

Consider rubber sphere initially at $T_i = 25^\circ\text{C}$

placed into boiling water at $T_\infty = 100^\circ\text{C}$ (large h).

Sphere properties: $k = 0.15 \frac{\text{W}}{\text{mK}}$, $\rho = 1000 \frac{\text{kg}}{\text{m}^3}$,
 $c = 2000 \frac{\text{J}}{\text{kgK}}$ with $\alpha = \frac{k}{\rho c} = \frac{0.15 \frac{\text{W}}{\text{mK}}}{1000 \frac{\text{kg}}{\text{m}^3} \cdot 2000 \frac{\text{J}}{\text{kgK}}}$
 $\alpha = 7.5 \times 10^{-8} \frac{\text{m}^2}{\text{s}}$, $R = 0.01 \text{ m}$

Using the infinite series solution obtained in class for constant T_s , plot $T(r, t)$.

$$\Theta = \frac{T(r, t) - T_\infty}{T_i - T_\infty} = \sum_{n=1}^{\infty} A_n \frac{\sin(\lambda_n r)}{\lambda_n r} \exp(-\alpha \lambda_n^2 t)$$

where $A_n = -2\cos(\lambda_n R)$, $\lambda_n = \frac{n\pi}{R}$, $n = 1, 2, 3, \dots$

Compare the exact solution with the semi-infinite solid solution for constant T_s :

$$\frac{T(x, t) - T_s}{T_i - T_s} = \text{erf}\left(\frac{x}{2\sqrt{\alpha t}}\right)$$

Note that in this expression, x is the position measured from the outer surface into the interior of the sphere.