

The following problems are worth 2 points each. You can get a total of 10 points.

4. Why is it not possible to create a transfer function that represents the exact behavior of a pendulum over the interval $-2\pi < \theta < 2\pi$?

Transfer functions are always linear, but the exact pendulum equation is non-linear.

5. What is the time-domain equation that is equivalent to the following frequency-domain equation?

$$Y(s) = \frac{2}{s+3} \cdot \frac{7}{s^2+49} \quad \text{is equivalent to} \quad y(t) = e^{-3t} u(t) * \sin(7t) u(t) \quad \text{where } * \text{ stands for}$$

convolution. You could get the $\sin(7t)$ from the given Laplace transform of a decaying sine wave, setting the decay constant a to zero.

6. What is the purpose of a Schmitt trigger?

A Schmitt trigger acts as a comparator with hysteresis. It saturates high as it passes one threshold, and saturates low as it passes a lower threshold. Its purpose is to reduce the effect of noise on the comparator's function.

7. What is the approximate doubling time of fibroblasts?

- a) 20 minutes
- b) 2 hours
- c) 20 hours
- d) 2 days

8. Which of the following probably does NOT describe a fibroblast that is rounded up (spherical)?

- a) Dead
- b) Dividing
- c) Freshly added to medium
- d) Moving itself around the dish

9. In a phase portrait, a stable spiral point...

- a) Always goes clockwise inward
- b) Can spiral inward or outward
- c) Always goes inward but either clockwise or counterclockwise
- d) Always goes counterclockwise inward

10. What does DMEM stand for?

Dulbecco's Modified Eagle's Medium (solution that mammalian cells grow in)

Other interesting answers:

Dull microscopes emit misguidance
Dilapidated Materials Exasperate Mentors
Differential MATLAB Expunges Matrices
Differential Multiple Equation Model
Don't make Everyone Mad
Definitely Made Extreme Mistakes

11. Propose a way to implement a PID controller $G(s)$ using some or all of the following components, but no software. The input is a voltage representing the error signal, and the output is a voltage. Capacitor, inductor, LED, resistor, voltage-controlled current source (VCCS), zener diode. *You may also use an op-amp.*

One option: The VCCS converts the error voltage to a current. This current is passed through R, L, and C in series. The total impedance of the series RLC is

$$\frac{1}{Cs} + R + Ls$$

which has the same form as the sum of the three PID terms. We set $1/C = K_i$, $R = K_p$, and $L = K_s$. The voltage is then taken across all three components, that is to say at the output of the VCCS. It is also a good idea to include an op-amp at the output to decouple $G(s)$ from the next stage in the system.

Equations

$$\frac{d}{dt} \sin(x) = \cos(x)$$

$$e^{-at} \sin(\omega t) \Leftrightarrow \frac{\omega}{(s+a)^2 + \omega^2}$$

$$e^{-at} \cos(\omega t) \Leftrightarrow \frac{s+a}{(s+a)^2 + \omega^2}$$

In the following definitions, ζ is defined in the following transfer function:

$$H(s) = \frac{1}{s^2 + 2\zeta\omega_n s + \omega_n^2}$$

Overshoot, as fraction of step response $M_{peak} = e^{-\pi\zeta / \sqrt{1-\zeta^2}}$

$$\text{Settling time } t_s = \frac{4.6}{\zeta\omega_n}$$