# ME556: Experimental Stress Analysis I

Take-Home Final Exam:

- Distributed via e-mail at/before 2pm on Tuesday 5 December
- Open-book, open notes
- Cannot be discussed with anyone other than Prof. Mark Tuttle
- If questions, call or e-mail:
  - tuttle@uw.edu
  - 206-543-5710
- Submit completed exam by 5pm on Thursday 7 December to dropbox:

https://www.dropbox.com/request/9d9vP8PYXIQ7ILkHoWbQ Clearly describe how solutions were obtained

Review of Stress, Strain, and Hooke's Law

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- Mathematical form of Hooke's law depends on
  - Material type (e.g., isotropic vs anisotropic)
  - Stress or strain state (e.g., 3-D, plane stress, plane strain, uniaxial stress, uniaxial strain)

Review of Methods to Predict Failure

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  - Use  $\Delta K_I$  to predict fatigue life via Paris Law/Paris Plot (Lab 4)

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  - Based on capacitance measurements
  - Based on inductance measurements
  - Based on resistance measurements (*strain gages*)

Resistance Strain Gages (Gauges):

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  - Common alloys
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    - Change in  $S_g$  (usually minimal; often ignored)
    - Apparent strain due to temperature (usually pronounced; never ignored) ...self-temperature-compensated (STC) gages

- Commercially available forms:
  - Uniaxial (Lab 1, Lab 2)
  - Biaxial rosettes
  - Three-element rosettes
    - Rectangular (Labs 3, 4)
    - Delta
  - Special forms
    - Shear strain gages
    - Stress gages
    - Residual stress gages ("hole drilling method")
    - Strip gages ("virtual" Lab 6)

Wheatstone Bridge Circuit:

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  - Shunt calibration

Strain Gage-Based Load Cells:

- Common configurations (S-beam, shear-beam, torque, etc)
- Common specifications (capacity, excitation, output, etc)

Brief Discussion of

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  - Gain
  - Phase
  - Cutoff frequency ("3 dB down point" or "half-power point")

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- Digital Data Acquisition
  - Unipolar vs bipolar A/D boards and D/A boards
  - Range and wordlength
  - Potential aliasing errors