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Section [AA] (Natalie), [AB] (Natalie), [AC] (Ryan), [AD] (Ryan), [AE] (Kelly), [AE] (Kelly)

The following problems are worth a total of 100 points. The exam is open book and open note, but not open Google. To look up probabilities, you can also either use the pdf of the statistics table:

http://courses.washington.edu/psy315/pdf/StatsTables.pdf

or the Excel file:

http://courses.washington.edu/psy315/excel\_files/StatTables.xlsx

For answers that require calculations, please show your work. You may use R, but be sure to show your work for partial credit. Give all answers **rounded to 4 decimal places**.

**Problem 1 (54 pts)** From our survey, the distribution of your Father's ages has a mean of 52.6 and a standard deviation of 5, and that the distribution of your Mother's ages has a mean of 51 and a standard deviation of 5.13. The ages of your mothers and fathers are strongly correlated with a value of r = 0.79.

Here's a scatterplot of the data:



a) (10 pts) Calculate the slope of the regression line that predicts your Mother's age from your Father's age.

b) (10 pts) Calculate the equation of the regression line that predicts your Mother's age from your Father's age. Write the answer in slope-intercept form.

c) (5 pts) Draw the regression line on the scatterplot on the first page.

d) (5 pts) What is the standard error of the estimate  $(s_{yx})$ ?

e) (5 pts) What is the proportion of the variance in the Mother's age that can be explained by the Father's age?

f) (5 pts) Suppose a new student enters the class, and her father is 56 years old. Based on the regression line, what is the predicted age of this student's mother?

g) (2 pts) Plot this student's father's age and the predicted mother's age as a point on the regression line on the first page.

h) (2 pts) Suppose that this student, whose father is 56 years old, has a mother is actually 51 years old. Plot this as a point on the scatterplot on the first page.

j) (10 pts) Assuming homoscedasticity, use the regression line and the standard error of the estimate to determine the probability that a student with father that is 56 years old will have a mother that is 51 years old or younger.

**Problem 2a (10 pts)** Suppose the probability that the proportion of left handed people in the population is 0.1. What is the probability a random sample of 5 people will have 1 or more left handers?

**Problem 2b (10 pts)** Again, assuming that the proportion of left-handers in the population is 0.1. Use the normal approximation to the binomial to estimate the probability that a sample of 36 people will have 6 or more left handers.

Problem 3 (6 pts) Choose the best answer for each of the following multiple choice questions.

a) (2 pts) Suppose heights of sisters are correlated with r=0.35. If you pick out a sister because she is taller than the average of the population then the other sister will be, on average,

- A) taller than the first sister
- B) taller than the average of the population
- C) less tall than the first sister
- **D**) as tall as the first sister
- E) less tall than the average of the population
- F) B and C

b) (2 pts) When is the standard error of the estimate equal to the standard deviation of y?

- A) When the coefficient of non-determination is zero.
- **B**) When the correlation is zero.
- C) When the coefficient of non-determiniation is one.
- **D**) E and A
- **E)** When the correlation is 1 or -1.
- F) B and C

c) (2 pts) If you increase your sample size from 9 to 81, the standard error of the mean is

- A) multiplied by 3
- **B**) multiplied by 9
- C) divided by 9
- D) divided by 3

**Problem 4 (20 pts)** Suppose that you know that the age of the population of UW psychology students is normally distributed with a mean of 23.3 and a standard deviation of 3.45 years. Consider the mean age from a sample of 100 students.

a) (10 pts) What is the mean and standard deviation of the population that this mean is drawn from?

b) (10 pts) What is the probability that a mean drawn from a sample of 100 students will exceed 23.8 years?