



$$H(s) = \frac{X(s)}{U(s)} = \frac{cs + k}{\frac{3}{2}ms^2 + cs + k}$$

Damping point impedance

$$Z(s) \equiv \frac{sU(s)}{F(s)}$$

$k(u-x) \leftarrow$
 $\bullet \rightarrow f(t)$
 $c(\dot{u}-\dot{x}) \leftarrow$

Equilibrium requires

$$f(t) = k(u-x) + c(\dot{u}-\dot{x})$$

OR

$$F(s) = (k+cs) [U(s) - X(s)]$$

Hence

$$\begin{aligned} \frac{F(s)}{sU(s)} &= \frac{k+cs}{s} \left[1 - \frac{X(s)}{U(s)} \right] \\ &= \frac{k+cs}{s} \left[1 - \frac{cs+k}{\frac{3}{2}ms^2 + cs + k} \right] \end{aligned}$$

$$= \frac{k+cs}{s} \left[\frac{\frac{3}{2}ms^2}{\frac{3}{2}ms^2 + cs + k} \right]$$

$$Z(s) = \frac{sU(s)}{F(s)} = \frac{\frac{3}{2}ms^2 + cs + k}{\frac{3}{2}ms(k+cs)}$$