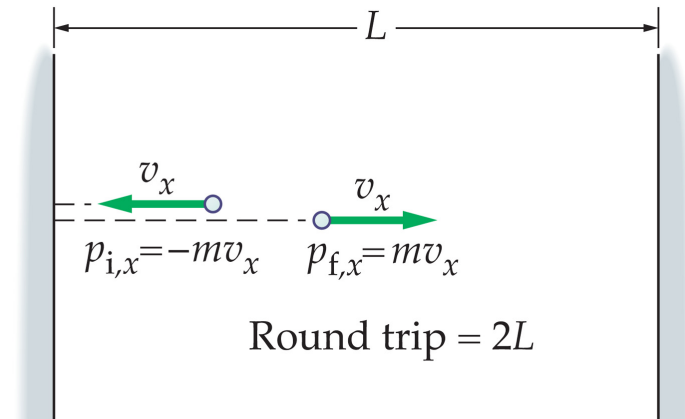


Physics 115

General Physics II

Session 9



Molecular motion and temperature

Phase equilibrium, evaporation

- R. J. Wilkes
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- Home page: <http://courses.washington.edu/phy115a/>

Lecture Schedule (up to exam 1)

Date	Day	Lect.	Topic	readings in Walker
31-Mar	Mon	1	Introduction, Preview	
1-Apr	Tues	2	Density & Pressure	15.1-15.3
3-Apr	Thurs	3	Static Fluids, Buoyancy	15.4-15.5
4-Apr	Fri	4	Fluid Flow, Bernoulli	15.6-15.8
7-Apr	Mon	5	Viscosity, Flow, Capillaries	15.9
8-Apr	Tues	6	Temperature, expansion	16.1-16.3
10-Apr	Thurs	7	Heat, Conduction	16.4-16.6
11-Apr	Fri	8	Ideal gas	17.1-17.2
14-Apr	Mon	9	Heat, Evaporation	17.4-17.5
15-Apr	Tues	10	Phase change	17.6
17-Apr	Thurs	11	First Law Thermodynamics	18.1-18.3
18-Apr	Fri		EXAM 1 Ch 15,16,17	

Just joined the class? See course home page

courses.washington.edu/phy115a/

for course info, and slides from previous sessions

Today

4/14/14

Physics 115

Announcements

- Prof. Jim Reid is standing in for RJW this week
- Exam 1 **this Friday 4/18**, in class, formula sheet provided
 - YOU bring a bubble sheet , pencil, calculator (NO laptops or phones; **NO personal notes allowed.**)
 - We will post sample questions tomorrow, and go over them in class Thursday
- Clicker responses from **last** week are posted, so you can check if your clicker is being detected. See link on class home page, <http://courses.washington.edu/phy115a>

Last time

Gas Law: Avogadro's number and R

Counting molecules to get N is difficult, so it is convenient to use Avogadro's number N_A , the number of carbon atoms in exactly 12 g (1 mole) of carbon. 1 mol = {molecular mass, A} grams of gas (For **elements**, what you see on the Periodic Table is A **averaged over isotopes**)

$N_A = 6.022 \times 10^{23}$ molecules/mole and $N = nN_A$, where n = number of moles of gas

$$PV = nN_A kT = nRT$$

Notice PV = energy: N-m $\frac{PV}{nT}, \text{J/mol} \cdot \text{K}$

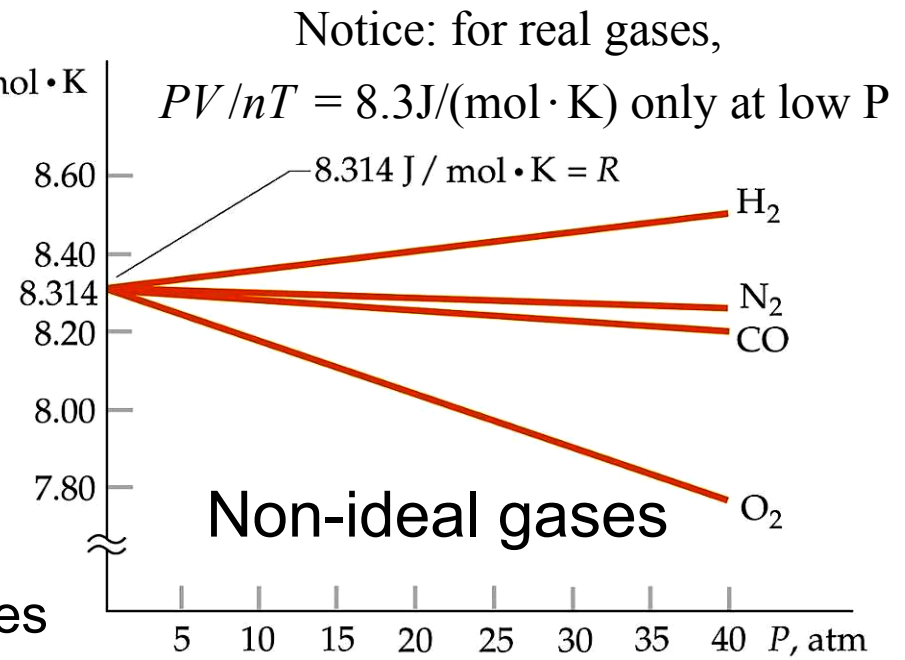
$$R = N_A k = 8.314 \text{ J/(mol} \cdot \text{K)}$$

$$PV = nRT$$

Ideal Gas Law, in moles

R = "Universal gas constant"

Good approx at low P for real gases



Isotherm plots

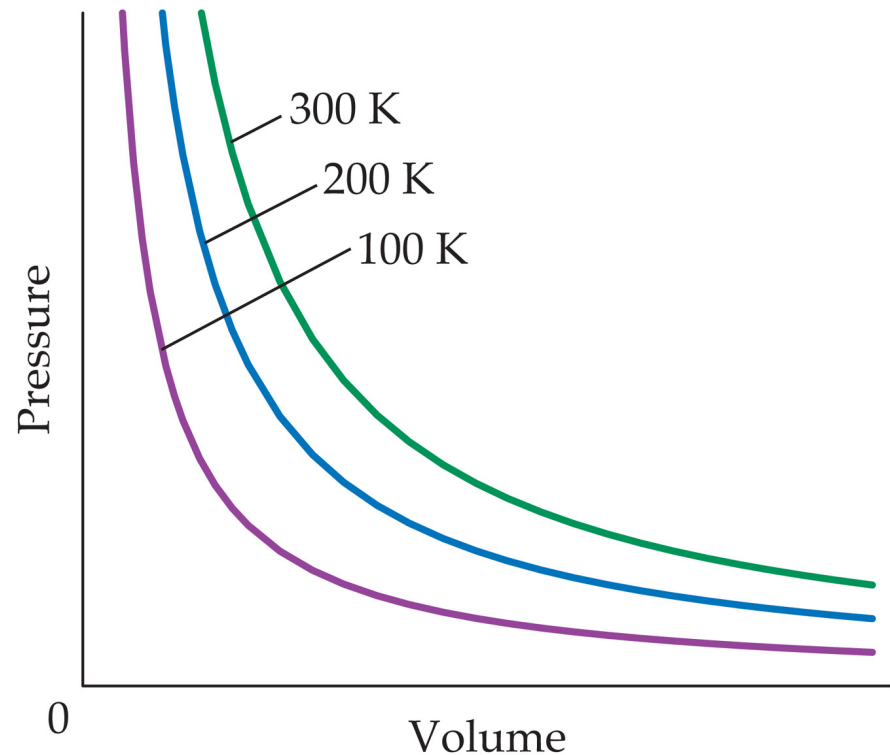
- $PV = NkT$ results from many different observations:
 - Hold N , T constant and see how P , V vary: find

$$PV = \text{const} \rightarrow P = \frac{\text{const}}{V}$$

(with T and N fixed)

Boyle's Law

For different T 's we get a set of $(1/V)$ -shaped curves



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Isobar plots

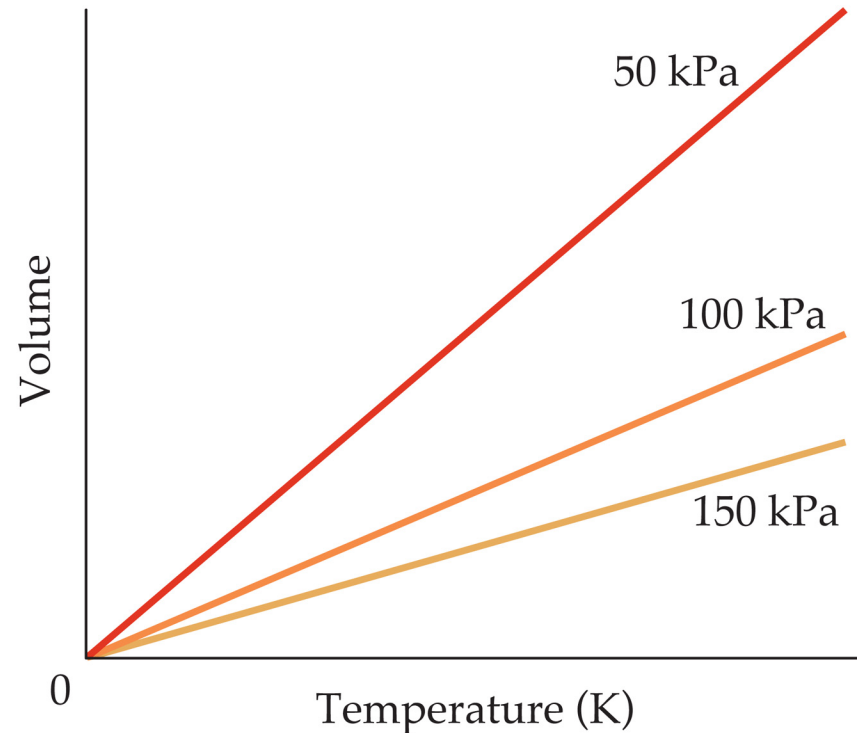
- Hold N , P constant and see how V , T vary: find

$$V = (\text{const})T$$

(constant N , P)

Charles & Gay-Lussac Law

For different P 's we get a set of linear plots



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Example: Volume of an ideal gas

- What volume is occupied by 1.00 mol of an ideal gas if it is at $T = 0.00^\circ\text{C}$ and $P = 1.00 \text{ atm}$?

$$PV = nRT \quad \text{so}$$

$$V = \frac{nRT}{P}$$

$$= \frac{(1.00 \text{ mol})[0.08206 \text{ L} \cdot \text{atm}/(\text{mol} \cdot \text{K})](273.15 \text{ K})}{(1.00 \text{ atm})}$$

$$= 22.41 \text{ L}$$

- If we increase the V available, with same T : P must drop
- If we increase the T , with V kept the same: P must rise
- **Standard Temperature and Pressure (STP) = 0°C , 1 atm**
 - At STP, one mole of any ideal gas occupies 22.4 liters

Example: heating and compressing a gas

- An ideal gas initially has a volume = 2.00 L, temperature = 30.0°C, and pressure = 1.00 atm.
- The gas is **heated** to 60.0°C and **compressed** to a volume of 1.50 L – what is its new pressure?

$$\frac{P_1 V_1}{T_1} = \frac{P_2 V_2}{T_2} \quad \text{so} \quad P_2 = P_1 \frac{V_1 T_2}{V_2 T_1} = (1.00 \text{ atm}) \frac{(2.0 \text{ L})(60.0^\circ\text{C} + 273.15^\circ\text{C})}{(1.5 \text{ L})(30.0^\circ\text{C} + 273.15^\circ\text{C})}$$
$$= 1.47 \text{ atm}$$

- Notice: we **must** use **Kelvin** temperatures when applying ideal gas laws – what would result have been if we use the ratio (60/30)?

Quiz 5

- Two containers with equal V and P each hold samples of the same ideal gas. Container A has twice as many molecules as container B.
- Which is the correct statement about the absolute temperatures in containers A and B, respectively?

A. $T_A = T_B$

B. $T_A = 2 T_B$

C. $T_A = (1/2)T_B$

D. $T_A = (1/4) T_B$

E. $T_A = (1/\sqrt{2})T_B$

Quiz 5

- Two containers with equal V and P each hold samples of the same ideal gas. Container A has twice as many molecules as container B.
- Which is the correct statement about the absolute temperatures in containers A and B, respectively?

A. $T_A = T_B$

B. $T_A = 2 T_B$

C. $T_A = (1/2)T_B$ $PV = nRT$ so $T = (PV / nR) \propto (1 / n)$

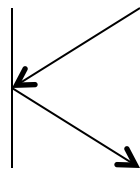
D. $T_A = (1/4) T_B$

E. $T_A = (1/\sqrt{2})T_B$

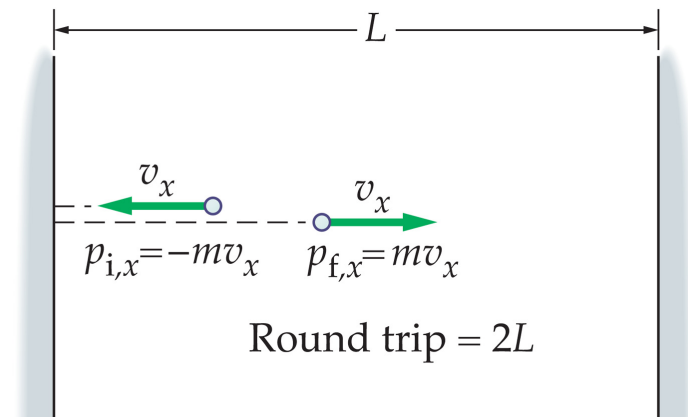
Relating gas laws to molecular motion

- P, V, T are macroscopic quantities
 - Human-scale quantities, measurable on a table-top
- Molecular motion (x, v vs t) = microscopic quantities
- Kinetic theory of gases: connect micro to macro
 - Model for ideal gas
 - N is large, molecules are identical point-particles
 - Molecules move randomly
 - No inelastic interactions: collisions are always elastic
 - Recall: elastic means no loss of KE due to collision

Elastic collision with wall means momentum (so, \mathbf{v}) component perpendicular to wall gets reversed



Speed unchanged
Vertical \mathbf{v} unchanged
Horizontal \mathbf{v} reversed



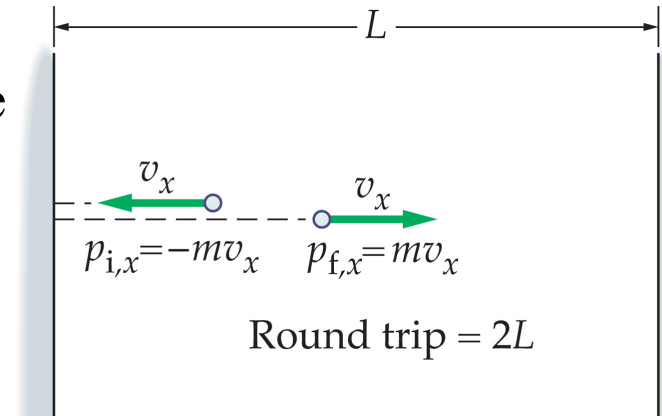
Calculate the pressure of a gas

Change in horizontal momentum of molecule

$$\Delta p_x = p_{x,f} - p_{x,i} = mv_x - (-mv_x) = 2mv_x$$

Change is due to force exerted by wall:

$$F\Delta t = \Delta p_x, \quad F_{ON\ WALL} = -F_{BY\ WALL}$$



Average force exerted on wall by one molecule $F_{AVG} = \frac{\Delta p_x}{\Delta t}$

where Δt = time between collisions = round-trip time

$$\Delta t = 2L / v_x \rightarrow F_{AVG} = \frac{2mv_x}{2L / v_x} = \frac{mv_x^2}{L}$$

Assume symmetrical container (LxLxL): (doesn't matter in the end)

$$P_{AVG} = \frac{F_{AVG}}{A} = \frac{1}{L^2} \left(\frac{mv_x^2}{L} \right) = \frac{mv_x^2}{V} \rightarrow \text{Adding up all molecules, } PV = N m \left(v_x^2 \right)_{AVG}$$

Defining temperature (again): molecular scale

- Now we can connect macro to micro:

$$PV = NkT = 2N\left(\frac{1}{2}mv_x^2\right)_{\text{av}} \rightarrow \left(\frac{1}{2}mv_x^2\right)_{\text{av}} = \frac{1}{2}kT$$

Nothing special about the x-direction: **random motion** means

$$\left(v_x^2\right)_{\text{av}} = \left(v_y^2\right)_{\text{av}} = \left(v_z^2\right)_{\text{av}} \quad \text{and} \quad \left(v^2\right)_{\text{av}} = \left(v_x^2\right)_{\text{av}} + \left(v_y^2\right)_{\text{av}} + \left(v_z^2\right)_{\text{av}} = 3\left(v_x^2\right)_{\text{av}}$$

(because **random** **v** components are **independent** of one another)

The average translational kinetic energy of the molecules is:

$$K_{\text{translational av}} = \left(\frac{1}{2}mv^2\right)_{\text{av}} = \frac{3}{2}kT \quad \text{per molecule}$$

Deep and fundamental !
Avg KE of gas molecule is proportional to T, with Boltzmann constant as the factor

$$K_{\text{trans}} = N\left(\frac{1}{2}mv^2\right)_{\text{av}} = \frac{3}{2}NkT = \frac{3}{2}nRT$$

Root-mean-square (RMS) - useful avg where quantity-squared is what matters:

$$\left(v^2\right)_{\text{av}} = \frac{3kT}{m_{\text{molecule}}} = \frac{3N_A kT}{N_A m_{\text{molecule}}} = \frac{3RT}{M_{\text{MOLE}}} \quad \text{and} \quad v_{\text{RMS}} = \sqrt{\left(v^2\right)_{\text{av}}} = \sqrt{\frac{3RT}{M_{\text{MOLE}}}}$$

Example: RMS speed of gas molecules

RMS means: take each molecule's speed and square it, **then** find the average of those numbers, and **THEN** take the square root.

In practice: we find the statistical speed **distribution** of the molecules, and use that to estimate RMS speed

Oxygen gas (O_2) has a molar mass* M of about 32.0 g/mol, and hydrogen gas (H_2) has a molar mass of about 2.00 g/mol. Assuming ideal-gas behavior, what is:

(a) the RMS speed of an oxygen molecule when the temperature is 300K (27°C), and

(b) RMS speed of a hydrogen molecule at the same temperature

Note: Walker says
“molecular mass” for molar mass – confusing.
 M_X = grams in 1 mole of X,
 m_X = mass (in kg) of one X molecule

$$v_{O_2 \text{ RMS}} = \sqrt{\frac{3RT}{M_O}} = \sqrt{\frac{3(8.314 \text{ J/mol} \cdot \text{K})(300 \text{ K})}{(0.0320 \text{ kg/mol})}} = 485 \text{ m/s}$$

$$v_{H_2 \text{ RMS}} = \sqrt{\frac{3RT}{M_H}} = \sqrt{\frac{3(8.314 \text{ J/mol} \cdot \text{K})(300 \text{ K})}{(0.0020 \text{ kg/mol})}} = 1,934 \text{ m/s}$$

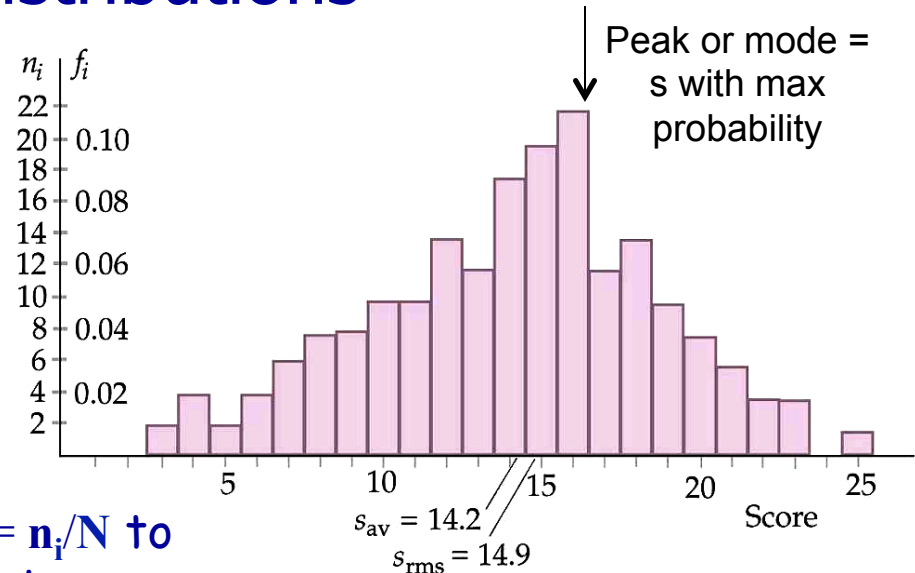
Probability Distributions

We give a 25 point quiz to N students, and plot the results as a **histogram**, showing the number n_i of students, or fraction $f_i = n_i/N$ of students, for each possible score vs. score, from 0 to 25.

Such plots represent **distributions**.

For reasonably large N , we can use $f_i = n_i/N$ to estimate the probability that a randomly selected student received a score s_i .

Notice, the fractions will add to 1 for all possible scores, so that $\sum f_i = 1$. In that case the histogram represents a **normalized distribution function**. We have the following relations:



It's not useful for class grades, but we could also calculate the average **squared score**:

$$\sum_i n_i = N \quad \sum_i f_i = 1$$

$$s_{\text{av}} = \frac{1}{N} \sum_i n_i s_i = \sum_i f_i s_i$$

$$s_{\text{av}}^2 = \frac{1}{N} \sum_i n_i s_i^2 = \sum_i f_i s_i^2$$

$$s_{\text{RMS}} = \sqrt{s_{\text{av}}^2} = \sqrt{\sum_i f_i s_i^2}$$