

Energy Dissipation Systems

Dorothy Reed
Civil & Environmental Engineering

Outline

- Definitions
- Focus on semi-active systems
- Conclusions

Energy Conservation

[Uang & Bertero (1988)]

$$E = E_k + E_s + E_h + E_d$$

E = absolute total energy input

E_k = absolute kinetic energy

E_s = recoverable elastic strain energy

E_h = irrecoverable energy dissipated by the structural system through inelastic or other forms of action

E_d = energy dissipated by supplemental damping devices

Energy Dissipation E_d aka Damping

- Passive
- Semi-active
- Active

Passive [Lowes presentation]

- Seismic Isolation
- Viscoelastic Solid Dampers
- Sometimes viscous fluid dampers included in this category

Semi-active

- “Fuzzy” category: sometimes lumped with active dampers
- Includes
 - Tuned mass dampers
 - Tuned liquid dampers
 - Variable stiffness and damping systems

Active

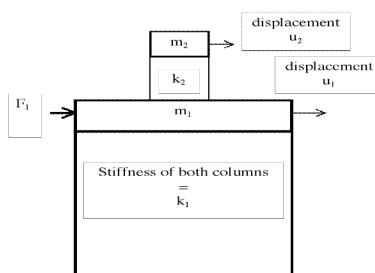
- Power added to system
- Active tuned mass dampers
- Active braced systems

Focus on Semi-active

- Observation
- Mathematical models
- Empirical analysis
- Design methodology

Observation

- Simple model
- Vibration
- Effect of sloshing



System Parameters: Ignore Damping

$$\text{let } F_1 = p_0 \sin \omega t \quad \text{so } F = \begin{bmatrix} p_0 \sin \omega t \\ 0 \end{bmatrix}$$

$$M = \begin{bmatrix} m_1 & 0 \\ 0 & m_2 \end{bmatrix}$$

$$K = \begin{bmatrix} k_1 + k_2 & -k_2 \\ -k_2 & k_2 \end{bmatrix}$$

EOM

$$m_1 \ddot{u}_1 + (k_1 + k_2)u_1 - k_2 u_2 = p_0 \sin \omega t$$

$$m_2 \ddot{u}_2 - k_2 u_1 + k_2 u_2 = 0$$

Steady-State

$$u_1 = C_1 \sin \omega t, \quad u_2 = C_2 \sin \omega t$$

$$\ddot{u}_1 = -\omega^2 C_1 \sin \omega t, \quad \ddot{u}_2 = -\omega^2 C_2 \sin \omega t$$

Substitute into EOM

$$m_1(-\omega^2 C_1) \sin \omega t + (k_1 + k_2) C_1 \sin \omega t - k_2 C_2 \sin \omega t = p_0 \sin \omega t$$

$$m_2(-\omega^2 C_2) \sin \omega t - k_1 C_1 \sin \omega t + k_2 C_2 \sin \omega t = 0$$

Solve for constants

$$\square m_1 \square^2 C_1 + (k_1 + k_2) C_1 - k_2 C_2 = p_0$$

$$C_1 = \frac{p_0 - k_2 C_2}{(k_1 + k_2) - m_1 \square^2}$$

This is zero (i.e., no displacement of m_1) when $C_2 = \frac{p_0}{k_2}$.

What else? Tuning

$$\square m_2 \square^2 - k_2 C_1 + k_2 C_2 = 0$$

$$C_2 (\square m_2 \square^2 + k_2) = k_2 C_1$$

$$C_1 = \frac{C_2 (\square m_2 \square^2 + k_2)}{k_2}$$

For $C_1 = 0$ but $C_2 \neq 0$, $-\square m_2 \square^2 + k_2 = 0$

$$\square \square = \sqrt{\frac{k_2}{m_2}} \quad \text{for } C_1 = 0$$

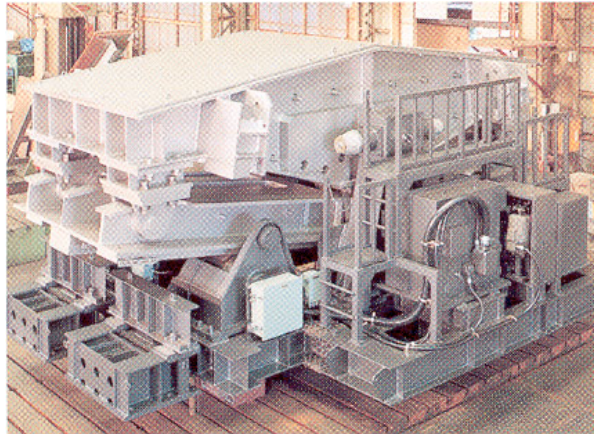
Solution Comments

$$u_2 = \frac{p_0}{k_2} \sin \sqrt{\frac{k_2}{m_2}} t \quad \text{for} \quad \square = \sqrt{\frac{k_2}{m_2}}$$

DUOX: solid mass damper



TRIGON



TRIGON

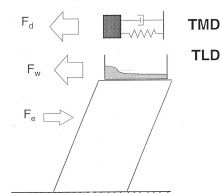


In practice, damping and MDOF systems complicate the process

- Devise experiments to test the limits of the theory
- Use water instead of solid mass

TMD and TLD Model

Damping Mechanism



Set-up for TLD analysis

Experiment

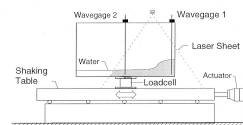


Figure 1: Test set-up

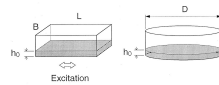
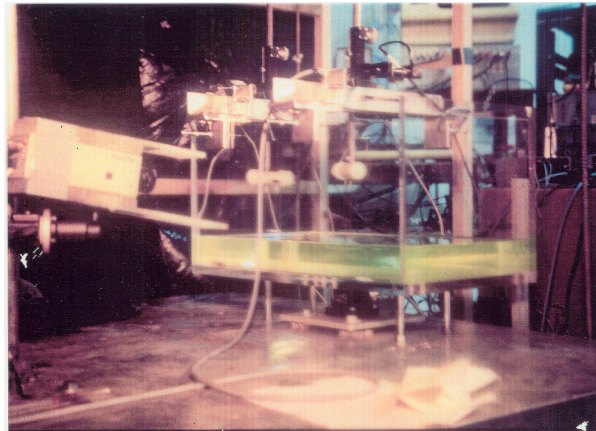


Figure 2: Tank Configurations

TLD-experiment



Deep water sloshing



Linear Wave Theory: Frequency
of sloshing for rectangular tank

$$f_w = \frac{1}{2\pi} \sqrt{\frac{g}{L} \tanh\left(\frac{h_0}{L}\right)}$$

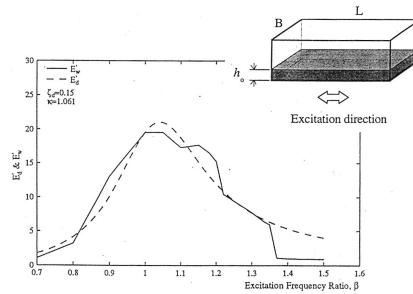
Circular Tank

$$f_w = \frac{1}{2\pi} \sqrt{\frac{1.17\pi g}{D} \tanh\left(\frac{1.17\pi h_0}{D}\right)}$$

Energy dissipation per cycle

$$E_w = \int_{T_s} F_w dx_s$$

Energy dissipation

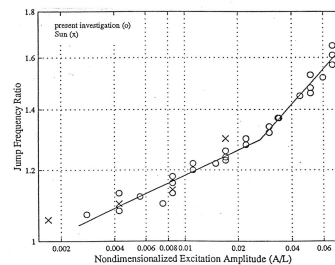


Movie Clip

Yeh, et al. experiments



Frequency investigation



Relationship between the jump frequency ratio and the nondimensional excitation amplitude based on experimental results of Sun, et al. (1991) and the present investigation.

NSD Model

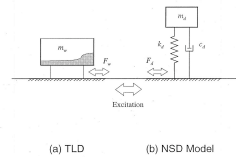
Definition of the NSD Model

The NSD is an equivalent TMD representation of the TLD with varying stiffness and damping.

Its stiffness and damping properties are derived from an energy dissipation matching scheme using shaking table data.

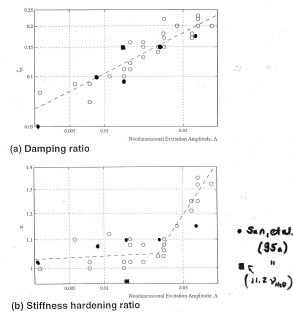
Diagram of NSD

NSD Model

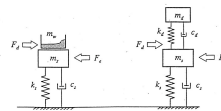


Comparison

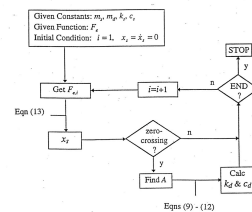
NSD Model



Design Algorithm

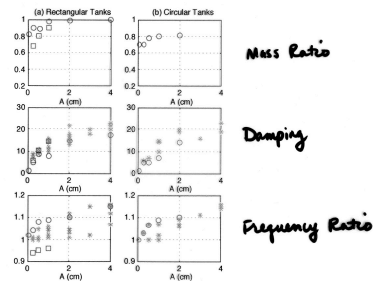


The algorithm for estimating structural behavior using the NSD model.

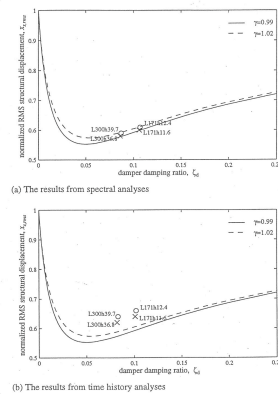


Comparison

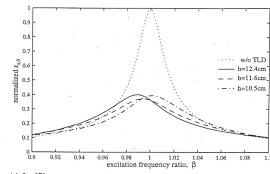
Figure 1. Comparison of the equivalent TMD models for Sun et al. (1995) (○ for water; □ for liquid with viscosity 11.2 times greater than that of water) with Yu (1997) (* water). Plots in column (a) are for rectangular tanks; in (b) are for circular tanks.



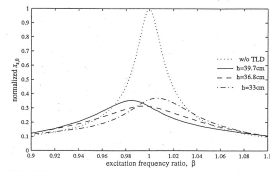
Additional damping investigation



Comparison

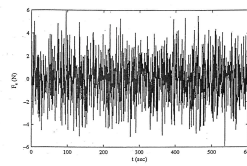


(a) $L = 171\text{cm}$

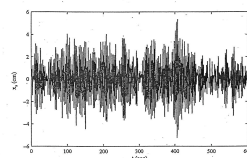


(b) $L = 500\text{cm}$

Simulation

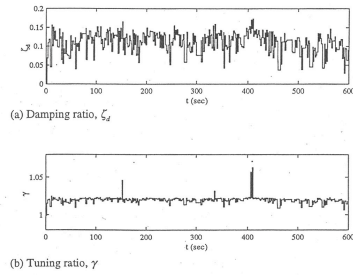


(a) White noise random forcing



(b) Structural displacement induced by the random forcing

Simulation



Design Equation

$$h_0 = \frac{L}{\Delta} \tanh \left[\frac{4 \Delta L f_s^2}{g \Delta^2} \right]$$

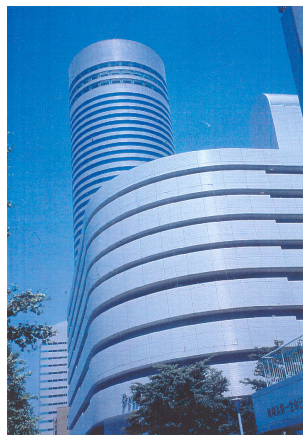
where $\Delta = 1.038 \left(\frac{x_s}{L} \right)^{0.0034}$ for $\frac{x_s}{L} \leq 0.03$ weak wave breaking

$\Delta = 1.59 \left(\frac{x_s}{L} \right)^{0.125}$ for $\frac{x_s}{L} > 0.03$ strong wave breaking

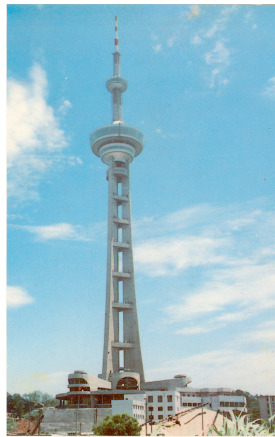
Shimizu TLD



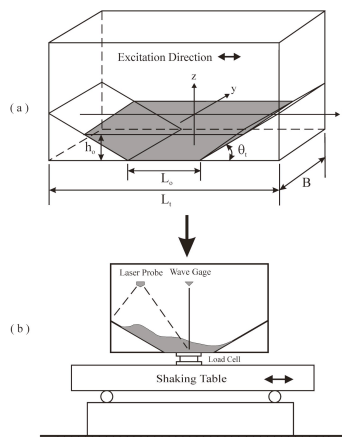
Rooftop of Yokohama Hotel



Nanjing Tower [PRC]



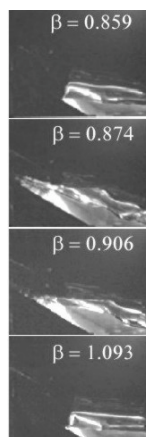
Sloped Bottom (Gardarsson, Olsen)



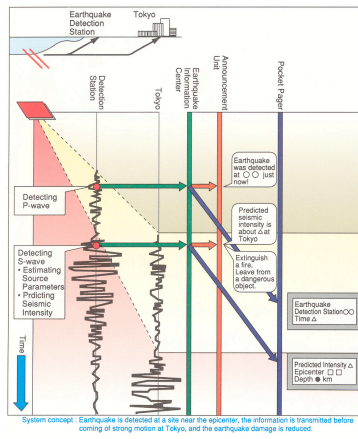
Sloped Tank Notes

- Angle of slope modifies water sloshing behavior
- No simple water frequency equation exists so empirical investigation of sloshing required
- Stiffness degrading system vs stiffness hardening

Tank behavior: $\beta = f_e / f_w$



Active Control Scheme



Active Mass Damper [AMD]

SENDAGAYA INTES



Year: 1991
 Location: Tokyo
 Occupancy: Office
 Height: 58m
 Stories: 81, 11F
 Effective weight: 3,280tonf
 Natural period:
 1.7sec(Trans.)
 2.1sec(Torsion)
 Moving Mass:
 Ice Thermal Storage Tank
 Weight of Mass: 36tonf x 2
 Actuator's Force: 5tonf/unit



AMD system



Actuator

AMD

APPLAUSE TOWER



Year: 1992
 Location: Osaka
 Occupancy: Commercial,
 Office, Hotel
 Height: 161m
 Stories: 53, 34F
 Effective weight: 13,943tonf
 Natural period:
 4.8sec(trans.)
 4.7sec(Longi.)
 Moving Mass: Heliport
 Weight of Mass: 460tonf
 Actuator's Force:
 5tonf X 2/direction



Actuator & Rubber Bearing



Control Panel

AMD

PORTE KANAZAWA



Year: 1993
 Location: Kanazawa
 Occupancy: Commercial,
 Office, Hotel
 Height: 131m
 Stories: 52, 30F, P2
 Effective weight: 10,150tonf
 Natural period:
 2.9sec(Trans.)
 2.5sec(Torsion)
 Moving Mass:
 Concrete Block
 Weight of Mass: 50tonf X 2
 Actuator's Force: 5tonf/unit

Design: MHS Planners, Architects & Engineers



AMD system



Actuator

AMD

HERBIS OSAKA



Year:1997
 Location:Osaka
 Occupancy:Commercial,
 Office,Hotel
 Height:100m
 Stories:85,48F,P1
 Effective weight:22,749tonf
 Natural period:
 5.4sec(Trans.)
 5.5sec(Torsion)
 Moving Mass:
 Ice Thermal Storage Tank
 Weight of Mass:160tonfX2
 Actuator's Force:5tonf/unit



AMD system



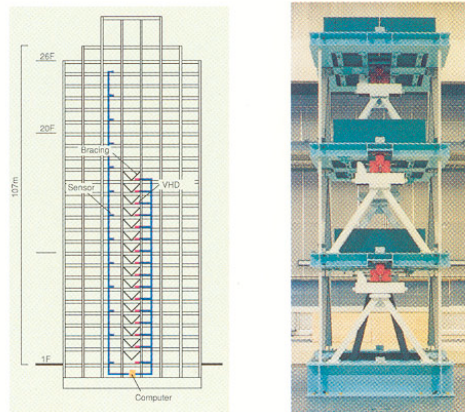
Actuator

AVS

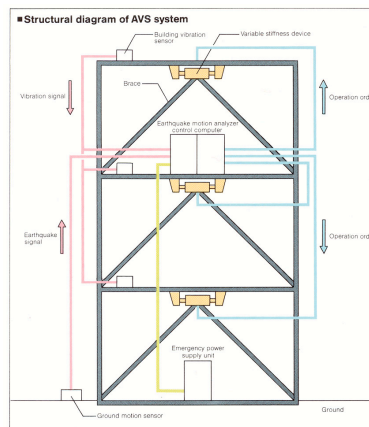
鹿島技研21号館 KaTRI No.21 Building



AVS



AVS



Conclusions

- Passive systems best for earthquakes
- Hybrid passive coupled with semi-active or active devices gaining in popularity
- Semi-active TMD, TLD most popular outside of US, especially for wind loadings
- AMD systems have promise but require reliable power sources