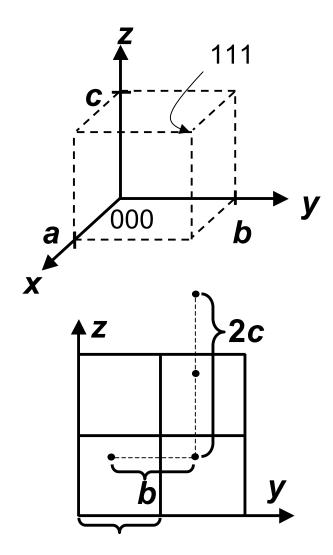
Point coordinates

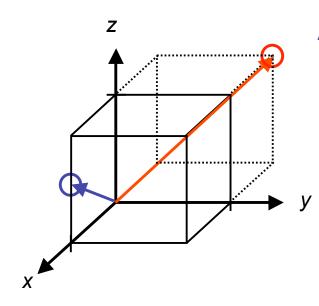


• Point coordinates for unit cell center are

a/2, b/2, c/2 ¹/₂ ¹/₂

- Point coordinates for unit cell corner are 111
- Translation: integer multiple of lattice constants → identical position in another unit cell

Directions



Algorithm

- 1. Vector repositioned (if necessary) to pass through origin.
- 2. Read off projections in terms of unit cell dimensions *a*, *b*, and *c*
- 3. Adjust to smallest integer values
- 4. Enclose in square brackets, no commas [*xyz*]

ex: 1, 0, $\frac{1}{2}$ => 2, 0, 1 => [201]

-1, 1, 1 = [111] where overbar represents a negative index

families of directions <xyz>

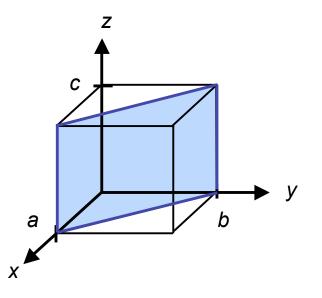
Miller Indices: Reciprocals of the (three) axial intercepts for a plane, cleared of fractions & common multiples. All parallel planes have same Miller indices.

Algorithm

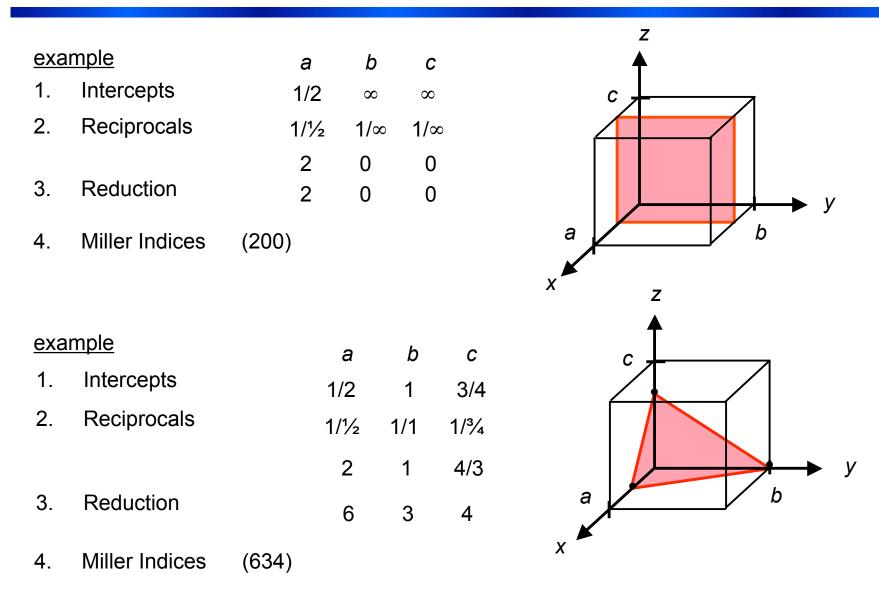
- 1. Read off intercepts of plane with axes in terms of a, b, c
- 2. Take reciprocals of intercepts
- 3. Reduce to smallest integer values
- 4. Enclose in parentheses, no commas i.e., (hkl)

mple	а	b	С
Intercepts	1	1	∞
Reciprocals	1/1	1/1	1/∞
Reduction	1	1	0
	<u>mple</u> Intercepts Reciprocals Reduction	Intercepts 1 Reciprocals 1/1	Intercepts 1 1 Reciprocals 1/1 1/1

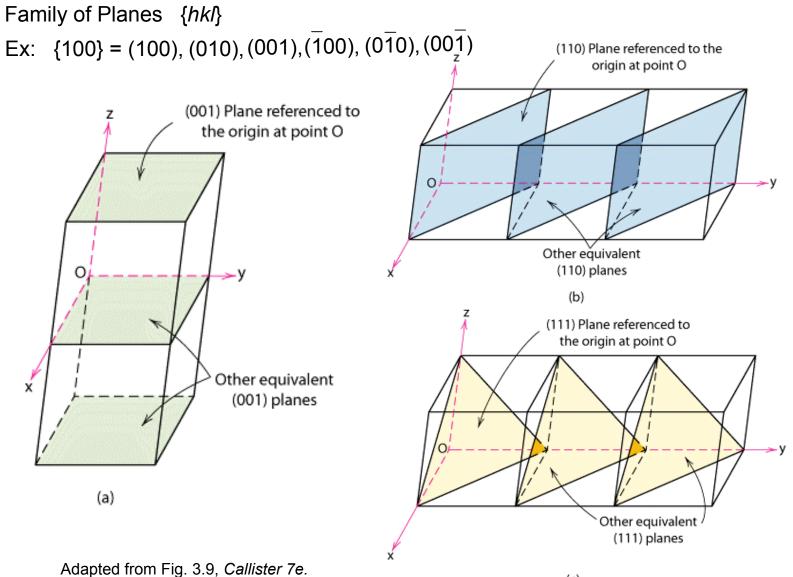
4. Miller Indices (110)



Crystallographic planes



Crystallographic planes

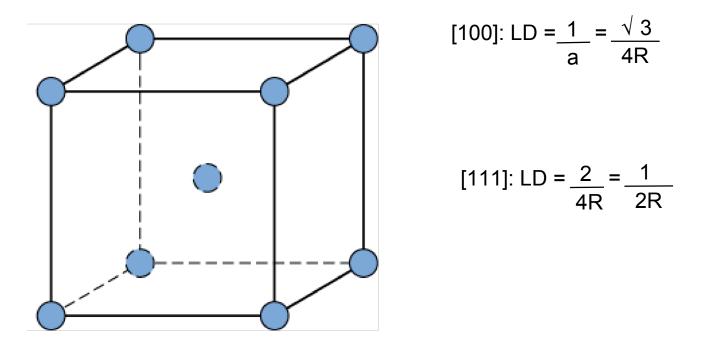


(c)

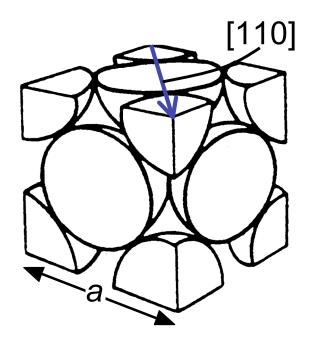
5

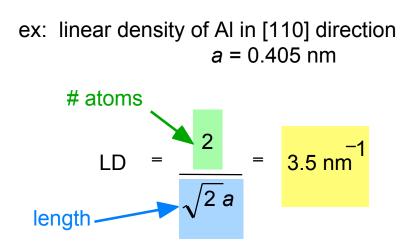
Linear density: BCC

Linear Density of Atoms = $LD = \frac{Number of atoms}{Unit length of direction vector}$



Linear density (FCC) and planar densitry

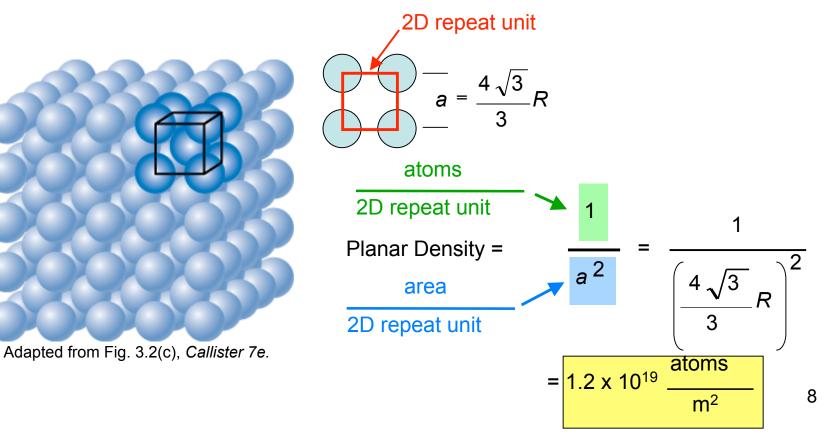




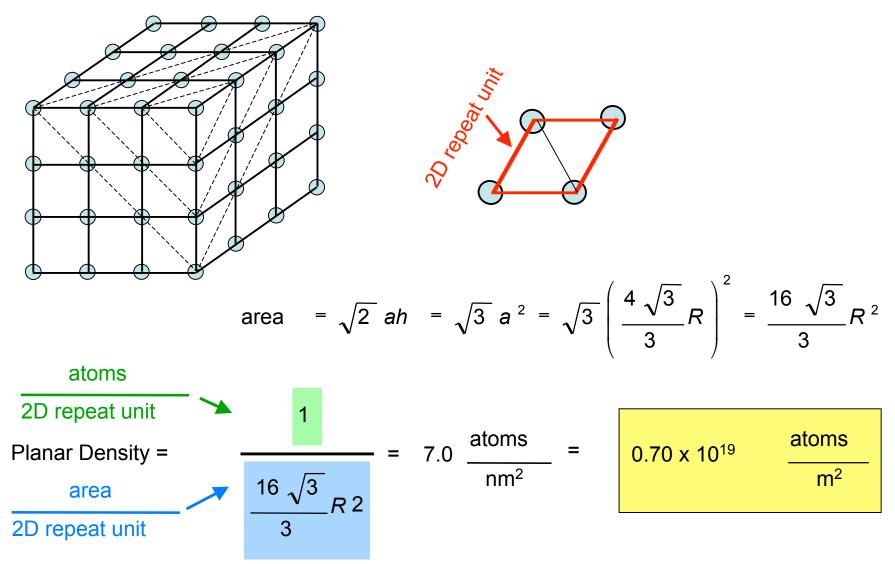
Planar Density of Atoms = PD = $\frac{\text{Number of atoms}}{\text{Area of plane}}$

Planar density

- We want to examine the atomic packing of crystallographic planes
- Iron foil can be used as a catalyst. The atomic packing of the exposed planes is important.
 - a) Draw (100) and (111) crystallographic planes for Fe.
 - b) Calculate the planar density for each of these planes.
 - R = 0.1241 nm and Fe has a BCC structure at room temperature



Planar density



Single crystal vs. Polycrystalline structures

Single crystals: Atoms all have the same arrangement throughout. Polycrystalline: Many crystals put together.

Anisotropic



Adapted from Fig. K, color inset pages of *Callister 5e*. (Fig. K is courtesy of Paul E. Danielson, Teledyne Wah Chang Albany)

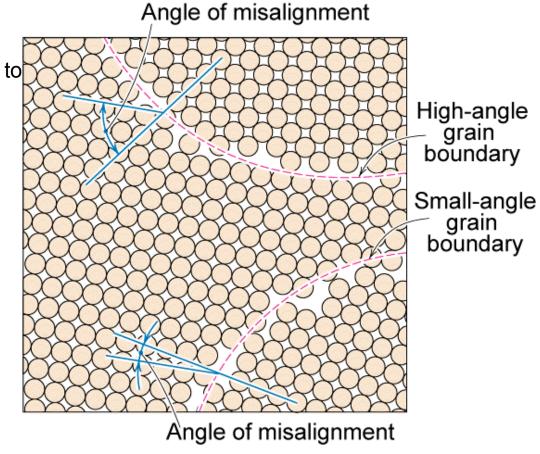
Isotropic

- Nb-Hf-W plate with an electron beam weld.
- Each "grain" is a single crystal.
- If grains are randomly oriented, overall component properties are not directional.
- Grain sizes typ. range from 1 nm to 2 cm (i.e., from a few to millions of atomic layers).

Polycrystalline structures

Grain Boundaries

- regions between crystals
- transition from lattice of one region to that of the other
- slightly disordered
- low density in grain boundaries
 - o high mobility
 - o high diffusivity
 - o high chemical reactivity

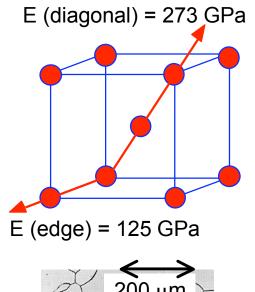


Adapted from Fig. 4.7, Callister 7e.

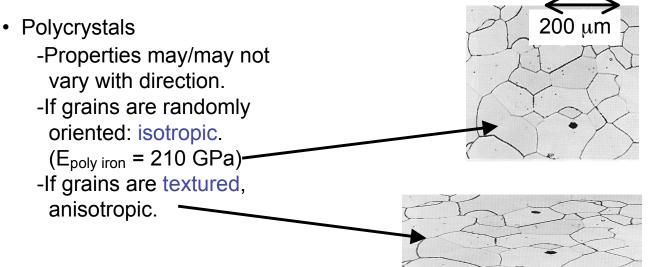
Single crystal vs. Polycrystalline structures

 Single Crystals

 Properties vary with direction: anisotropic.
 Example: the modulus of elasticity (E) in BCC iron:



Data from Table 3.3, *Callister 7e*. (Source of data is R.W. Hertzberg, *Deformation and Fracture Mechanics of Engineering Materials*, 3rd ed., John Wiley and Sons, 1989.)

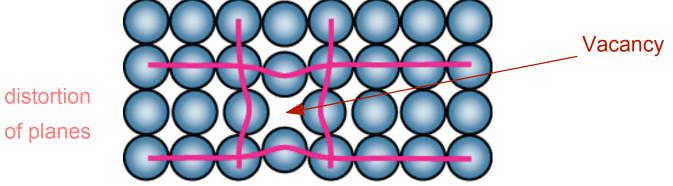


Adapted from Fig. 4.14(b), *Callister 7e*. (Fig. 4.14(b) is courtesy of L.C. Smith and C. Brady, the National Bureau of Standards, Washington, DC [now the National Institute of Standards and Technology, Gaithersburg, MD].)

Point defects

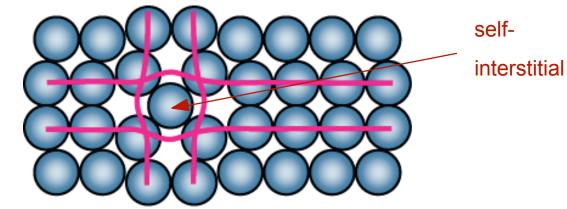
• Vacancies:

-vacant atomic sites in a structure.



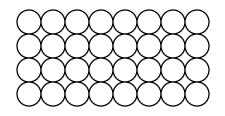
- Self-Interstitials:
 - -"extra" atoms positioned between atomic sites.



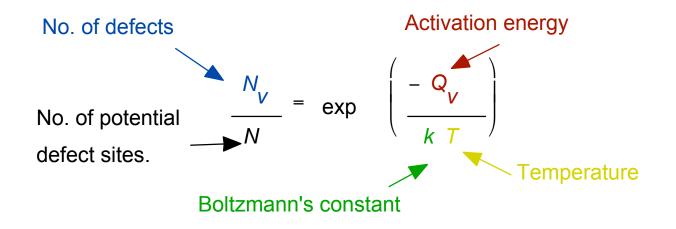


Equilibrium concentration of defects

• Equilibrium concentration varies with temperature



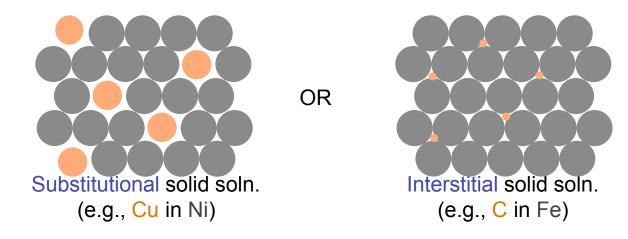
Each lattice site is a potential vacancy



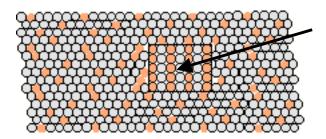
Point defects in alloys

Two outcomes if impurity (B) added to host (A):

• Solid solution of B in A (i.e., random dist. of point defects)



 Solid solution of B in A plus particles of a new phase (usually for a larger amount of B)



Second phase particle --different composition --often different structure.

Imperfections of solids

Conditions for substitutional solid solution (S.S.)

W. Hume – Rothery rule

- 1. Δr (atomic radius) < 15%
- 2. Proximity in periodic table
 - i.e., similar electronegativities
- 3. Same crystal structure for pure metals
- 4. Valency

All else being equal, a metal will have a greater tendency to dissolve a metal of higher valency than one of lower valency

	Element	Atomic Radius (nm)	Crystal Structure	Electro- nega- tivity	Valence
 Would you predict more Al or Ag to dissolve in Zn? More Zn or Al in Cu? 	Cu C	0.1278 0.071	FCC	1.9	+2
	H O Ag	0.046 0.060 0.1445	FCC	1.9	+1
Table on p. 106, <i>Callister 7e.</i>	Al Ni Zn	0.1431 0.1246 0.1332	FCC FCC HCP	1.5 1.8 1.6	+3 +2 ₁₆ +2

Line defects

•Linear Defects (Dislocations)

Are one-dimensional defects around which atoms are misaligned

•Edge dislocation:

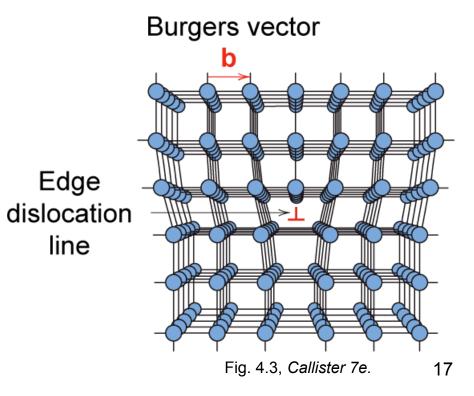
•extra half-plane of atoms inserted in a crystal structure

 $\bullet \textbf{b} \perp \text{to dislocation line}$

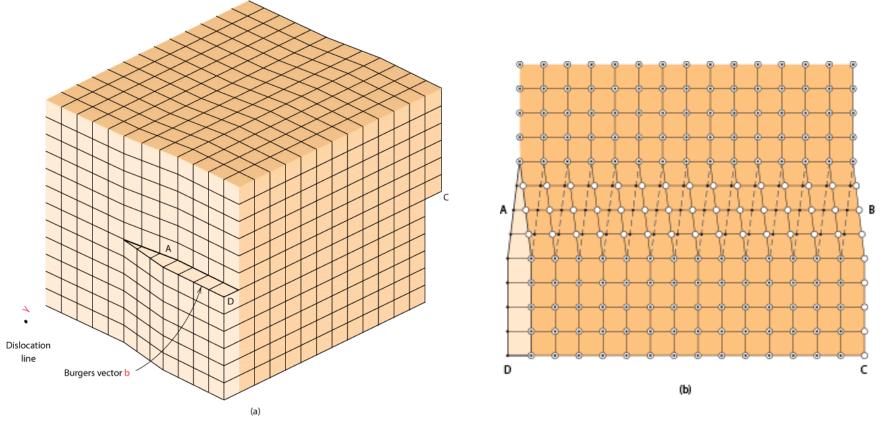
Screw dislocation:

•spiral planar ramp resulting from shear deformation

•b || to dislocation line

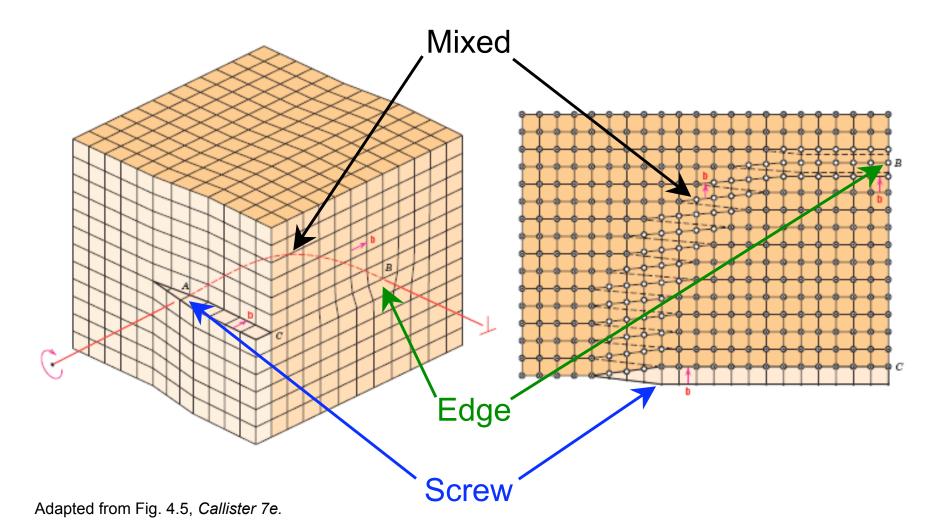


Screw defects



Adapted from Fig. 4.4, Callister 7e.

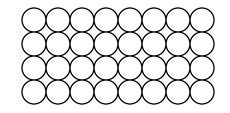
Mixed defects



Planar defects

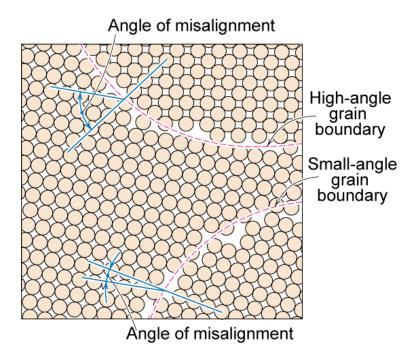
•External defects

On the surfaceUnsatisfied bonds



Internal defects

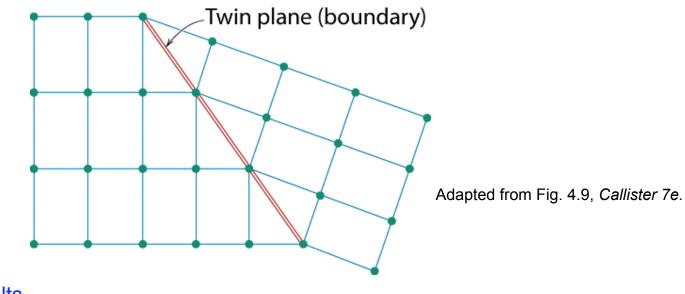
•Grain boundaries



Planar defects

• Twin boundary (plane)

Essentially a reflection of atom positions across the twin plane.



• Stacking faults

For FCC metals an error in ABCABC packing sequence Ex: ABCABABC