

ME556 Homework Problem #2

Solution

• Beam theory predicts: $\epsilon_{xx} = \frac{M_y z}{EI_y} - \frac{M_z y}{EI_z}$

• In this case: $I_z = \frac{bh^3}{12}$ $I_y = \frac{hb^3}{12}$

$M_z = M \cos \theta = \frac{Pd}{2} \cos \theta$ $M_y = M \sin \theta = \frac{Pd}{2} \sin \theta$

• Combining the above, we have:

$$\epsilon_{xx} = \frac{6Pd}{hbE} \left[\frac{z \sin \theta}{b^2} - \frac{y \cos \theta}{h^2} \right]$$

• This expression is valid for any point in the cross-section, as defined by coordinates (y,z). Point a is located at $y = h/2$ and $z = b/2$. Substituting these particular coordinates we have:

$$\epsilon_{xx} = \frac{3Pd}{hbE} \left[\frac{\sin \theta}{b} - \frac{\cos \theta}{h} \right]$$

• Finally, the problem states to plot ϵ_{xx} for $0 < P < 500$ lbf, assuming

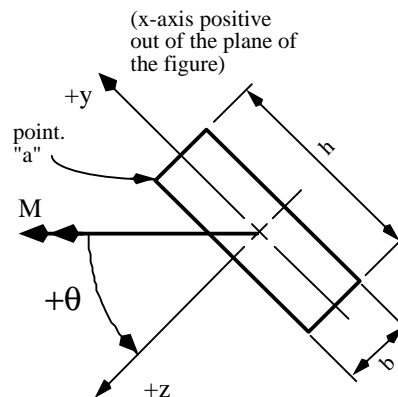
$$E = 10 \times 10^6 \text{ psi}, d = 5.0 \text{ in}, b = 0.5 \text{ in}, h = 1.0 \text{ in}$$

Plots appear on the following page. Note that by inspection it can be seen that:

-strains at point "a" should be of equal magnitude but opposite algebraic sign for two cases:

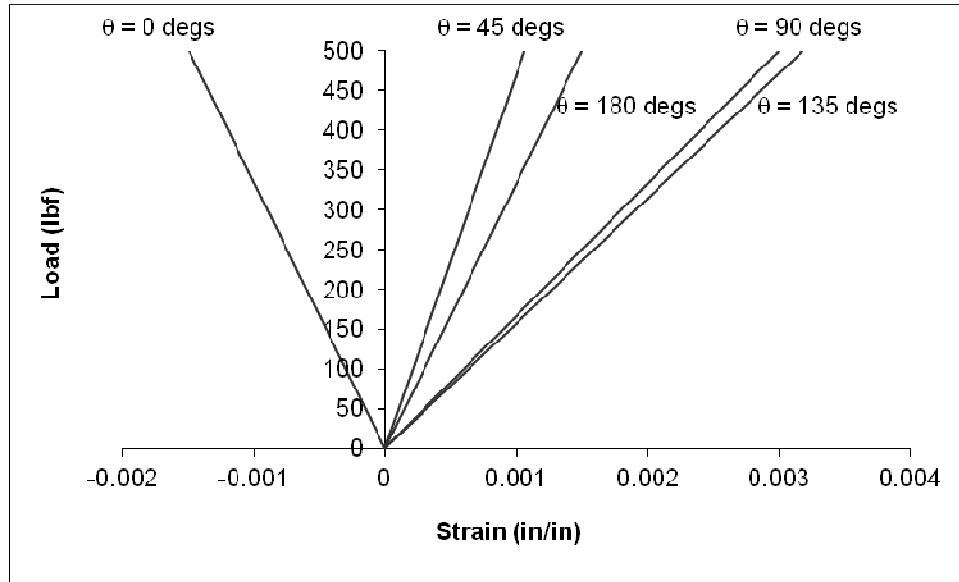
$$\theta = 0^\circ \quad (\text{and}) \quad \theta = 180^\circ$$

- strains at point "a" are compressive if $\theta = 0^\circ$



STRAIN INDUCED AT POINT "a" BY A PURE BENDING MOMENT

Plotted as Load vs Strain:



Or Plotted as Strain vs Load:

