

## Propositional Logic

Prove the following three Boolean equations:

(Note: ! means NOT ( $\neg$ ); & means AND ( $\wedge$ ); and | means OR ( $\vee$ ))

- $\neg A \& B \mid A \& \neg B = (\neg A \mid \neg B) \& (A \mid B)$
- $(A \& B \mid C) \& B = A \& B \& \neg C \mid \neg A \& B \& C \mid A \& B \& C$
- $A \& B \mid A \& B \& C \mid A \& \neg B = A$

For each pair of propositions P and Q, state whether  $P \equiv Q$ .

(Note: ! means NOT ( $\neg$ ); & means AND ( $\wedge$ ); and | means OR ( $\vee$ ))

- $P = p, Q = p \mid q$
- $P = p \rightarrow q, Q = \neg p \mid q$
- $P = p \rightarrow q, Q = \neg q \rightarrow \neg p$
- $P = (p \rightarrow q) \& (q \rightarrow r), Q = p \rightarrow r$
- $P = (p \rightarrow q) \rightarrow r, Q = p \rightarrow (q \rightarrow r)$

Expand the following Boolean equations with De Morgan's Laws

- $f = \neg(A \mid B) \& \neg(A \& B \& C) \& \neg(\neg A \& C)$
- $f = \neg((A \& B \mid \neg B \& C) \mid (B \& \neg C \mid \neg A \& B))$
- $f = \neg((A \& B \mid \neg B \& C) \& (A \& C \mid \neg A \& \neg C))$

<b>Date:</b>	<b>Group #:</b>
<b>Group Members:</b> (Circle the group representative name)	