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8.20 am, Friday May 4, 2007

Electrodynamics, Physics 323 Spring 2007 **First midterm** Instructor: David Cobden

Do not turn this page until the buzzer goes at 8.20. You must hand your exam to me before I leave the room at 9.25.

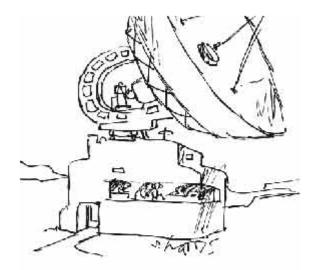
Attempt all the questions.

Please write your name on every page and your SID on the first page.

Write all your working on these question sheets. Use this front page for extra working. It is important to show your calculation or derivation. Some of the marks are given for showing clear and accurate working and reasoning.

Watch the blackboard for corrections or clarifications during the exam.

This is a closed book exam. No books, notes or calculators allowed.



<sup>&</sup>quot;HOLD ON TO YOUR HATS. WEIZE PICKING UP ANOTHER BIG BANG."

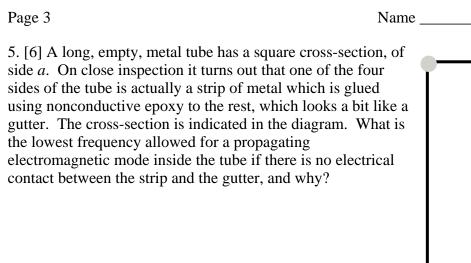
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1. [10] State Maxwell's equations in vacuum.

2. [10] For a monochromatic plane wave, show that **E**, **B** and **k** are mutually perpendicular.

3. [3] A certain laser beam can be treated as a monochromatic plane wave with  $\mathbf{k} = k\hat{\mathbf{z}}$  and electric field amplitude  $\mathbf{E}_0 = E(\hat{\mathbf{x}} + 2i\hat{\mathbf{y}})$ . What kind of polarization is this?

4. [12] The laser is reflected normally from a perfectly conducting surface. Find the average momentum density in the incident wave and hence the pressure exerted on the surface.



6. [10] At a frequency low enough that only this one mode can propagate, *sketch on the diagram* the electric and magnetic field lines inside at some instant in time. Remember to take into account the boundary conditions on **E** and **B**. Also, what can you say about the field components along the tube?

7. [5] Suppose that somewhere along the tube the strip actually makes electrical contact with the gutter. What effect will this have on propagation at this low frequency, and why?

8. [5] Is it still possible for the tube to carry waves at higher frequencies, and why?

9. [12] By considering the phase variation of incident and transmitted waves over a planar interface between media with different refractive indices, derive Snell's law of refraction.

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10. [10] By dimensional analysis, or otherwise, find the form of the relationship between the square of the plasma frequency  $\omega_p^2$  and the electron concentration *N*, the charge  $e = 1.6 \times 10^{-19}$  C, the electron mass  $m = 10^{-30}$  kg, and  $\varepsilon_0 \approx 10^{-11}$  Fm<sup>-1</sup>.

11. [10] The ionosphere carries a free electron density  $N \approx 10^{11} \text{ m}^{-3}$ . *Estimate* the shortest wavelength of radio waves that can be channeled around the earth by reflection from the ionosphere.

12. [12] By considering the **E** and **B** fields, determine what distribution of charge and/or current generates the following potentials *in cylindrical coordinates*:

 $\mathbf{A} = \frac{\mu_0 I \hat{\mathbf{z}} \ln(r/b)}{2\pi} - \frac{Q \hat{\mathbf{r}} t}{r}, \quad V = Q \ln(r/a).$