VBZ [0.4]		
			JJ [0.1]	

	$S \rightarrow NP VP$	[1.0]
	$VP \rightarrow VBG NNS$	[0.1]
	$VP \rightarrow VBZ VP$	[0.1]
	$VP \rightarrow VBZ NP$	[0.3]
	$NP \rightarrow DT NN$	[0.3]
	$NP \rightarrow JJ NNS$	[0.4]
	$DT \rightarrow a$	[0.3]
	$NN \rightarrow pilot$	[0.1]
	$VBZ \rightarrow likes$	[0.4]
	$VBG \rightarrow flying$	[0.5]
#	$JJ \rightarrow flying$	[0.1]
	$NNS \rightarrow planes$	[.34]

# Probabilistic CKY: best parse

a 1	pilot 2	likes 3	flying 4	planes 5
DT [0.3]	NP [.009]	-		
	NN [0.1]	-		
		VBZ [0.4]		
			JJ [0.1] VBG [0.5]	

	$S \rightarrow NP VP$	[1.0]
	$VP \rightarrow VBG NNS$	[0.1]
	$VP \rightarrow VBZ VP$	[0.1]
	$VP \rightarrow VBZ NP$	[0.3]
	$NP \rightarrow DT NN$	[0.3]
	$NP \rightarrow JJ NNS$	[0.4]
	$DT \rightarrow a$	[0.3]
	$NN \rightarrow pilot$	[0.1]
	$VBZ \rightarrow likes$	[0.4]
#	$VBG \rightarrow flying$	[0.5]
	$JJ \rightarrow flying$	[0.1]
	$NNS \rightarrow planes$	[.34]

# Probabilistic CKY: best parse

a 1	pilot 2	likes 3	flying 4	planes 5
DT [0.3]	NP [.009]	-		
	NN [0.1]	-		
		VBZ [0.4]	-	
			JJ [0.1] VBG [0.5]	

$S \rightarrow NP VP$  [1.0]  
 $VP \rightarrow VBG NNS$  [0.1]  
 $VP \rightarrow VBZ VP$  [0.1]  
 $VP \rightarrow VBZ NP$  [0.3]  
 $NP \rightarrow DT NN$  [0.3]  
 $NP \rightarrow JJ NNS$  [0.4]  
 $DT \rightarrow a$  [0.3]  
 $NN \rightarrow pilot$  [0.1]  
 $VBZ \rightarrow likes$  [0.4]  
 $VBG \rightarrow flying$  [0.5]  
 $JJ \rightarrow flying$  [0.1]  
 $NNS \rightarrow planes$  [.34]

# Probabilistic CKY: best parse

a 1	pilot 2	likes 3	flying 4	planes 5
DT [0.3]	NP [.009]	-		
	NN [0.1]	-	-	
		VBZ [0.4]	-	
			JJ [0.1] VBG [0.5]	

$S \rightarrow NP VP$  [1.0]  
 $VP \rightarrow VBG NNS$  [0.1]  
 $VP \rightarrow VBZ VP$  [0.1]  
 $VP \rightarrow VBZ NP$  [0.3]  
 $NP \rightarrow DT NN$  [0.3]  
 $NP \rightarrow JJ NNS$  [0.4]  
 $DT \rightarrow a$  [0.3]  
 $NN \rightarrow pilot$  [0.1]  
 $VBZ \rightarrow likes$  [0.4]  
 $VBG \rightarrow flying$  [0.5]  
 $JJ \rightarrow flying$  [0.1]  
 $NNS \rightarrow planes$  [.34]

# Probabilistic CKY: best parse

a 1	pilot 2	likes 3	flying 4	planes 5
DT [0.3]	NP [.009]	-	-	
	NN [0.1]	-	-	
		VBZ [0.4]	-	
			JJ [0.1] VBG [0.5]	

*S* → *NP VP* [1.0]  
*VP* → *VBG NNS* [0.1]  
*VP* → *VBZ VP* [0.1]  
*VP* → *VBZ NP* [0.3]  
*NP* → *DT NN* [0.3]  
*NP* → *JJ NNS* [0.4]  
*DT* → *a* [0.3]  
*NN* → *pilot* [0.1]  
*VBZ* → *likes* [0.4]  
*VBG* → *flying* [0.5]  
*JJ* → *flying* [0.1]  
*NNS* → *planes* [.34]

# Probabilistic CKY: best parse

a 1	pilot 2	likes 3	flying 4	planes 5
DT [0.3]	NP [.009]	-	-	
	NN [0.1]	-	-	
		VBZ [0.4]	-	
			JJ [0.1] VBG [0.5]	
				NNS [.34]

<i>S</i> → <i>NP VP</i>	[1.0]
<i>VP</i> → <i>VBG NNS</i>	[0.1]
<i>VP</i> → <i>VBZ VP</i>	[0.1]
<i>VP</i> → <i>VBZ NP</i>	[0.3]
<i>NP</i> → <i>DT NN</i>	[0.3]
<i>NP</i> → <i>JJ NNS</i>	[0.4]
<i>DT</i> → <i>a</i>	[0.3]
<i>NN</i> → <i>pilot</i>	[0.1]
<i>VBZ</i> → <i>likes</i>	[0.4]
<i>VBG</i> → <i>flying</i>	[0.5]
<i>JJ</i> → <i>flying</i>	[0.1]
<i>NNS</i> → <i>planes</i>	[.34]

#

# Probabilistic CKY: best parse

a 1	pilot 2	likes 3	flying 4	planes 5
DT [0.3]	NP [.009]	-	-	
	NN [0.1]	-	-	
		VBZ [0.4]	-	
			JJ [0.1] VBG [0.5]	NP [.0136]
				NNS [.34]

	$S \rightarrow NP VP$	[1.0]
	$VP \rightarrow VBG NNS$	[0.1]
	$VP \rightarrow VBZ VP$	[0.1]
	$VP \rightarrow VBZ NP$	[0.3]
	$NP \rightarrow DT NN$	[0.3]
#	$NP \rightarrow JJ NNS$	[0.4]
	$DT \rightarrow a$	[0.3]
	$NN \rightarrow pilot$	[0.1]
	$VBZ \rightarrow likes$	[0.4]
	$VBG \rightarrow flying$	[0.5]
	$JJ \rightarrow flying$	[0.1]
	$NNS \rightarrow planes$	[.34]

$$0.1 \times 0.34 \times 0.4 = 0.0136$$

# Probabilistic CKY: best parse

a 1	pilot 2	likes 3	flying 4	planes 5
DT [0.3]	NP [.009]	-	-	
	NN [0.1]	-	-	
		VBZ [0.4]	-	
			JJ [0.1] VBG [0.5]	NP [.0136] VP [.017]
				NNS [.34]

#	<i>S</i> → <i>NP VP</i>	[1.0]
	<i>VP</i> → <i>VBG NNS</i>	[0.1]
	<i>VP</i> → <i>VBZ VP</i>	[0.1]
	<i>VP</i> → <i>VBZ NP</i>	[0.3]
	<i>NP</i> → <i>DT NN</i>	[0.3]
	<i>NP</i> → <i>JJ NNS</i>	[0.4]
	<i>DT</i> → <i>a</i>	[0.3]
	<i>NN</i> → <i>pilot</i>	[0.1]
	<i>VBZ</i> → <i>likes</i>	[0.4]
	<i>VBG</i> → <i>flying</i>	[0.5]
	<i>JJ</i> → <i>flying</i>	[0.1]
	<i>NNS</i> → <i>planes</i>	[.34]

$$0.5 \times 0.34 \times 0.1 = 0.017$$

# Probabilistic CKY: best parse

a 1	pilot 2	likes 3	flying 4	planes 5
DT [0.3]	NP [.009]	-	-	
	NN [0.1]	-	-	
		VBZ [0.4]	-	VP [.001632]
			JJ [0.1] VBG [0.5]	NP [.0136] VP [.017]
				NNS [.34]

#	$S \rightarrow NP VP$	[1.0]
	$VP \rightarrow VBG NNS$	[0.1]
	$VP \rightarrow VBZ VP$	[0.1]
	$VP \rightarrow VBZ NP$	[0.3]
	$NP \rightarrow DT NN$	[0.3]
	$NP \rightarrow JJ NNS$	[0.4]
	$DT \rightarrow a$	[0.3]
	$NN \rightarrow pilot$	[0.1]
	$VBZ \rightarrow likes$	[0.4]
	$VBG \rightarrow flying$	[0.5]
	$JJ \rightarrow flying$	[0.1]
	$NNS \rightarrow planes$	[.34]

$$0.4 \times 0.0136 \times 0.3 = 0.001632$$

# Probabilistic CKY: best parse

a 1	pilot 2	likes 3	flying 4	planes 5
DT [0.3]	NP [.009]	-	-	
	NN [0.1]	-	-	
		VBZ [0.4]	-	VP [.001632]
			JJ [0.1] VBG [0.5]	NP [.0136] VP [.017]
				NNS [.34]

#	<i>S</i> → <i>NP VP</i>	[1.0]
	<i>VP</i> → <i>VBG NNS</i>	[0.1]
	<i>VP</i> → <i>VBZ VP</i>	[0.1]
	<i>VP</i> → <i>VBZ NP</i>	[0.3]
	<i>NP</i> → <i>DT NN</i>	[0.3]
	<i>NP</i> → <i>JJ NNS</i>	[0.4]
	<i>DT</i> → <i>a</i>	[0.3]
	<i>NN</i> → <i>pilot</i>	[0.1]
	<i>VBZ</i> → <i>likes</i>	[0.4]
	<i>VBG</i> → <i>flying</i>	[0.5]
	<i>JJ</i> → <i>flying</i>	[0.1]
	<i>NNS</i> → <i>planes</i>	[.34]

Move second VP to  
chart?  
 $0.4 \times 0.017 \times 0.1 =$   
 0.00068

# Probabilistic CKY: best parse

a 1	pilot 2	likes 3	flying 4	planes 5
DT [0.3]	NP [.009]	-	-	
	NN [0.1]	-	-	
		VBZ [0.4]	-	VP [.001632]
			JJ [0.1] VBG [0.5]	NP [.0136] VP [.017]
				NNS [.34]

*S* → *NP VP* [1.0]  
*VP* → *VBG NNS* [0.1]  
*VP* → *VBZ VP* [0.1]  
*VP* → *VBZ NP* [0.3]  
*NP* → *DT NN* [0.3]  
*NP* → *JJ NNS* [0.4]  
*DT* → *a* [0.3]  
*NN* → *pilot* [0.1]  
*VBZ* → *likes* [0.4]  
*VBG* → *flying* [0.5]  
*JJ* → *flying* [0.1]  
*NNS* → *planes* [.34]

Is 0.001632  
less than 0.00068 ?

# Probabilistic CKY: best parse

a 1	pilot 2	likes 3	flying 4	planes 5
DT [0.3]	NP [.009]	-	-	
	NN [0.1]	-	-	-
		VBZ [0.4]	-	VP [.001632]
			JJ [0.1] VBG [0.5]	NP [.0136] VP [.017]
				NNS [.34]

*S* → *NP VP* [1.0]  
*VP* → *VBG NNS* [0.1]  
*VP* → *VBZ VP* [0.1]  
*VP* → *VBZ NP* [0.3]  
*NP* → *DT NN* [0.3]  
*NP* → *JJ NNS* [0.4]  
*DT* → *a* [0.3]  
*NN* → *pilot* [0.1]  
*VBZ* → *likes* [0.4]  
*VBG* → *flying* [0.5]  
*JJ* → *flying* [0.1]  
*NNS* → *planes* [.34]

# Probabilistic CKY: best parse

a 1	pilot 2	likes 3	flying 4	planes 5
DT [0.3]	NP [.009]	-	-	S [1.4688x10 <sup>-5</sup> ]
	NN [0.1]	-	-	-
		VBZ [0.4]	-	VP [.001632]
			JJ [0.1] VBG [0.5]	NP [.0136] VP [.017]
				NNS [.34]

#	<i>S</i> → <i>NP VP</i>	[1.0]
	<i>VP</i> → <i>VBG NNS</i>	[0.1]
	<i>VP</i> → <i>VBZ VP</i>	[0.1]
	<i>VP</i> → <i>VBZ NP</i>	[0.3]
	<i>NP</i> → <i>DT NN</i>	[0.3]
	<i>NP</i> → <i>JJ NNS</i>	[0.4]
	<i>DT</i> → <i>a</i>	[0.3]
	<i>NN</i> → <i>pilot</i>	[0.1]
	<i>VBZ</i> → <i>likes</i>	[0.4]
	<i>VBG</i> → <i>flying</i>	[0.5]
	<i>JJ</i> → <i>flying</i>	[0.1]
	<i>NNS</i> → <i>planes</i>	[.34]

$$0.009 \times 0.001632 \times 1.0 = 1.4688 \times 10^{-5}$$