



Anomaly Detection

Some slides taken or adapted from:

“Anomaly Detection: A Tutorial”

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Anomaly detection

Anomalies and **outliers**
are essentially
the same thing:

objects that are different from most other objects

The techniques used for detection are the same.

Anomaly detection

- Historically, the field of statistics tried to find and remove outliers as a way to improve analyses.
- There are now many fields where the outliers / anomalies are the objects of greatest interest.
 - The rare events may be the ones with the greatest impact, and often in a negative way.

Causes of anomalies

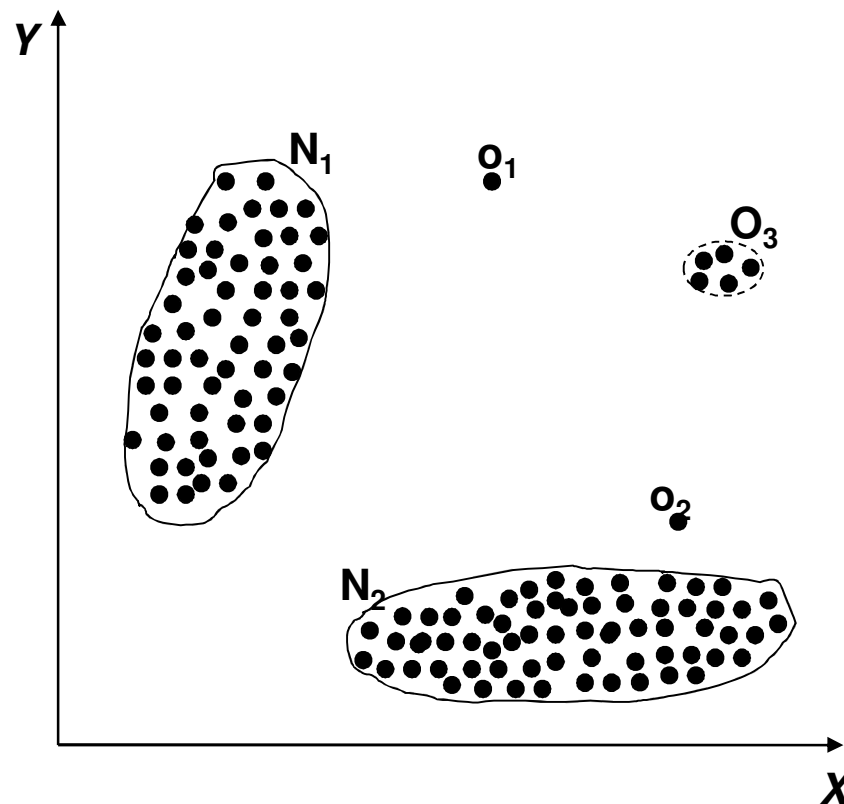
- Data from different class of object or underlying mechanism
 - disease vs. non-disease
 - fraud vs. not fraud
- Natural variation
 - tails on a Gaussian distribution
- Data measurement and collection errors

Structure of anomalies

- Point anomalies
- Contextual anomalies
- Collective anomalies

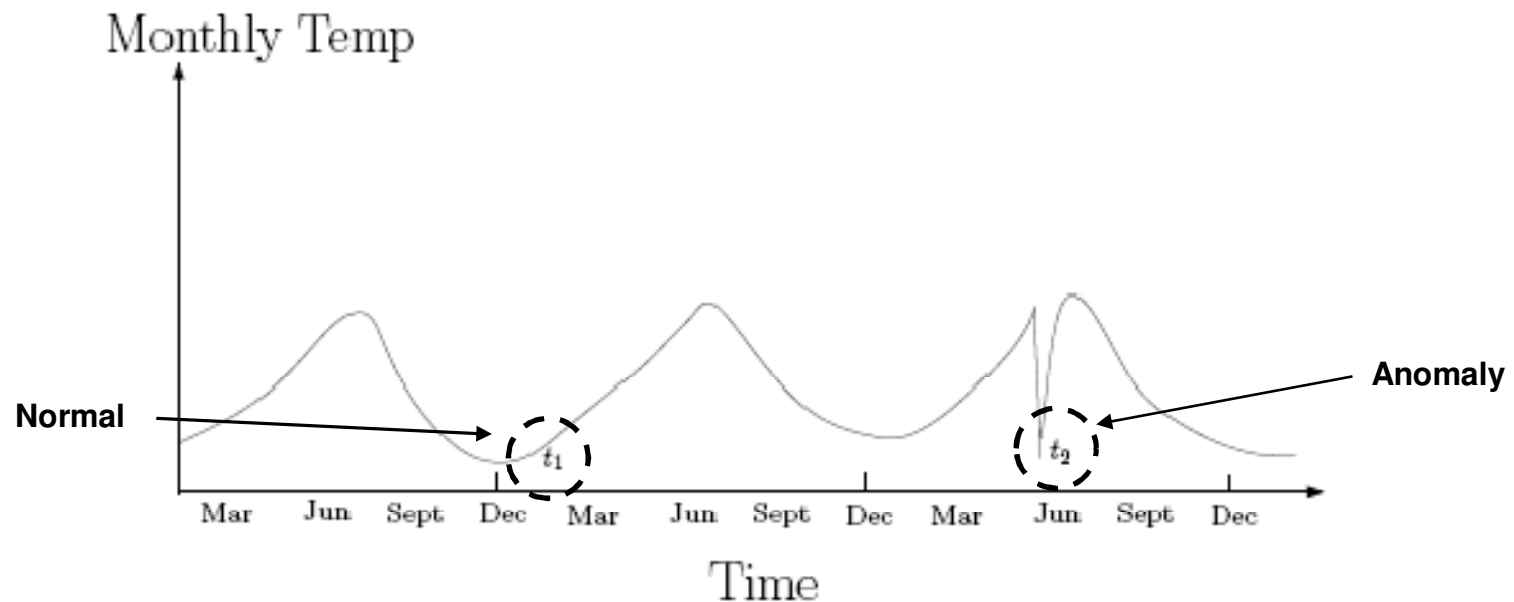
Point anomalies

- An individual data instance is anomalous with respect to the data



Contextual anomalies

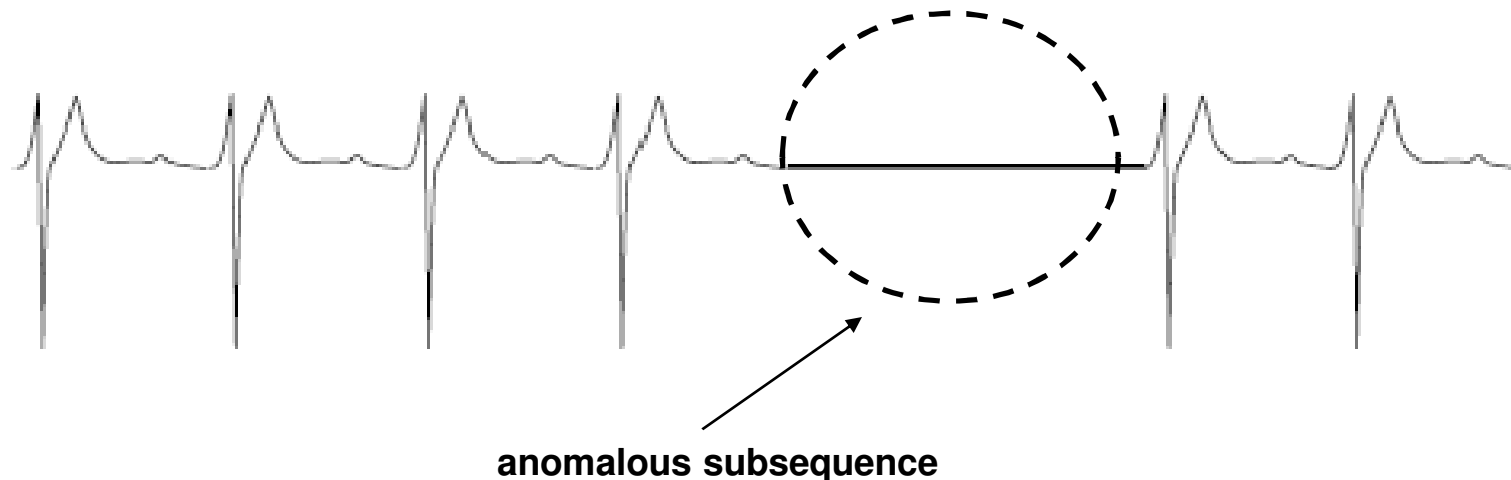
- An individual data instance is anomalous within a context
- Requires a notion of context
- Also referred to as conditional anomalies *



* Song, et al, "Conditional Anomaly Detection", IEEE Transactions on Data and Knowledge Engineering, 2006.

Collective anomalies

- A collection of related data instances is anomalous
- Requires a relationship among data instances
 - Sequential data
 - Spatial data
 - Graph data
- The individual instances within a collective anomaly are not anomalous by themselves



Applications of anomaly detection

- Network intrusion
- Insurance / credit card fraud
- Healthcare informatics / medical diagnostics
- Industrial damage detection
- Image processing / video surveillance
- Novel topic detection in text mining
- ...

Intrusion detection

- Intrusion detection
 - Monitor events occurring in a computer system or network and analyze them for intrusions
 - Intrusions defined as attempts to bypass the security mechanisms of a computer or network
- Challenges
 - Traditional intrusion detection systems are based on signatures of known attacks and cannot detect emerging cyber threats
 - Substantial latency in deployment of newly created signatures across the computer system
- Anomaly detection can alleviate these limitations



Fraud detection

- Detection of criminal activities occurring in commercial organizations.
- Malicious users might be:
 - Employees
 - Actual customers
 - Someone posing as a customer (identity theft)
- Types of fraud
 - Credit card fraud
 - Insurance claim fraud
 - Mobile / cell phone fraud
 - Insider trading
- Challenges
 - Fast and accurate real-time detection
 - Misclassification cost is very high



Healthcare informatics

- Detect anomalous patient records
 - Indicate disease outbreaks, instrumentation errors, etc.
- Key challenges
 - Only normal labels available
 - Misclassification cost is very high
 - Data can be complex: spatio-temporal



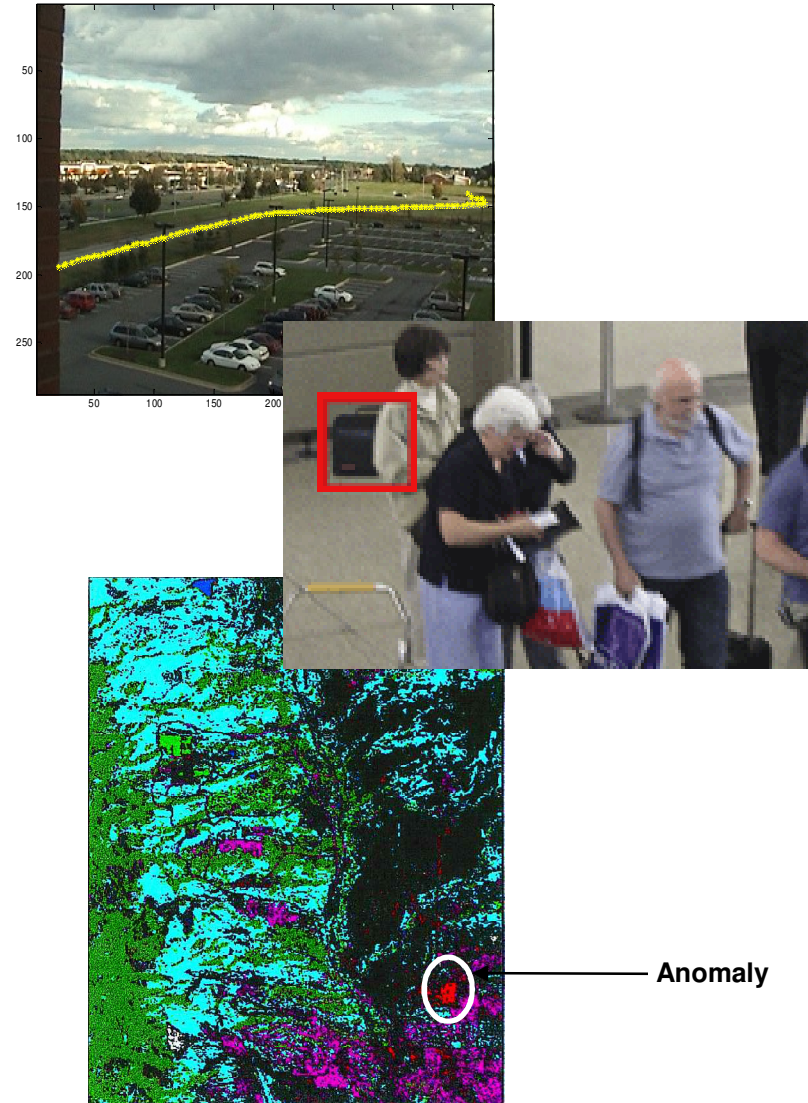
Industrial damage detection

- Detect faults and failures in complex industrial systems, structural damages, intrusions in electronic security systems, suspicious events in video surveillance, abnormal energy consumption, etc.
 - Example: aircraft safety
 - ◆ anomalous aircraft (engine) / fleet usage
 - ◆ anomalies in engine combustion data
 - ◆ total aircraft health and usage management
- Key challenges
 - Data is extremely large, noisy, and unlabelled
 - Most of applications exhibit temporal behavior
 - Detected anomalous events typically require immediate intervention



Image processing

- Detecting outliers in a image monitored over time
- Detecting anomalous regions within an image
- Used in
 - mammography image analysis
 - video surveillance
 - satellite image analysis
- Key Challenges
 - Detecting collective anomalies
 - Data sets are very large



Use of data labels in anomaly detection

- Supervised anomaly detection
 - Labels available for both normal data and anomalies
 - Similar to classification with high class imbalance
- Semi-supervised anomaly detection
 - Labels available only for normal data
- Unsupervised anomaly detection
 - No labels assumed
 - Based on the assumption that anomalies are very rare compared to normal data

Output of anomaly detection

- Label
 - Each test instance is given a *normal* or *anomaly* label
 - Typical output of classification-based approaches
- Score
 - Each test instance is assigned an anomaly score
 - ◆ allows outputs to be ranked
 - ◆ requires an additional threshold parameter

Variants of anomaly detection problem

- Given a dataset D , find all the data points $\mathbf{x} \in D$ with anomaly scores greater than some threshold t .
- Given a dataset D , find all the data points $\mathbf{x} \in D$ having the top- n largest anomaly scores.
- Given a dataset D , containing mostly normal data points, and a test point \mathbf{x} , compute the anomaly score of \mathbf{x} with respect to D .

Unsupervised anomaly detection

- No labels available
- Based on assumption that anomalies are very rare compared to “normal” data
- General steps
 - Build a profile of “normal” behavior
 - ◆ summary statistics for overall population
 - ◆ model of multivariate data distribution
 - Use the “normal” profile to detect anomalies
 - ◆ anomalies are observations whose characteristics differ significantly from the normal profile

Techniques for anomaly detection

- Statistical
- Proximity-based
- Density-based
- Clustering-based

[following slides illustrate these techniques for unsupervised detection of point anomalies]

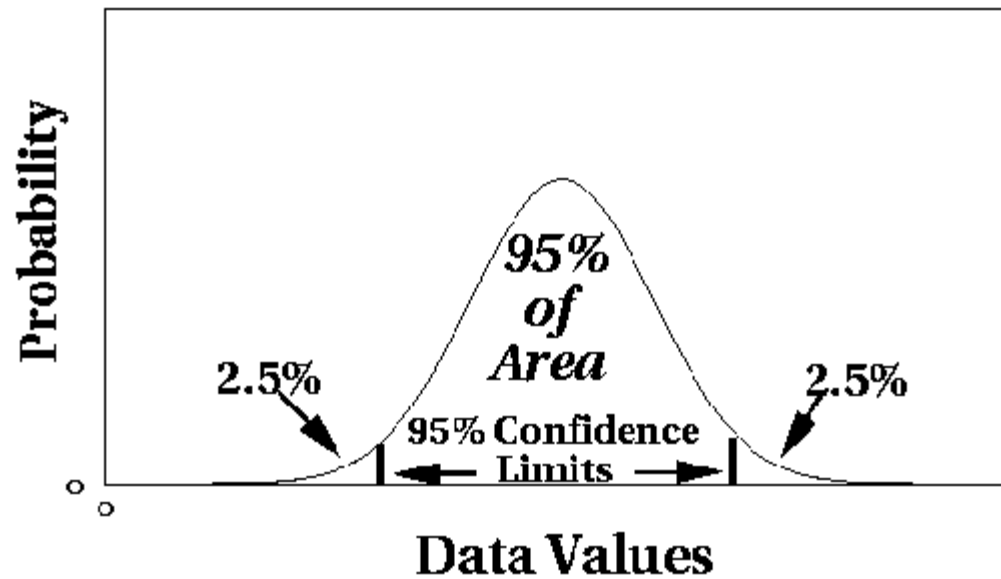
Statistical outlier detection

Outliers are objects that are fit poorly by a statistical model.

- Estimate a parametric model describing the distribution of the data
- Apply a statistical test that depends on
 - Properties of test instance
 - Parameters of model (e.g., mean, variance)
 - Confidence limit (related to number of expected outliers)

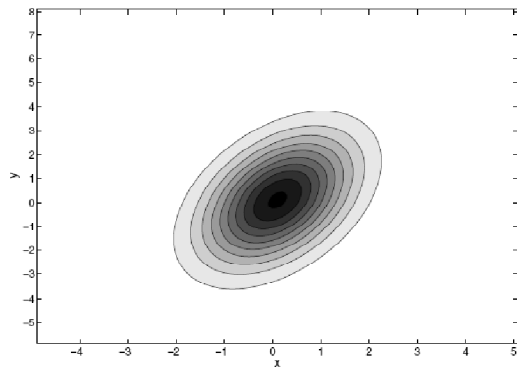
Statistical outlier detection

- Univariate Gaussian distribution
 - Outlier defined by $z\text{-score} > \text{threshold}$

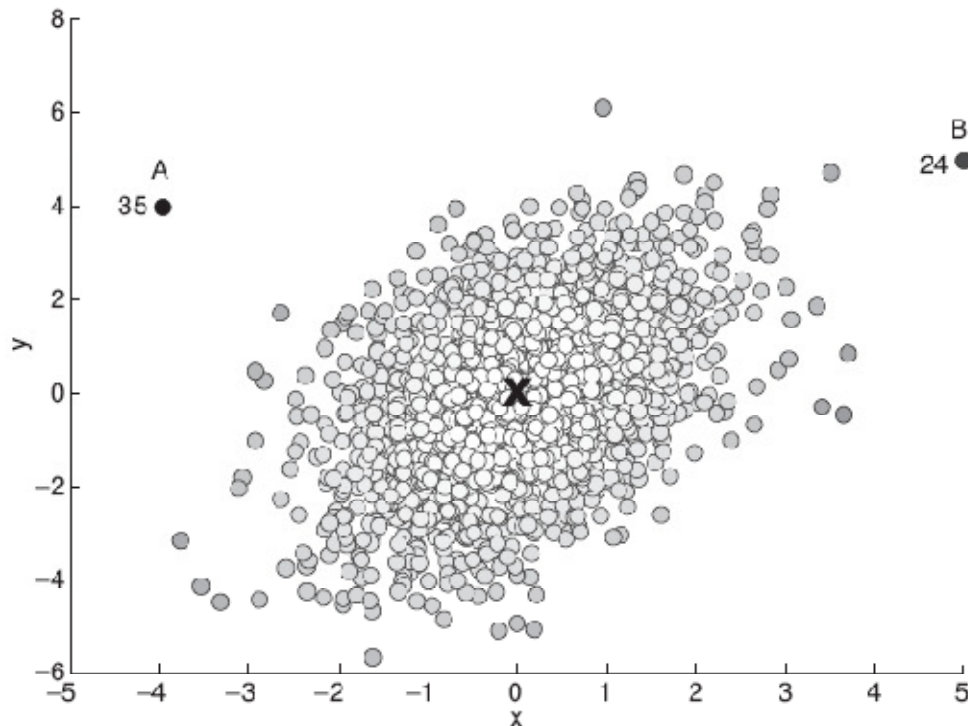


Statistical anomaly detection

- Multivariate Gaussian distribution
 - Outlier defined by Mahalanobis distance $>$ threshold



	Distance	
	Euclidean	Mahalanobis
A	5.7	35
B	7.1	24



Grubbs' test

- Detect outliers in univariate data
- Assume data comes from normal distribution
- Detects one outlier at a time, remove the outlier, and repeat
 - H_0 : There is no outlier in data
 - H_A : There is at least one outlier

- Grubbs' test statistic:
$$G = \frac{\max |X - \bar{X}|}{s}$$

- Reject H_0 if:

$$G > \frac{(N-1)}{\sqrt{N}} \sqrt{\frac{t^2_{(\alpha/N, N-2)}}{N-2 + t^2_{(\alpha/N, N-2)}}}$$

Likelihood approach

- Assume the dataset D contains samples from a mixture of two probability distributions:
 - M (majority distribution)
 - A (anomalous distribution)
- General approach:
 - Initially, assume all the data points belong to M
 - Let $L_t(D)$ be the log likelihood of D at time t
 - For each point x_t that belongs to M , move it to A
 - ◆ Let $L_{t+1}(D)$ be the new log likelihood.
 - ◆ Compute the difference, $\Delta = L_t(D) - L_{t+1}(D)$
 - ◆ If $\Delta > c$ (some threshold), then x_t is declared as an anomaly and moved permanently from M to A

Likelihood approach

- Data distribution, $D = (1 - \lambda) M + \lambda A$
- M is a probability distribution estimated from data
 - Can be based on any modeling method (naïve Bayes, maximum entropy, etc)
- A is initially assumed to be uniform distribution
- Likelihood at time t :

$$L_t(D) = \prod_{i=1}^N P_D(x_i) = \left((1 - \lambda)^{|M_t|} \prod_{x_i \in M_t} P_{M_t}(x_i) \right) \left(\lambda^{|A_t|} \prod_{x_i \in A_t} P_{A_t}(x_i) \right)$$

$$LL_t(D) = |M_t| \log(1 - \lambda) + \sum_{x_i \in M_t} \log P_{M_t}(x_i) + |A_t| \log \lambda + \sum_{x_i \in A_t} \log P_{A_t}(x_i)$$

Statistical outlier detection

- Pros

- Statistical tests are well-understood and well-validated.
- Quantitative measure of degree to which object is an outlier.

- Cons

- Data may be hard to model parametrically.
 - ◆ multiple modes
 - ◆ variable density
- In high dimensions, data may be insufficient to estimate true distribution.

Proximity-based outlier detection

Outliers are objects far away from other objects.

- Common approach:
 - Outlier score is distance to k^{th} nearest neighbor.
 - Score sensitive to choice of k .

Proximity-based outlier detection

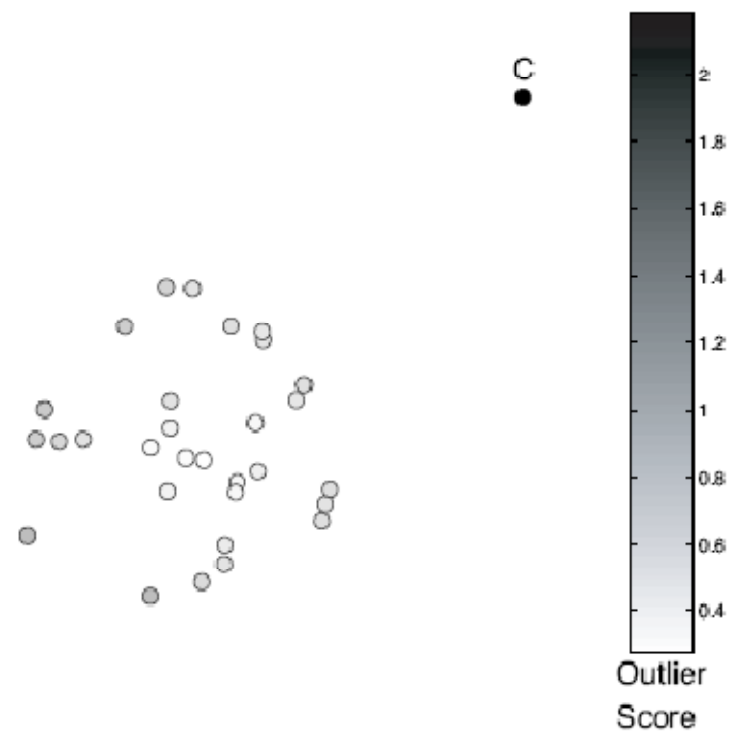


Figure 10.4. Outlier score based on the distance to fifth nearest neighbor.

Proximity-based outlier detection

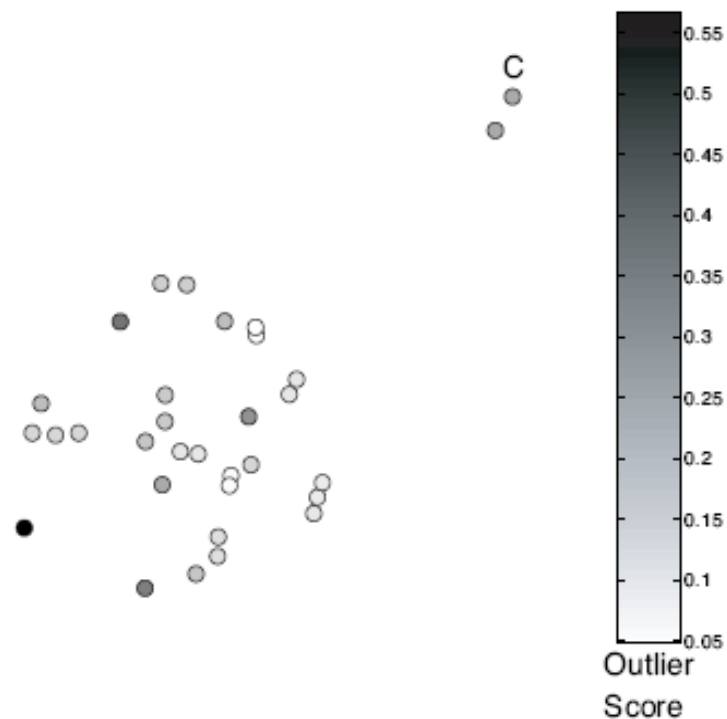


Figure 10.5. Outlier score based on the distance to the first nearest neighbor. Nearby outliers have low outlier scores.

Proximity-based outlier detection

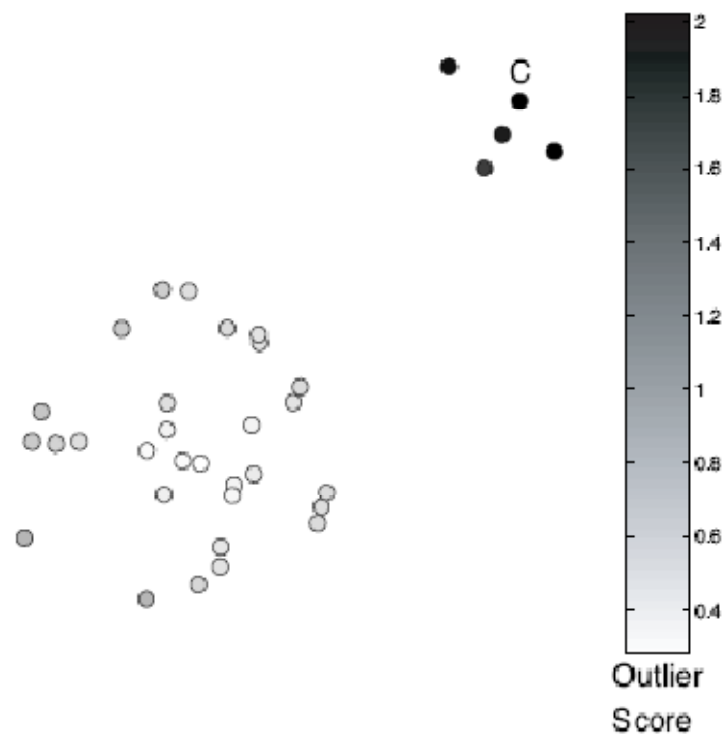


Figure 10.6. Outlier score based on distance to the fifth nearest neighbor. A small cluster becomes an outlier.

Proximity-based outlier detection

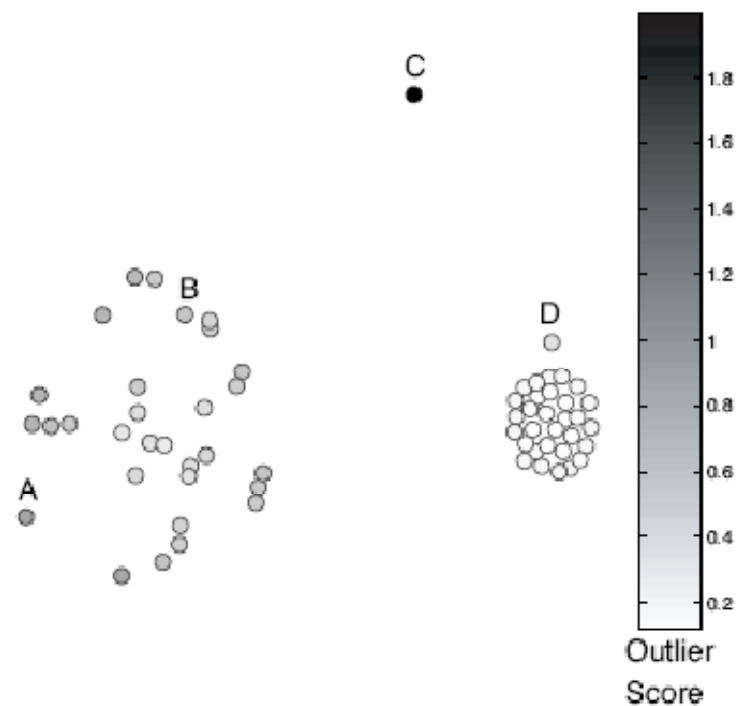


Figure 10.7. Outlier score based on the distance to the fifth nearest neighbor. Clusters of differing density.

Proximity-based outlier detection

- Pros

- Easier to define a proximity measure for a dataset than determine its statistical distribution.
- Quantitative measure of degree to which object is an outlier.
- Deals naturally with multiple modes.

- Cons

- $O(n^2)$ complexity.
- Score sensitive to choice of k .
- Does not work well if data has widely variable density.

Density-based outlier detection

Outliers are objects in regions of **low density**.

- Outlier score is inverse of density around object.
- Scores usually based on proximities.
- Example scores:
 - Reciprocal of average distance to k nearest neighbors:

$$\text{density}(\mathbf{x}, k) = \left(\frac{1}{k} \sum_{\mathbf{y} \in N(\mathbf{x}, k)} \text{distance}(\mathbf{x}, \mathbf{y}) \right)^{-1}$$

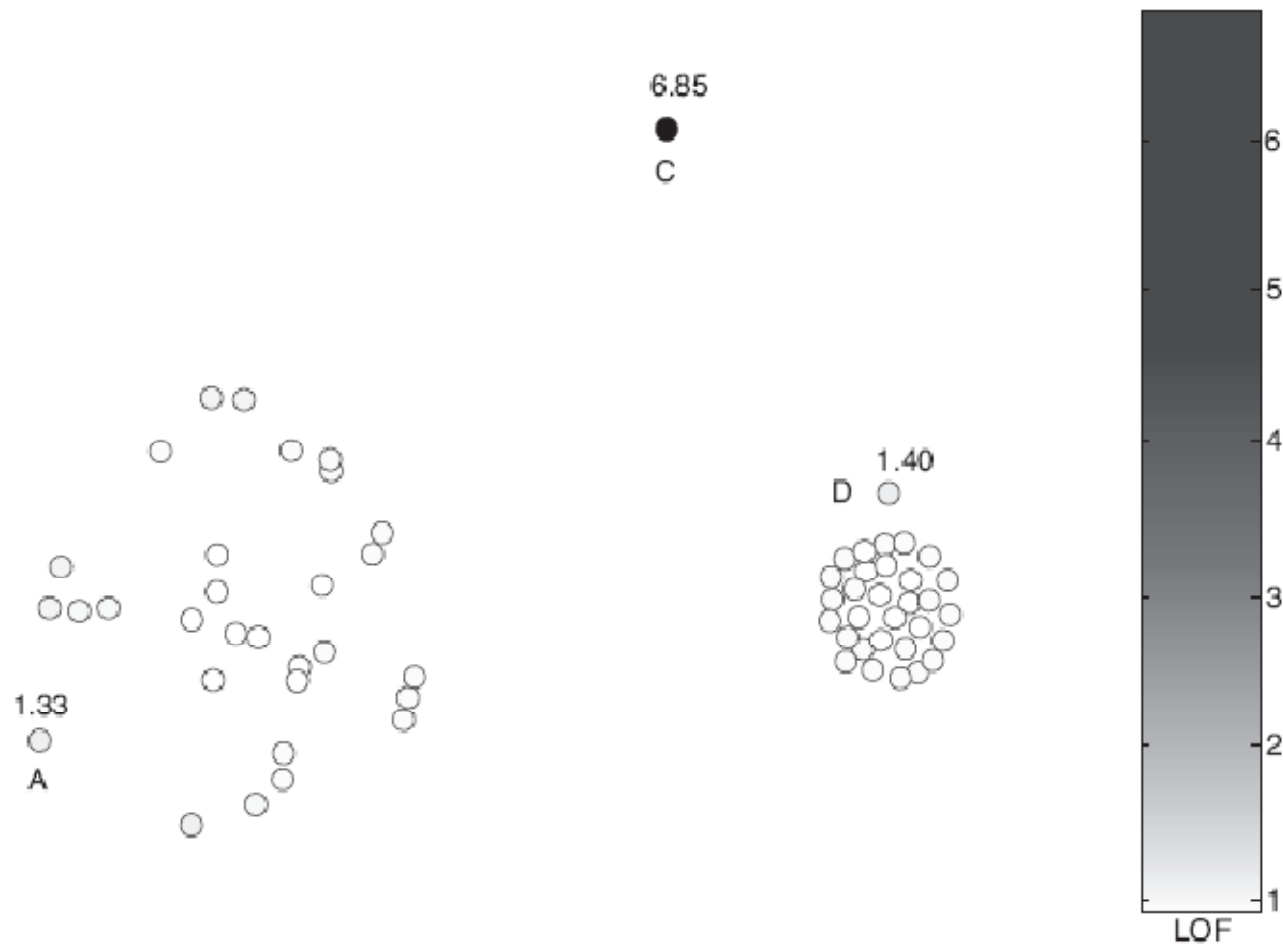
- Number of objects within fixed radius d (DBSCAN).
 - These two example scores work poorly if data has variable density.

Density-based outlier detection

- Relative density outlier score (Local Outlier Factor, LOF)
 - Reciprocal of average distance to k nearest neighbors, relative to that of those k neighbors.

$$\text{relative density}(\mathbf{x}, k) = \frac{\text{density}(\mathbf{x}, k)}{\frac{1}{k} \sum_{\mathbf{y} \in N(\mathbf{x}, k)} \text{density}(\mathbf{y}, k)}$$

Density-based outlier detection



relative density (LOF) outlier scores

Density-based outlier detection

- Pros

- Quantitative measure of degree to which object is an outlier.
- Can work well even if data has variable density.

- Cons

- $O(n^2)$ complexity
- Must choose parameters
 - ◆ k for nearest neighbor
 - ◆ d for distance threshold

Cluster-based outlier detection

Outliers are objects that do not belong strongly to any cluster.

- Approaches:
 - Assess degree to which object belongs to any cluster.
 - Eliminate object(s) to improve objective function.
 - Discard small clusters far from other clusters.
- Issue:
 - Outliers may affect initial formation of clusters.

Cluster-based outlier detection

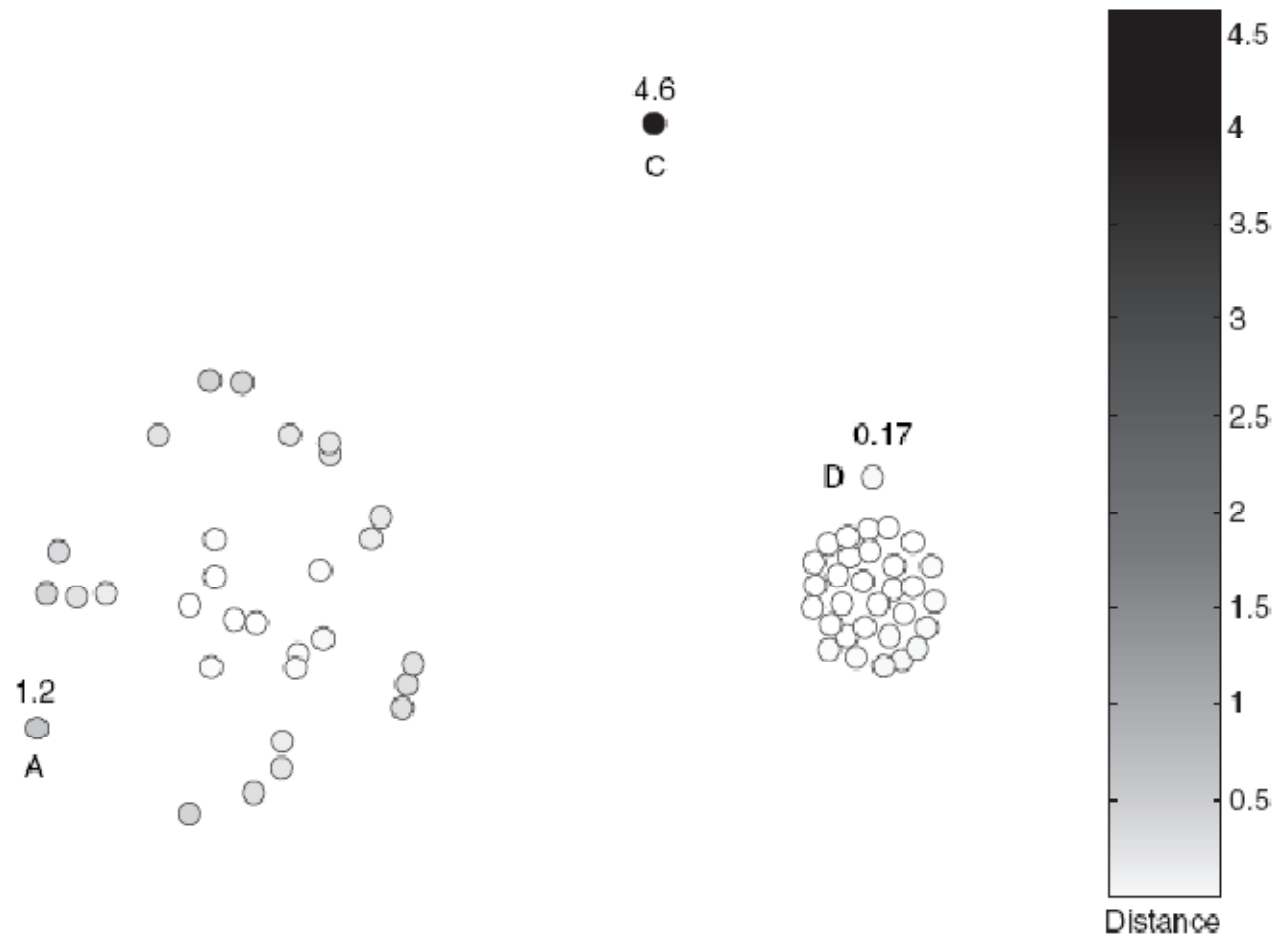
Assess degree to which object belongs to any cluster.

- For prototype-based clustering (e.g. k-means), use distance to cluster centers.
 - To deal with variable density clusters, use relative distance:

$$\frac{\text{distance}(\mathbf{x}, \text{centroid}_C)}{\text{median}(\{\forall_{x' \in C} \text{distance}(\mathbf{x}', \text{centroid}_C)\})}$$

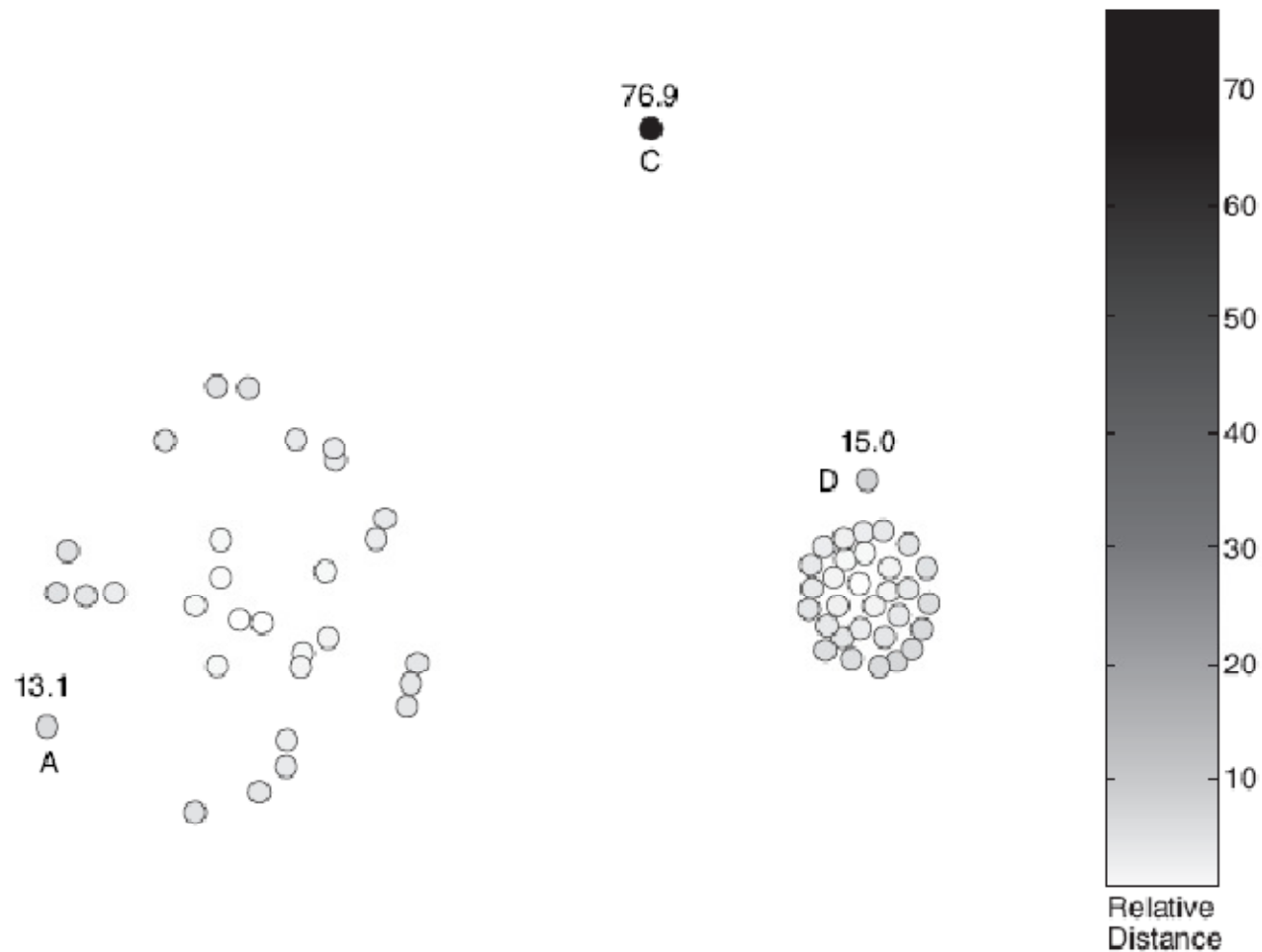
- Similar concepts for density-based or connectivity-based clusters.

Cluster-based outlier detection



distance of points from nearest centroid

Cluster-based outlier detection



relative distance of points from nearest centroid

Cluster-based outlier detection

Eliminate object(s) to improve objective function.

- 1) Form initial set of clusters.
- 2) Remove the object which most improves objective function.
- 3) Repeat step 2) until ...

Cluster-based outlier detection

Discard small clusters far from other clusters.

- Need to define thresholds for “small” and “far”.

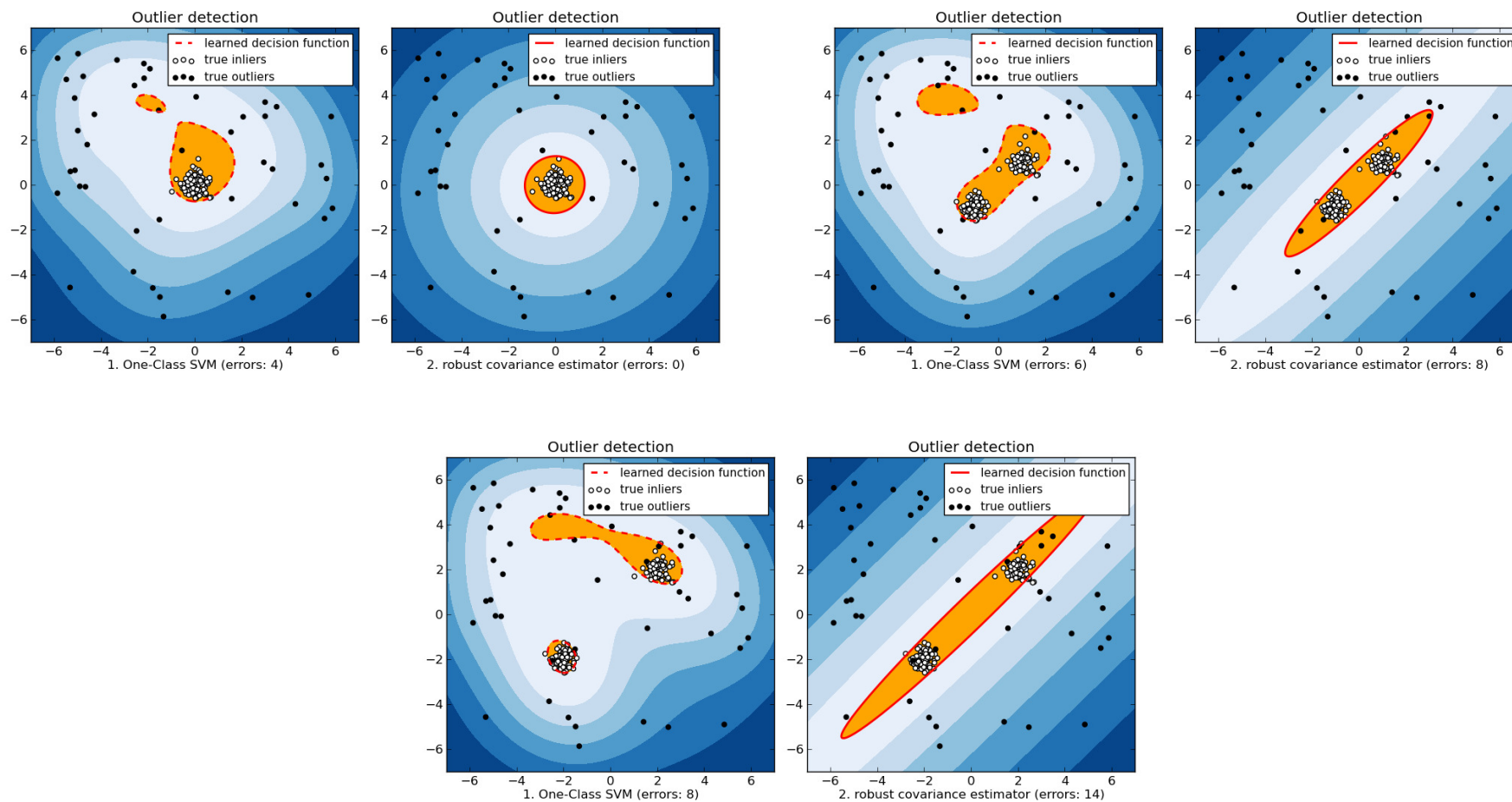
Cluster-based outlier detection

- Pro:
 - Some clustering techniques have $O(n)$ complexity.
 - Extends concept of outlier from single objects to groups of objects.
- Cons:
 - Requires thresholds for minimum size and distance.
 - Sensitive to number of clusters chosen.
 - Hard to associate outlier score with objects.
 - Outliers may affect initial formation of clusters.

One-class support vector machines

- Data is unlabelled, unlike usual SVM setting.
- Goal: find hyperplane (in higher-dimensional kernel space) which encloses as much data as possible with minimum volume.
 - Tradeoff between amount of data enclosed and tightness of enclosure; controlled by regularization of slack variables.

One-class SVM vs. Gaussian envelope



Images from http://scikit-learn.org/stable/modules/outlier_detection.html

One-class SVM demo

LIBSVM

<http://www.csie.ntu.edu.tw/~cjlin/libsvm/>

-s 2 -t 2 -g 50 -n 0.35

Anomaly detection on real network data

• Three groups of features

– Basic features of individual TCP connections

- ◆ source & destination IP *Features 1 & 2*
- ◆ source & destination port *Features 3 & 4*
- ◆ Protocol *Feature 5*
- ◆ Duration *Feature 6*
- ◆ Bytes per packets *Feature 7*
- ◆ number of bytes *Feature 8*

<i>dst ... service ... flag</i>		<i>dst ... service ... flag %S0</i>
h1 http S0	syn flood	h1 http S0 70
h1 http S0		h1 http S0 72
h1 http S0		h1 http S0 75
h2 http S0	normal	h2 http S0 0
h4 http S0		h4 http S0 0
h2 ftp S0		h2 ftp S0 0

existing features useless construct features with high information gain

– Time based features

- ◆ For the same source (*destination*) IP address, number of unique destination (*source*) IP addresses inside the network *in last T seconds* – *Features 9 (13)*
- ◆ Number of connections from source (*destination*) IP to the same destination (*source*) port *in last T seconds* – *Features 11 (15)*

– Connection based features

- ◆ For the same source (*destination*) IP address, number of unique destination (*source*) IP addresses inside the network *in last N connections* - *Features 10 (14)*
- ◆ Number of connections from source (*destination*) IP to the same destination (*source*) port *in last N connections* - *Features 12 (16)*

Typical anomaly detection output

score	srcIP	sPort	dstIP	dPort	protocol	flags	packets	bytes	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16
37674.69	63.150.X.253	1161	128.101.X.29	1434	17	16	[0,2)	[0,1829)	0	0	0	0	0	0	0	0	0.81	0	0.59	0	0	0	0	0
26676.62	63.150.X.253	1161	160.94.X.134	1434	17	16	[0,2)	[0,1829)	0	0	0	0	0	0	0	0	0.81	0	0.59	0	0	0	0	0
24323.55	63.150.X.253	1161	128.101.X.185	1434	17	16	[0,2)	[0,1829)	0	0	0	0	0	0	0	0	0.81	0	0.58	0	0	0	0	0
21169.49	63.150.X.253	1161	160.94.X.71	1434	17	16	[0,2)	[0,1829)	0	0	0	0	0	0	0	0	0.81	0	0.58	0	0	0	0	0
19525.31	63.150.X.253	1161	160.94.X.19	1434	17	16	[0,2)	[0,1829)	0	0	0	0	0	0	0	0	0.81	0	0.58	0	0	0	0	0
19235.39	63.150.X.253	1161	160.94.X.80	1434	17	16	[0,2)	[0,1829)	0	0	0	0	0	0	0	0	0.81	0	0.58	0	0	0	0	0
17679.1	63.150.X.253	1161	160.94.X.220	1434	17	16	[0,2)	[0,1829)	0	0	0	0	0	0	0	0	0.81	0	0.58	0	0	0	0	0
8183.58	63.150.X.253	1161	128.101.X.108	1434	17	16	[0,2)	[0,1829)	0	0	0	0	0	0	0	0	0.82	0	0.58	0	0	0	0	0
7142.98	63.150.X.253	1161	128.101.X.223	1434	17	16	[0,2)	[0,1829)	0	0	0	0	0	0	0	0	0.82	0	0.57	0	0	0	0	0
5139.01	63.150.X.253	1161	128.101.X.142	1434	17	16	[0,2)	[0,1829)	0	0	0	0	0	0	0	0	0.82	0	0.57	0	0	0	0	0
4048.49	142.150.Y.101	0	128.101.X.127	2048	1	16	[2,4)	[0,1829)	0	0	0	0	0	0	0	0	0.83	0	0.56	0	0	0	0	0
4008.35	200.250.Z.20	27016	128.101.X.116	4629	17	16	[2,4)	[0,1829)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0
3657.23	202.175.Z.237	27016	128.101.X.116	4148	17	16	[2,4)	[0,1829)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0
3450.9	63.150.X.253	1161	128.101.X.62	1434	17	16	[0,2)	[0,1829)	0	0	0	0	0	0	0	0	0.82	0	0.57	0	0	0	0	0
3327.98	63.150.X.253	1161	160.94.X.223	1434	17	16	[0,2)	[0,1829)	0	0	0	0	0	0	0	0	0.82	0	0.57	0	0	0	0	0
2796.13	63.150.X.253	1161	128.101.X.241	1434	17	16	[0,2)	[0,1829)	0	0	0	0	0	0	0	0	0.82	0	0.57	0	0	0	0	0
2693.88	142.150.Y.101	0	128.101.X.168	2048	1	16	[2,4)	[0,1829)	0	0	0	0	0	0	0	0	0.83	0	0.56	0	0	0	0	0
2683.05	63.150.X.253	1161	160.94.X.43	1434	17	16	[0,2)	[0,1829)	0	0	0	0	0	0	0	0	0.82	0	0.57	0	0	0	0	0
2444.16	142.150.Y.236	0	128.101.X.240	2048	1	16	[2,4)	[0,1829)	0	0	0	0	0	0	0	0	0.83	0	0.56	0	0	0	0	0
2385.42	142.150.Y.101	0	128.101.X.45	2048	1	16	[0,2)	[0,1829)	0	0	0	0	0	0	0	0	0.83	0	0.56	0	0	0	0	0
2114.41	63.150.X.253	1161	160.94.X.183	1434	17	16	[0,2)	[0,1829)	0	0	0	0	0	0	0	0	0.82	0	0.57	0	0	0	0	0
2057.15	142.150.Y.101	0	128.101.X.161	2048	1	16	[0,2)	[0,1829)	0	0	0	0	0	0	0	0	0.83	0	0.56	0	0	0	0	0
1919.54	142.150.Y.101	0	128.101.X.99	2048	1	16	[2,4)	[0,1829)	0	0	0	0	0	0	0	0	0.83	0	0.56	0	0	0	0	0
1634.38	142.150.Y.101	0	128.101.X.219	2048	1	16	[2,4)	[0,1829)	0	0	0	0	0	0	0	0	0.83	0	0.56	0	0	0	0	0
1596.26	63.150.X.253	1161	128.101.X.160	1434	17	16	[0,2)	[0,1829)	0	0	0	0	0	0	0	0	0.82	0	0.57	0	0	0	0	0
1513.96	142.150.Y.107	0	128.101.X.2	2048	1	16	[0,2)	[0,1829)	0	0	0	0	0	0	0	0	0.83	0	0.56	0	0	0	0	0
1389.09	63.150.X.253	1161	128.101.X.30	1434	17	16	[0,2)	[0,1829)	0	0	0	0	0	0	0	0	0.82	0	0.57	0	0	0	0	0
1315.88	63.150.X.253	1161	128.101.X.40	1434	17	16	[0,2)	[0,1829)	0	0	0	0	0	0	0	0	0.82	0	0.57	0	0	0	0	0
1279.75	142.150.Y.103	0	128.101.X.202	2048	1	16	[0,2)	[0,1829)	0	0	0	0	0	0	0	0	0.83	0	0.56	0	0	0	0	0
1237.97	63.150.X.253	1161	160.94.X.32	1434	17	16	[0,2)	[0,1829)	0	0	0	0	0	0	0	0	0.83	0	0.56	0	0	0	0	0
1180.82	63.150.X.253	1161	128.101.X.61	1434	17	16	[0,2)	[0,1829)	0	0	0	0	0	0	0	0	0.83	0	0.56	0	0	0	0	0

- Anomalous connections that correspond to the “slammer” worm
- Anomalous connections that correspond to the ping scan
- Connections corresponding to Univ. Minnesota machines connecting to “half-life” game servers

Real-world issues in anomaly detection

- Data often streaming, not static
 - Credit card transactions
- Anomalies can be *bursty*
 - Network intrusions

Quote of the day

An excerpt from advice given by a machine learning veteran on StackOverflow:

“ ... you are training and testing on the same data.
A kitten dies every time this happens.”