Name \_\_\_\_

11.30 am Wed 1 March 06

Electrodynamics, Physics 321 Winter 2006

Second midterm Instructor: David Cobden

Do not turn this page until I say 'go' at 11.30. You have 50 minutes. Hand your exam to me before I leave the room at 12.25.

This exam contains 100 points. Be sure to attempt all the questions.

Please write your name on every page and your SID on the first page.

Write all your working on these question sheets. Use this front page for extra working. It is important to show your calculation or derivation. You probably won't get full marks just for stating the correct answer if you don't show how you get it.

Watch the blackboard/overhead for corrections or clarifications during the exam.

This is a closed book exam. No books, notes or calculators allowed.

$$\int_{-1}^{1} P_{l}(x)P_{m}(x)dx = \frac{2}{2l+1}\delta_{mn} \qquad P_{0}(x) = 1 \qquad P_{1}(x) = x \qquad P_{2}(x) = (3x^{2}-1)/2 \qquad P_{3}(x) = (5x^{3}-3x)/2$$
$$\nabla\left(\frac{\mathbf{p}.\hat{\mathbf{r}}}{r^{2}}\right) = \frac{3(\mathbf{p}.\hat{\mathbf{r}})\hat{\mathbf{r}}-\mathbf{p}}{r^{3}}$$



<sup>&</sup>quot;IT'S AN EXCELLENT PROOF, BUT IT LACKS WARMTH AND FEELING,"

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1. [10] State the uniqueness theorem for Laplace's equation as carefully as you can (the general one we proved in class, not one of the special ones in Griffiths). Specify the types of boundary conditions that are sufficient (you don't need to remember their names).

2. [10] A conducting sphere of radius R carries a positive charge Q. A particle with positive charge q is placed somewhere near the sphere. Show that the particle is repelled from the sphere when it is far away and attracted when it is close.

3. [10] Find an implicit equation for the distance  $z_c$  (between particle and center of sphere) at which the force between particle and sphere vanishes. Simplify the equation but do not try to solve for  $z_c$ .

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4. [10] A spherical cavity of radius *R* has an azimuthally symmetric potential  $V_0 \sin \theta$  maintained over its inner surface, where  $\theta$  is the usual polar angle. Write down the appropriate general eigenfunction expansion for  $V(r, \theta)$  in the cavity.

5. [20] Identify all coefficients in the expansion which are zero (don't forget to account for symmetry of the Legendre polynomials), and evaluate the first nonzero coefficient.

6. [10] Now consider the same cavity, with the same potential on its surface, but with a point charge q located at its center. What is the difference in the eigenfunction expansion for this case compared with the situation with no point charge?

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7. [10] Show that the dipole moment of a an object with a rigid charge distribution is independent of choice of origin only if the total charge is zero.

8. [10] A small simple dipole **p** is located a distance *d* from and parallel to the flat surface of a conductor, as indicated below. Using the image charge method (sketch as required on the diagram below), find an expression for the electric potential  $V(\mathbf{r})$  outside the conductor (not valid very close to the dipole).

9. [10] Sketch the electric field lines (solid) and equipotentials (dashed).

z = d -

- **p** - →+

## z = 0 - conducto

10. [5 extra on top of 100] Find an expression for the charge density on the surface of the conductor.