

Relativity

| | |
|------------------------------------|--|
| time dilation/Lorentz contraction: | $\gamma = 1/\sqrt{1 - \vec{v}^2/c^2}$ |
| 4-coordinates: | $x^\mu = (x^0, x^1, x^2, x^3), \quad x^0 = ct$ |
| Lorentz transformation matrix: | $\ F^\mu{}_\nu\ = \begin{pmatrix} \gamma & \gamma(v/c) & 0 & 0 \\ \gamma(v/c) & \gamma & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}$ for boost along \hat{x}^1 |
| Lorentz invariant dot product: | $a \cdot b = -a^0 b^0 + \vec{a} \cdot \vec{b} = -a^0 b^0 + a^1 b^1 + a^2 b^2 + a^3 b^3$ |
| invariant interval: | $s^2 = -(\Delta x^0)^2 + (\Delta x^1)^2 + (\Delta x^2)^2 + (\Delta x^3)^2$ |
| 4-velocity: | $u = \frac{dx(\tau)}{d\tau}, \quad u^\mu = (\gamma c, \gamma \vec{v}), \quad u^2 = -c^2$ |
| 4-momentum: | $p = m u, \quad p^\mu = (E/c, \vec{p}) = (\gamma mc, \gamma m \vec{v})$ $p^2 = -(E/c)^2 + \vec{p}^2 = -m^2 c^2$ |
| 4-force: | $f = \frac{dp}{d\tau}, \quad p \cdot f = 0$ |
| 4-acceleration: | $a = \frac{du}{d\tau}, \quad u \cdot a = 0$ |
| constant acceleration: | $u^0(\tau)/c = \cosh \frac{F\tau}{mc}, \quad u^1(\tau)/c = \sinh \frac{F\tau}{mc}$ |
| wave-vector: | $k^\mu = (\omega/c, \vec{k})$ |
| observed frequency: | $\omega_{\text{obs}} = -u_{\text{obs}} \cdot k$ |
| E&M field strength: | $\ F^\mu{}_\nu\ = \begin{pmatrix} 0 & E_x & E_y & E_z \\ E_x & 0 & cB_z & -cB_y \\ E_y & -cB_z & 0 & cB_x \\ E_z & cB_y & -cB_x & 0 \end{pmatrix}$ |
| Lorentz force: | $f_{\text{Lorentz}}^\mu = \frac{q}{c} F^\mu{}_\nu u^\nu$ |

Constants and Units

$$c = 2.997 \dots \times 10^8 \text{ m/s}$$

$$\hbar = 6.582 \dots \times 10^{-22} \text{ MeV s}$$

$$\hbar c = 197.3 \dots \text{ MeV fm}, \quad 1 \text{ fm} = 10^{-15} \text{ m}$$

$$(\hbar c)^2 = 0.389 \dots \text{ GeV}^2 \text{ mbarn}, \quad 1 \text{ barn} = 10^{-28} \text{ m}^2$$

$$\alpha = e^2/(4\pi\epsilon_0\hbar c) = 1/137.0 \dots$$

Nuclei

| nucleus | symbol | rest energy | lifetime | spin* | decay type |
|--------------|--------------------------|-------------|-----------------------|-------|----------------|
| neutron | n | 939.6 MeV | 15 min | 1/2 | β decay |
| hydrogen | ${}^1_1\text{H}$ | 938.27 MeV | stable | 1/2 | — |
| deuterium | ${}^2_1\text{H}$ | 1875.61 MeV | stable | 1 | — |
| tritium | ${}^3_1\text{H}$ | 2808.92 MeV | 17.8 yr | 1/2 | β decay |
| helium-3 | ${}^3_2\text{He}$ | 2808.39 MeV | stable | 1/2 | — |
| helium-4 | ${}^4_2\text{He}$ | 3727.38 MeV | stable | 0 | — |
| helium-6 | ${}^6_2\text{He}$ | 5605.5 MeV | 1.16 s | 0 | β decay |
| lithium-6 | ${}^6_3\text{Li}$ | 5601.5 MeV | stable | 1 | — |
| lithium-7 | ${}^7_3\text{Li}$ | 6533.8 MeV | stable | 3/2 | — |
| beryllium-7 | ${}^7_4\text{Be}$ | 6534.2 MeV | 77 day | 3/2 | e^- capture |
| beryllium-10 | ${}^{10}_4\text{Be}$ | 9325.5 MeV | 2.2 Myr | 0 | β decay |
| boron-10 | ${}^{10}_5\text{B}$ | 9324.4 MeV | stable | 3 | — |
| boron-11 | ${}^{11}_5\text{B}$ | 10253 MeV | stable | 3/2 | — |
| boron-14 | ${}^{14}_5\text{B}$ | 13062 MeV | 18 ms | 2 | β decay |
| carbon-11 | ${}^{11}_6\text{C}$ | 10254 MeV | 29 m | 3/2 | e^+ emission |
| carbon-12 | ${}^{12}_6\text{C}$ | 11175 MeV | stable | 0 | — |
| carbon-14 | ${}^{14}_6\text{C}$ | 13041 MeV | 5.7 Kyr | 0 | β decay |
| calcium-41 | ${}^{41}_{20}\text{Ca}$ | 38146 MeV | 1.5 Myr | 7/2 | e^- capture |
| bismuth-209 | ${}^{209}_{83}\text{Bi}$ | 194622 MeV | 2×10^{19} yr | 9/2 | α decay |

Leptons

| particle | symbol | rest energy | lifetime | spin* | charge [†] | L |
|-------------------------|----------------------------|-------------|------------------|-------|---------------------|--------|
| electron (anti)neutrino | $\nu_e(\bar{\nu}_e)$ | < 2 eV | \approx stable | 1/2 | 0 | +1(−1) |
| muon (anti)neutrino | $\nu_\mu(\bar{\nu}_\mu)$ | < 2 eV | \approx stable | 1/2 | 0 | +1(−1) |
| tau (anti)neutrino | $\nu_\tau(\bar{\nu}_\tau)$ | < 2 eV | \approx stable | 1/2 | 0 | +1(−1) |
| electron(positron) | $e^-(e^+)$ | 0.511 MeV | stable | 1/2 | −1(+1) | +1(−1) |
| muon(antimuon) | $\mu^-(\mu^+)$ | 105.7 MeV | $2 \mu\text{s}$ | 1/2 | −1(+1) | +1(−1) |
| tau(antitau) | $\tau^-(\tau^+)$ | 1777 MeV | 0.3 ps | 1/2 | −1(+1) | +1(−1) |

*In units of \hbar .

†In units of $|e| = 1.602 \dots \times 10^{-19}$ C.

Hadrons

| particle | symbol | rest energy | lifetime | spin | charge | B |
|---------------|---|-------------|-----------------------|------|---------------|-------|
| pion | π^0 | 135.0 MeV | 8×10^{-17} s | 0 | 0 | 0 |
| pion | π^+, π^- | 139.57 MeV | 26 ns | 0 | +1, -1 | 0 |
| kaon | K^+, K^- | 493.7 MeV | 12 ns | 0 | +1, -1 | 0 |
| kaon | K^0 | 497.7 MeV | 90 ps/51 ns | 0 | 0 | 0 |
| eta | η | 547.5 MeV | 5×10^{-19} s | 0 | 0 | 0 |
| rho | ρ^+, ρ^0, ρ^- | 775 MeV | 4×10^{-24} s | 1 | +1, 0, -1 | 0 |
| omega | ω | 783 MeV | 8×10^{-23} s | 1 | 0 | 0 |
| (anti)proton | $p(\bar{p})$ | 938 MeV | stable | 1/2 | +1(-1) | 1(-1) |
| (anti)neutron | $n(\bar{n})$ | 940 MeV | 886 s | 1/2 | 0 | 1(-1) |
| eta-prime | η' | 958 MeV | 3×10^{-21} s | 0 | 0 | 0 |
| Lambda | Λ | 1116 MeV | 0.26 ns | 1/2 | 0 | 1 |
| Delta | $\Delta^{++}, \Delta^+, \Delta^0, \Delta^-$ | 1232 MeV | 6×10^{-24} s | 3/2 | +2, +1, 0, -1 | 1 |
| Cascade | Ξ^0 | 1315 MeV | 0.29 ns | 1/2 | 0 | 1 |
| Cascade | Ξ^- | 1321 MeV | 0.16 ns | 1/2 | -1 | 1 |
| Omega | Ω^- | 1672 MeV | 0.08 ns | 1/2 | -1 | 1 |