

A photograph showing the interior of a glacier, with dark, jagged ice formations and a central stream of meltwater. The scene is dimly lit, highlighting the textures and colors of the ice and water.

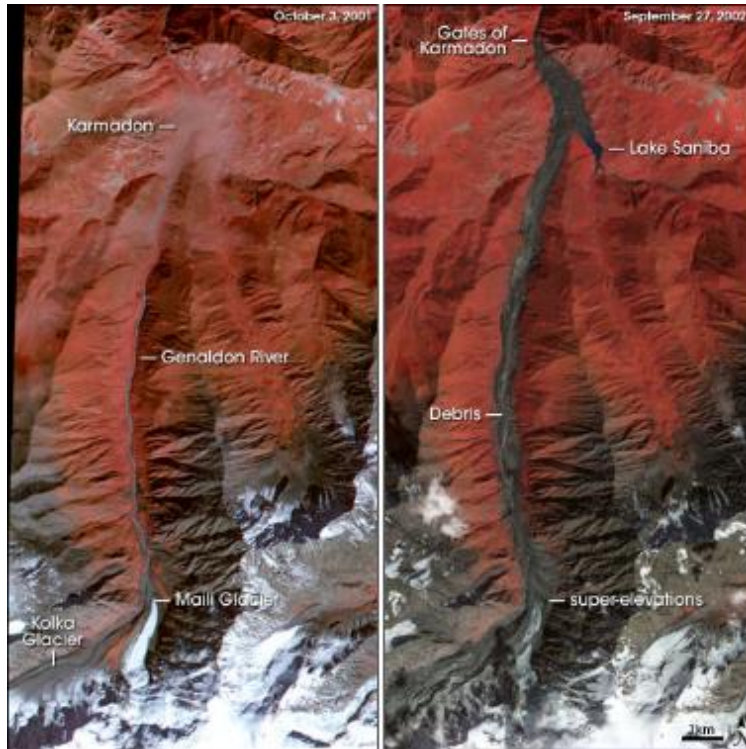
GLACIER SLIDING and HYDROLOGY

PRINCIPLES OF GLACIOLOGY
THE CRYOSPHERE
ESS 431/ESS 505
OCTOBER 24, 2016

Nick Holschuh / Knut Christianson

Ice Avalanche

NASA Earth Observatory



NASA Earth Observatory



September 20, 2002, North Ossetia, (Russian Caucasus)

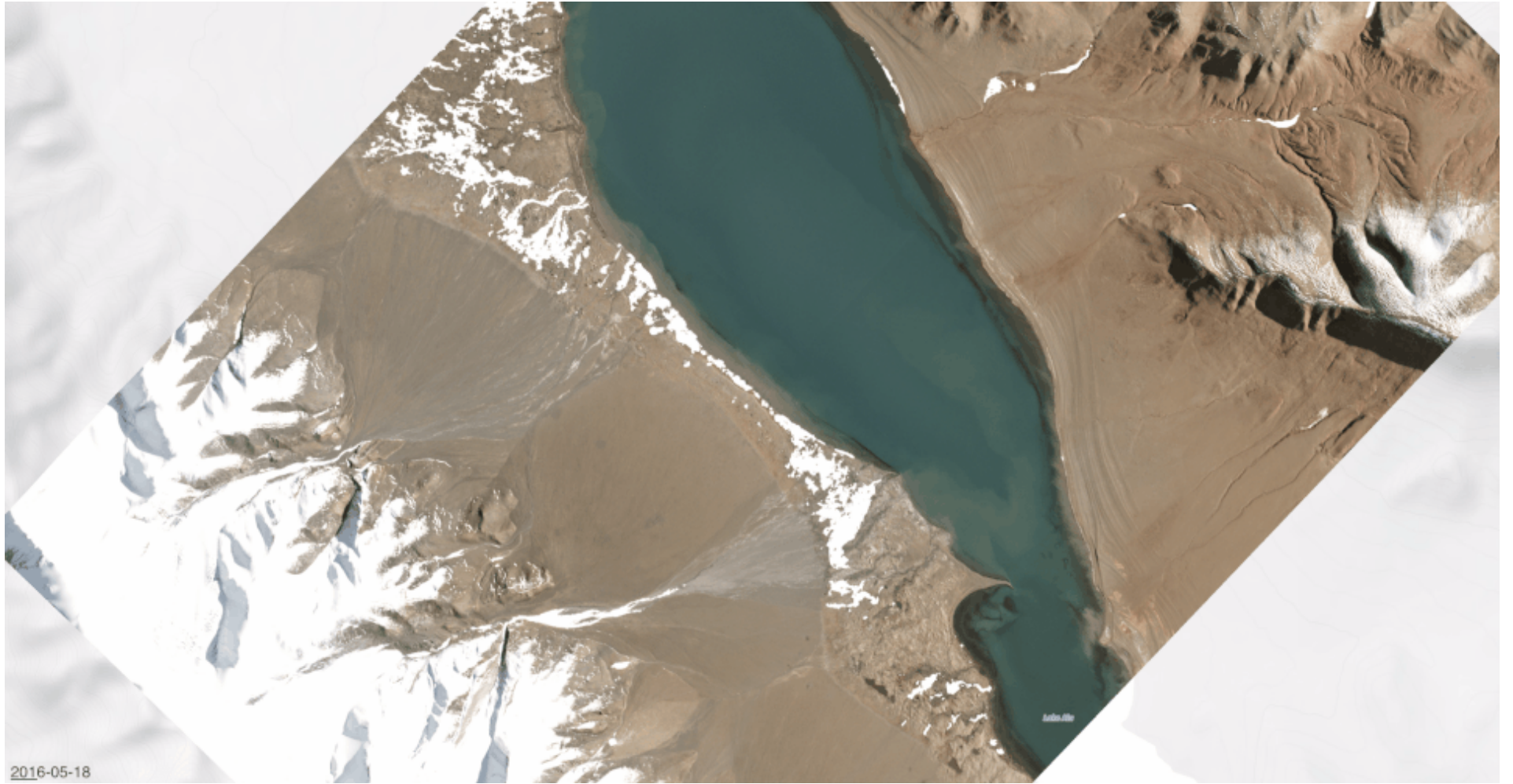
- Part of Maili Glacier broke off and avalanched, ~100 km per hour
- 20×10^6 tonnes of ice, rock, mud swept ~16 km through Karmadon Gorge
- ~140 fatalities, village of Nizhny Karmadon destroyed



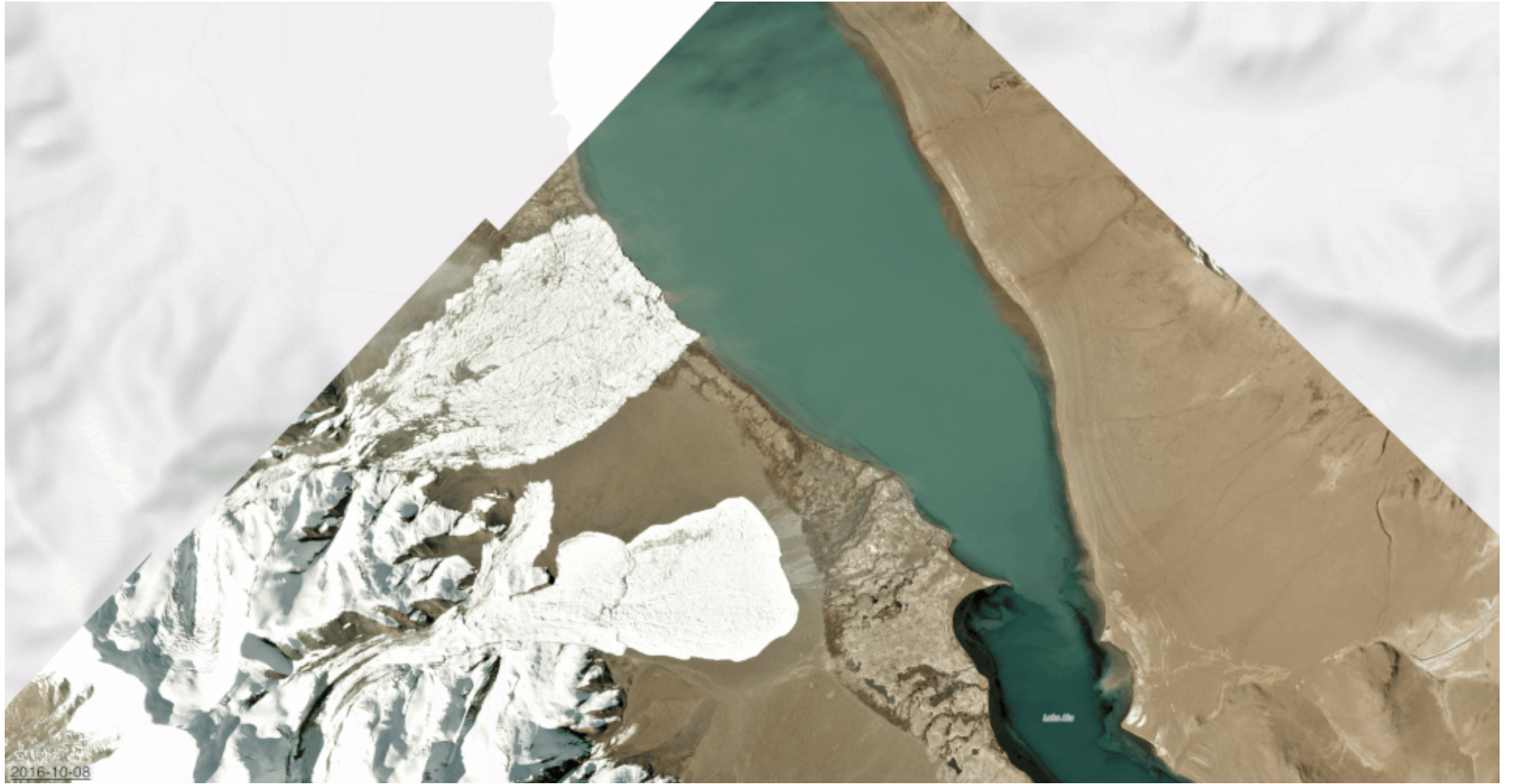
The glacier before its collapse in early July. Some crevasses, a sign of imminent surging, can be seen at its base. (Planet)

July 3rd, 2016









Today's Objectives:

Basal Sliding:

- What are the controls on basal sliding? How do they compare with the physics of internal deformation?
- What are the two dominant processes that allow sliding past bed features? What is the role of water in each process?

Hydrology:

- How is water transported in a glacial system?
- How does the amount of water in the system affect the water transport regime?

Importance of Sliding

Internal deformation u_d is always present

Sliding contribution to ice transport:

$u_s = 0 \times u_d$ e.g. frozen bed

$u_s = 10^N \times u_d$ e.g. glacier surges and ice streams

N can be as high as ~ 3

In “typical” temperate mountain glaciers, it is commonly supposed that

Ice transport due to sliding \approx Ice transport due to internal deformation

What's it like under a glacier?

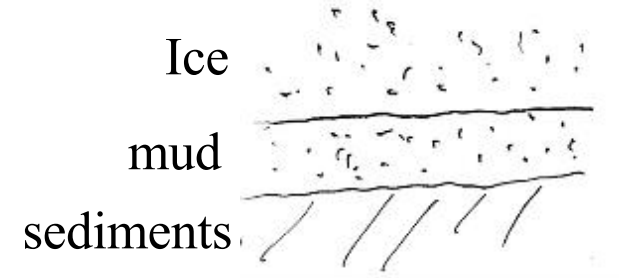
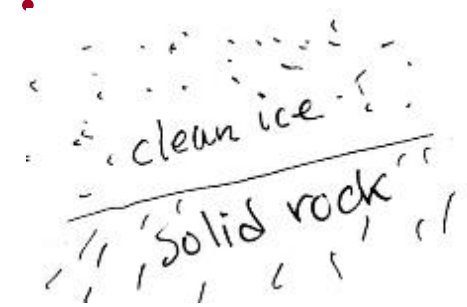
Smooth clean bedrock

Frozen ground (tundra, gravel, till)

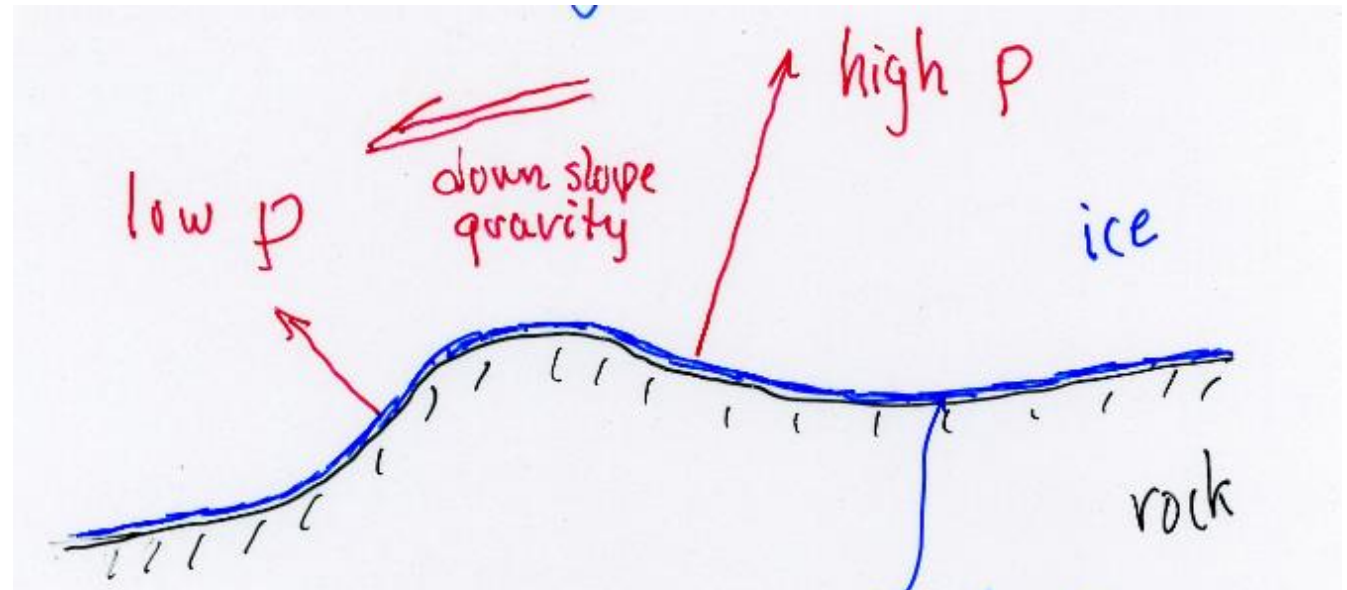
Soft marine mud

Glacial till – unsorted gravel, mud

- Soft, wet deformable
- Hard, overconsolidated
- Wet, thawing (geothermal flux, frictional heat)
- Wet, freezing (ice fingers into pores)



Hard-bed sliding



Force equilibrium requires difference in pressure across the bump

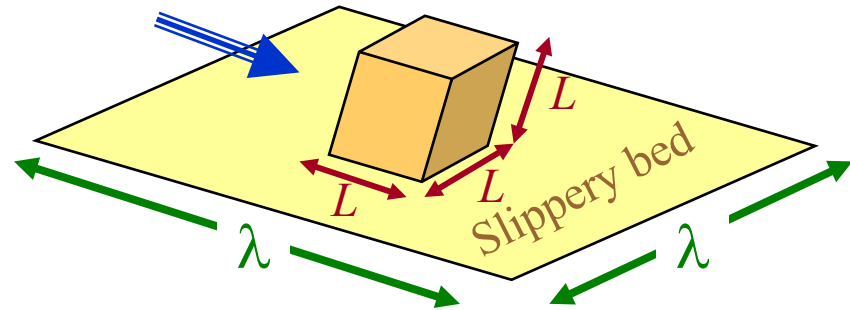
Water layer provides local lubrication

What allows slip to occur?

Tombstone Model

(J. Weertman, 1957)

A simple starting model
for sliding



1) Regelation

2) Enhanced Deformation

Weertman, J. (1957), *J. Glac.* 3, 33.

ON THE SLIDING OF GLACIERS

By J. WEERTMAN

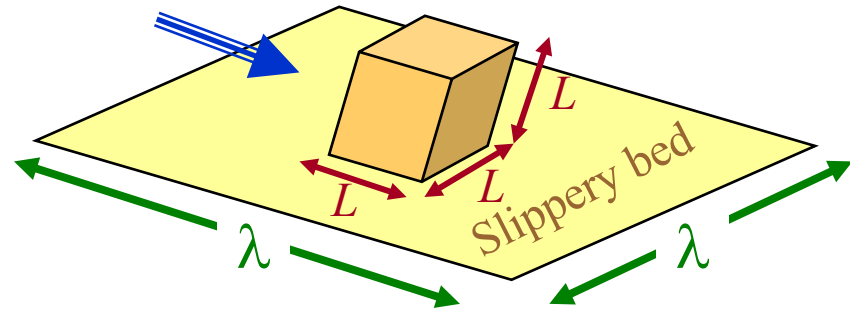
(Naval Research Laboratory, Washington, D.C.)

ABSTRACT. A model is proposed to explain the sliding of any glacier whose bottom surface is at the pressure melting point. Two mechanisms are considered. One is pressure melting and the other is creep rate enhancement through stress concentrations. Neither of the mechanisms operating alone is sufficient to explain sliding. If both mechanisms operate together appreciable sliding can occur.

Tombstone Model

(J. Weertman, 1957)

A simple starting model
for sliding



If ice is not accelerating off the mountain (i.e. an ice avalanche), then there must be a restraining force to balance the down-slope driving shear stress

$\tau = \rho g h \sin(\theta)$ acting on area $\lambda \times \lambda$. $h =$ ice thickness
 $\theta =$ surface slope

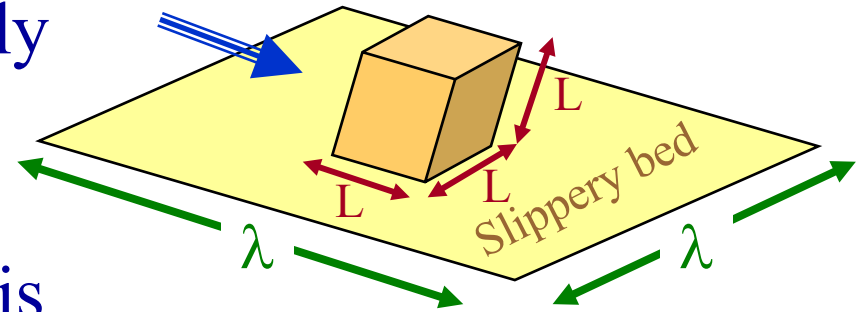
Force = stress \times Area on area $\lambda \times \lambda$:

$$F = \tau \lambda^2$$

- But there is no basal shear stress on slippery bed ...

Tombstone face

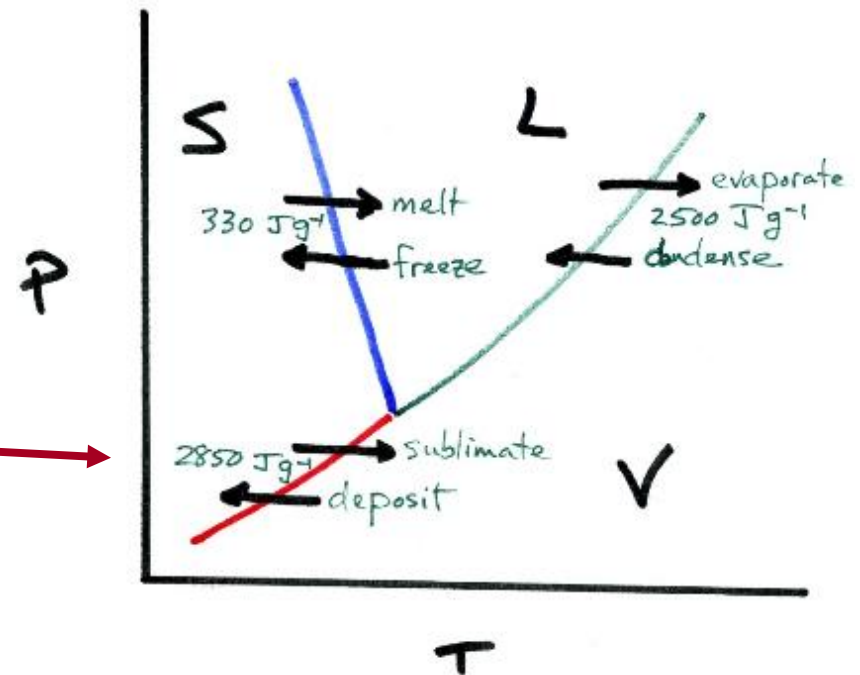
- Force $\tau \lambda^2$ is supported entirely by uphill face of bump
- This face has area L^2
- Pressure (stress) on that face is $P = \tau \lambda^2 / L^2$ (force/Area)



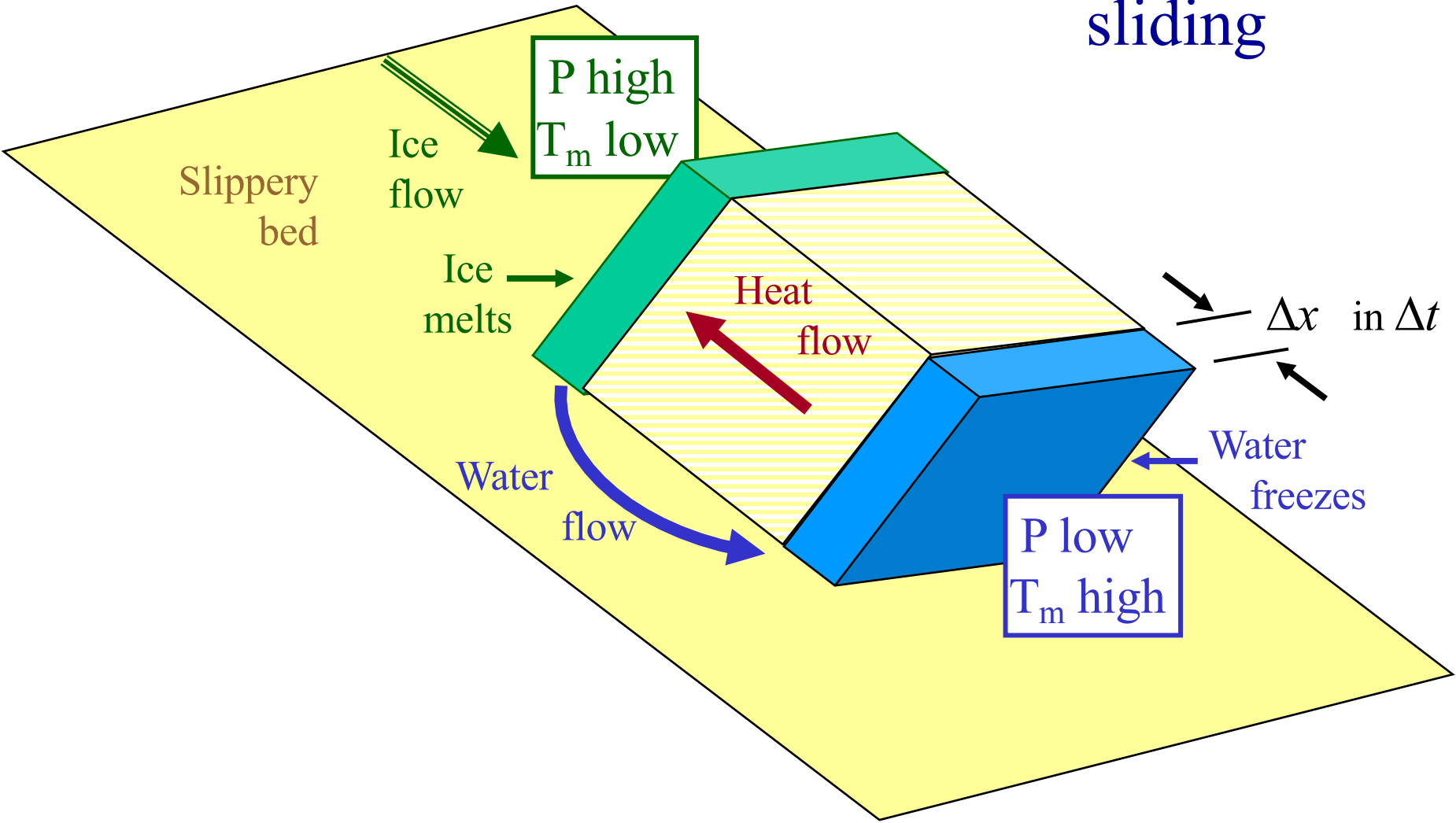
High pressure depresses freezing point

- $\Delta T = c P$
- $c = -7 \times 10^{-8} \text{ } ^\circ\text{C Pa}^{-1}$ (slope on phase boundary)

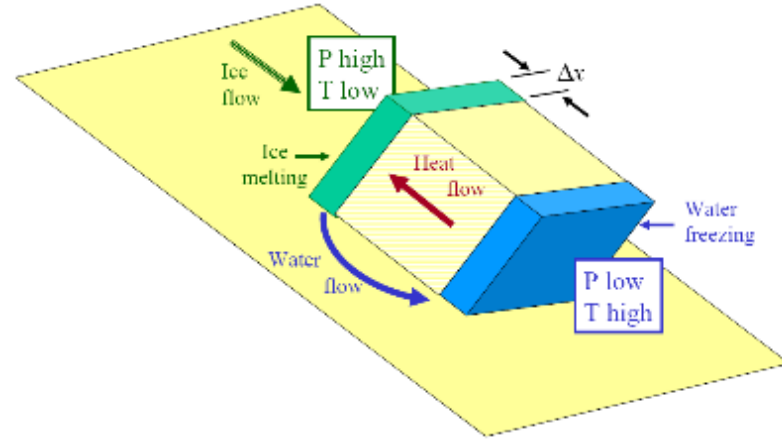
$$\Delta T = c \tau \lambda^2 / L^2$$



Regelation sliding



Can ice slide past a Bump?



- How fast ice can move past bump depends on how fast heat can get back through bump.
- Heat flux Q depends on temperature gradient $\Delta T/L$ (Fourier's Law).

$$Q = -K \Delta T / L$$

K = rock conductivity $\cong 2 \text{ W m}^{-1} \text{ deg}^{-1}$

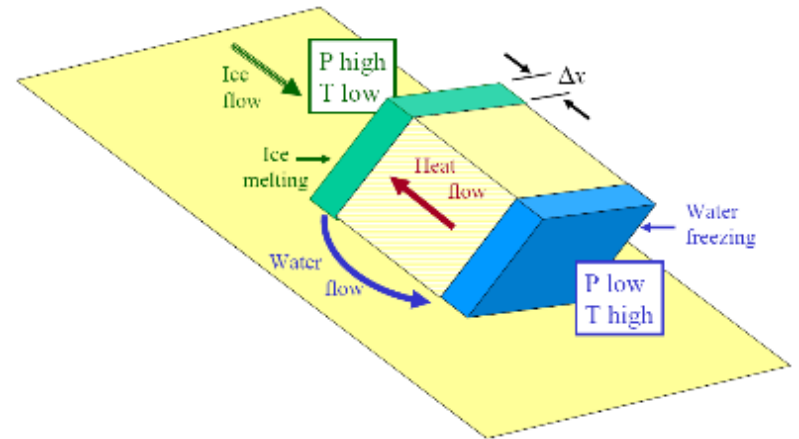
L = rock scale length (m)

$$\Delta T = c \tau \lambda^2 / L^2$$

$$Q = - \left(\frac{Kc\tau}{L} \right) \left(\frac{\lambda^2}{L^2} \right)$$

Sliding Speed by Regelation

In time Δt , heat flux Q (W m^{-2}) delivered to Area $=L^2$ of rock face can melt a volume V of ice given by: $V = L^2 \times \Delta x$ (1)



$$V = (\text{energy delivered}) / (\text{energy to melt } 1\text{m}^3)$$

$$V = (Q \times L^2 \times \Delta t) / (\rho H) \quad (2)$$

$$H = \text{heat of fusion} = 3.31 \text{ J kg}^{-1}$$

$$\rho = \text{ice density} = 900 \text{ kg m}^{-3}$$

Equating (1) and (2) and using

$$Q = - \left(\frac{Kc\tau}{L} \right) \left(\frac{\lambda^2}{L^2} \right)$$

$$U_{slide} = \frac{\Delta x}{\Delta t} = \frac{Kc\tau}{\rho HL} \frac{\lambda^2}{L^2}$$

Regelation Demonstration



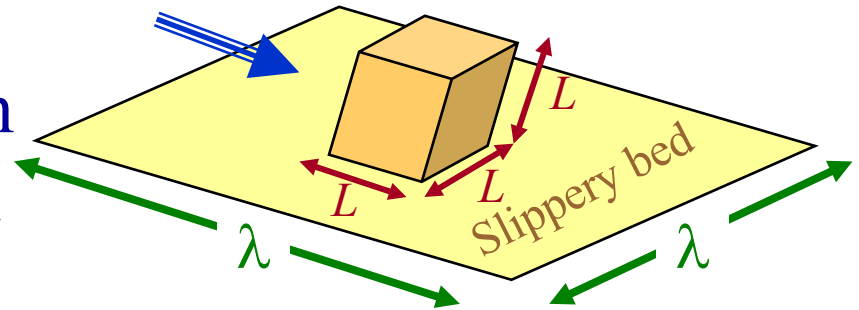
Example of sliding speed

$$U_{slide} = \frac{Kc\tau}{\rho HL} \frac{\lambda^2}{L^2}$$

If $L = 0.02 \text{ m}$

$\lambda = 0.2 \text{ m}$

$\tau = 10^5 \text{ Pa}$



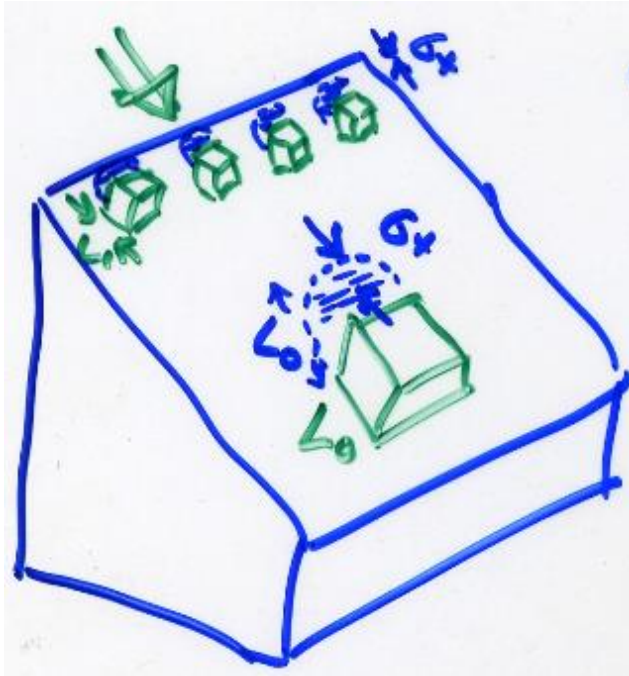
$$U_{slide} = \frac{2W \text{ m}^{-1} \text{ deg}^{-1} 7 \times 10^{-8} \text{ deg Pa}^{-1} 10^5 \text{ Pa}}{900 \text{ kg m}^{-3} 3.3 \times 10^5 \text{ J kg}^{-1} 0.02 \text{ m}} \frac{0.2^2 \text{ m}^2}{0.02^2 \text{ m}^2}$$

$$\approx 2 \times 10^{-7} \text{ m s}^{-1}$$

$$\approx 2 \times 10^{-7} \text{ m s}^{-1} \times 3 \times 10^7 \text{ s yr}^{-1} \approx 6 \text{ m yr}^{-1}$$

How will sliding speed change if bumps are bigger?

Can ice flow around bumps?



σ_x is compressive stress in ice upstream of bump

- Ice “knows” that bump is there for a distance $\sim L_0$ upstream

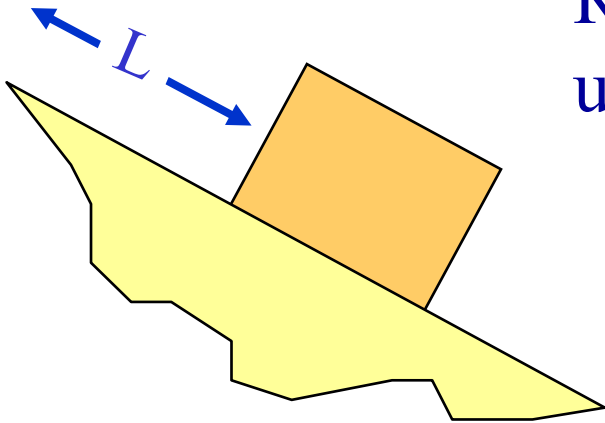
- one large bump stresses a bigger volume of ice compared to many smaller faces with the same total restraining face area (as required for force balance)

Ice deforms in response to stress
(Glen Flow Law)

$$\dot{\epsilon}_x = A \sigma_x^3$$

Strain near bumps

Rate of shortening of a line upstream from bump



$$\dot{\epsilon}_x = \left(\frac{\Delta L}{L} \right) \frac{1}{\Delta t}$$

$$U_{slide} = \frac{\Delta L}{\Delta t} = L \dot{\epsilon}_x = LA \sigma_x^3$$

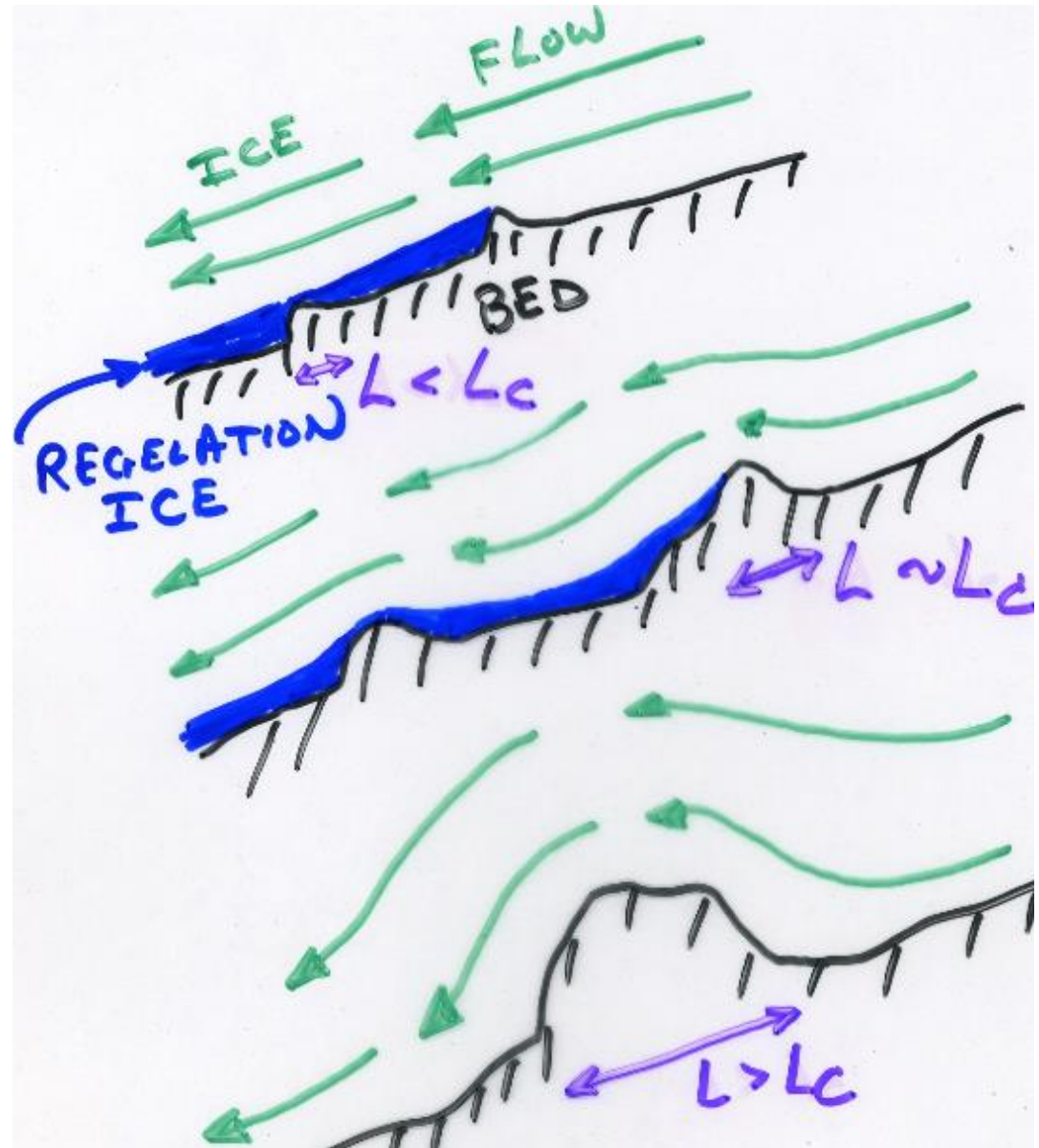
We used Glen flow law:
$$\dot{\epsilon}_x = A \sigma_x^3$$

Stress σ_x on 4 small bumps is the same as stress on 1 large bump.

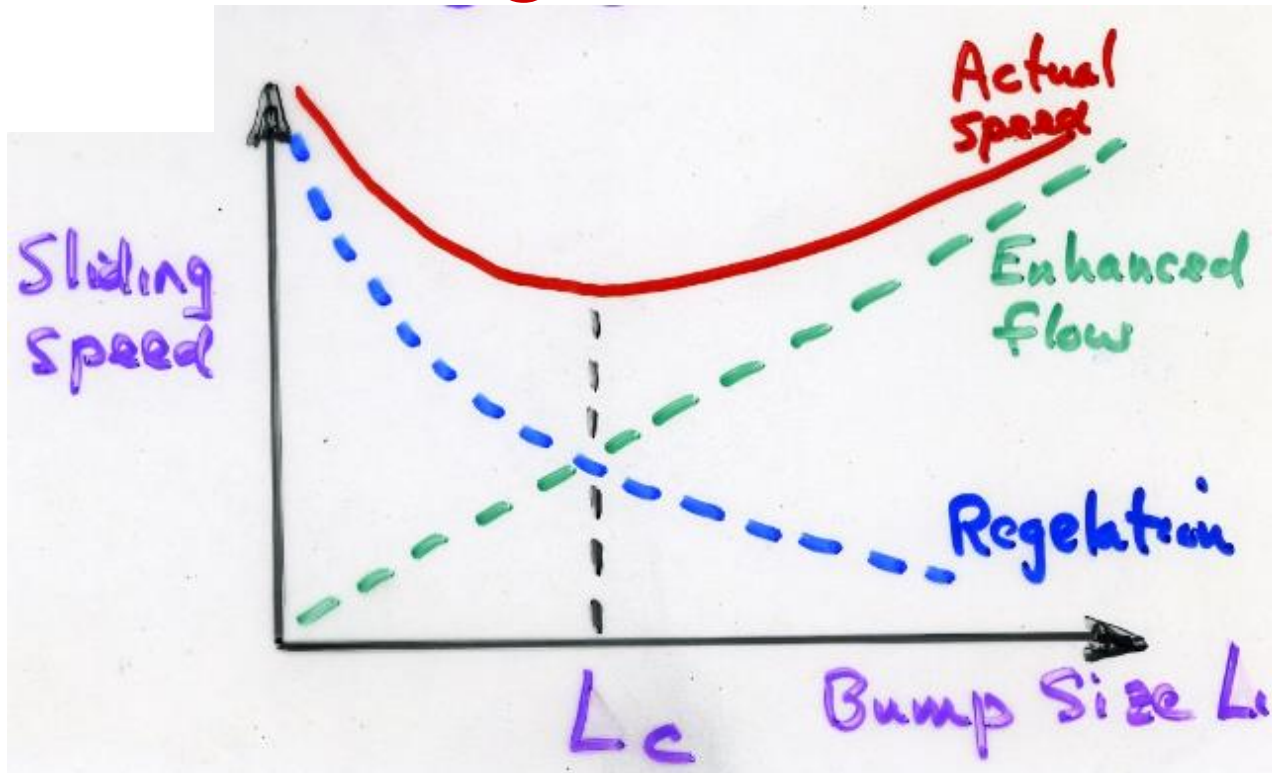
Ice can move faster around larger bumps

Regelation- Deformation Tradeoff

- Regelation allows ice to slide past small bumps easily.
- Enhanced strain gets ice past large bumps easily.
- At some intermediate scale $L=L_c$, both processes are equally effective (or ineffective).



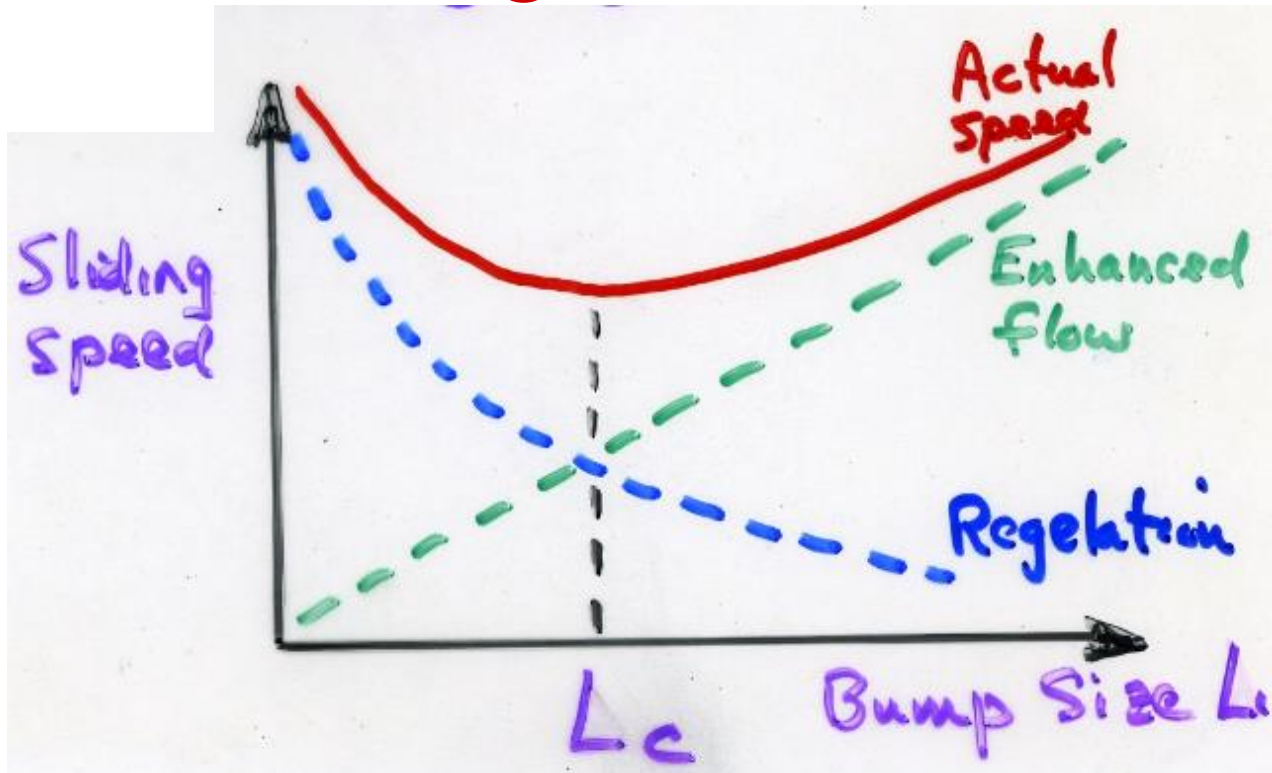
Controlling-Obstacle Size



- Actual sliding speed is sum of 2 processes
- At $L=L_c$, U_{slide} is minimum
- Bedrock bumps with size L_c control sliding speed.

What assumptions are built into this concept?

Controlling-Obstacle Size

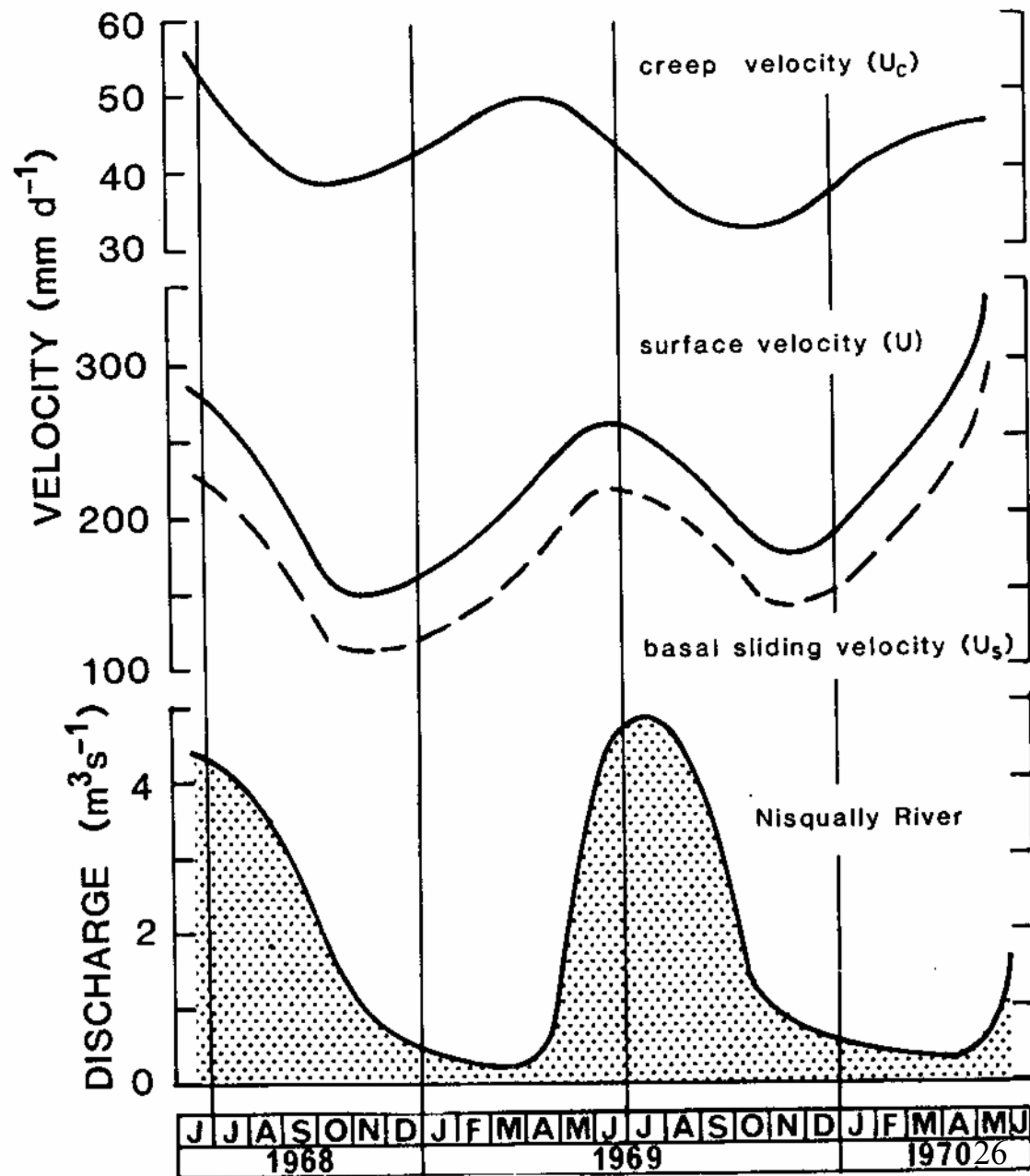


- Actual sliding speed is sum of 2 processes
- At $L=L_c$, U_{slide} is minimum
- Bedrock bumps with size L_c control sliding speed.

What assumptions are built into this concept?

Flow on Nisqually Glacier

Can Tombstone Model explain these data?

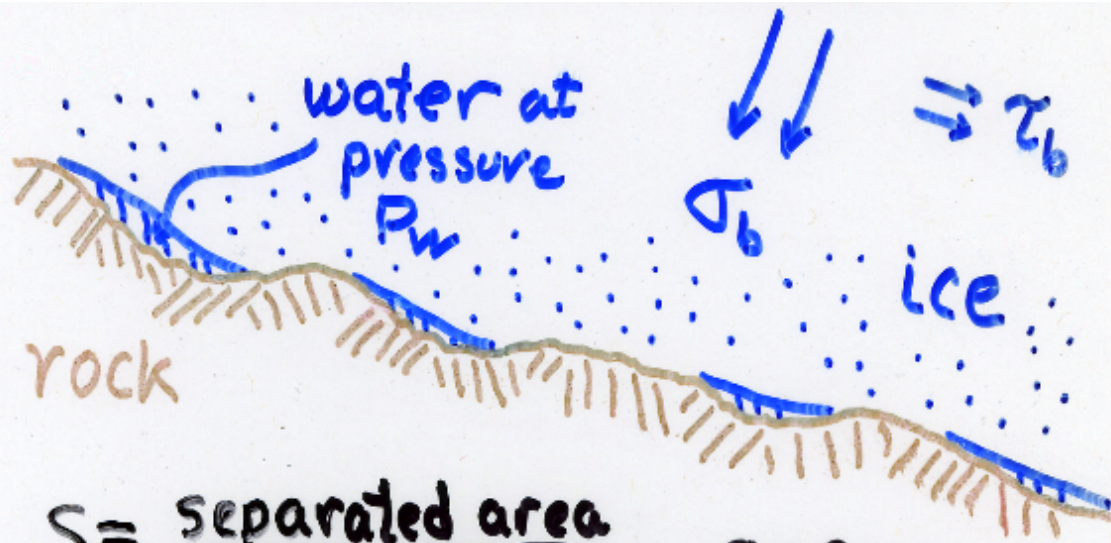


Based on Hodge, S.M. 1974
J. Glaciol. 13(69) 349-369.

Water is very important

- Meltwater from surface
- Meltwater from the bed
- Drainage through till?
- Water pressure
- What does water do in a glacier?

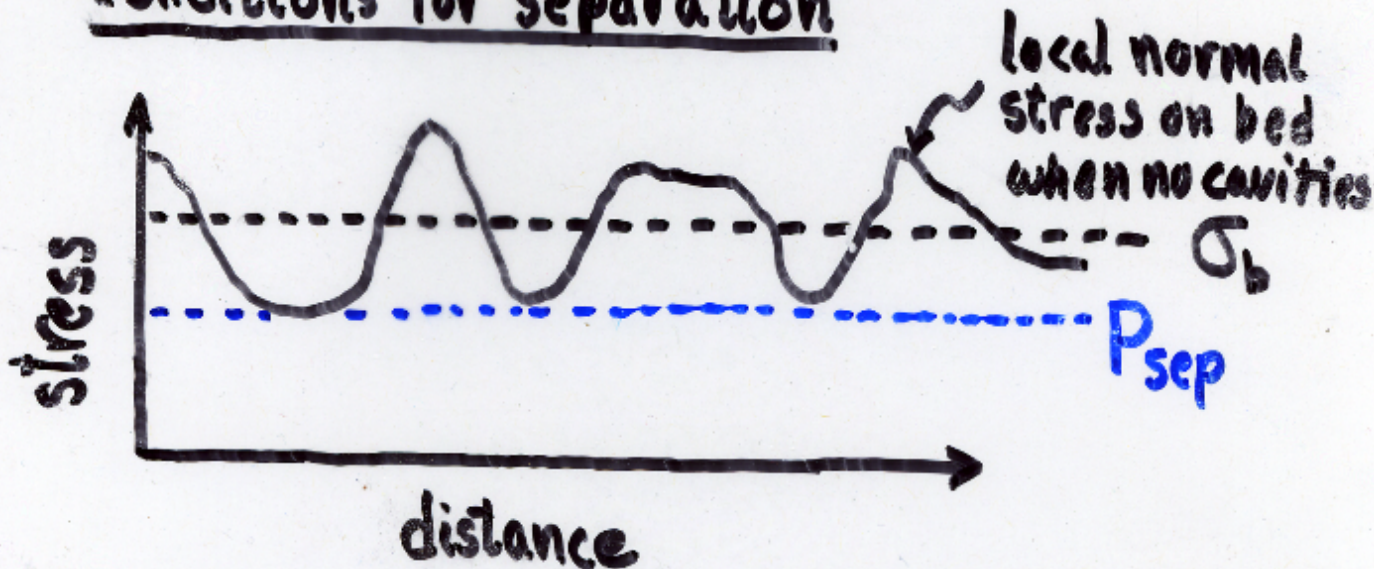
Bed Separation and Sliding



$$S = \frac{\text{separated area}}{\text{total area}}$$

$$0 \leq S < 1$$

conditions for separation



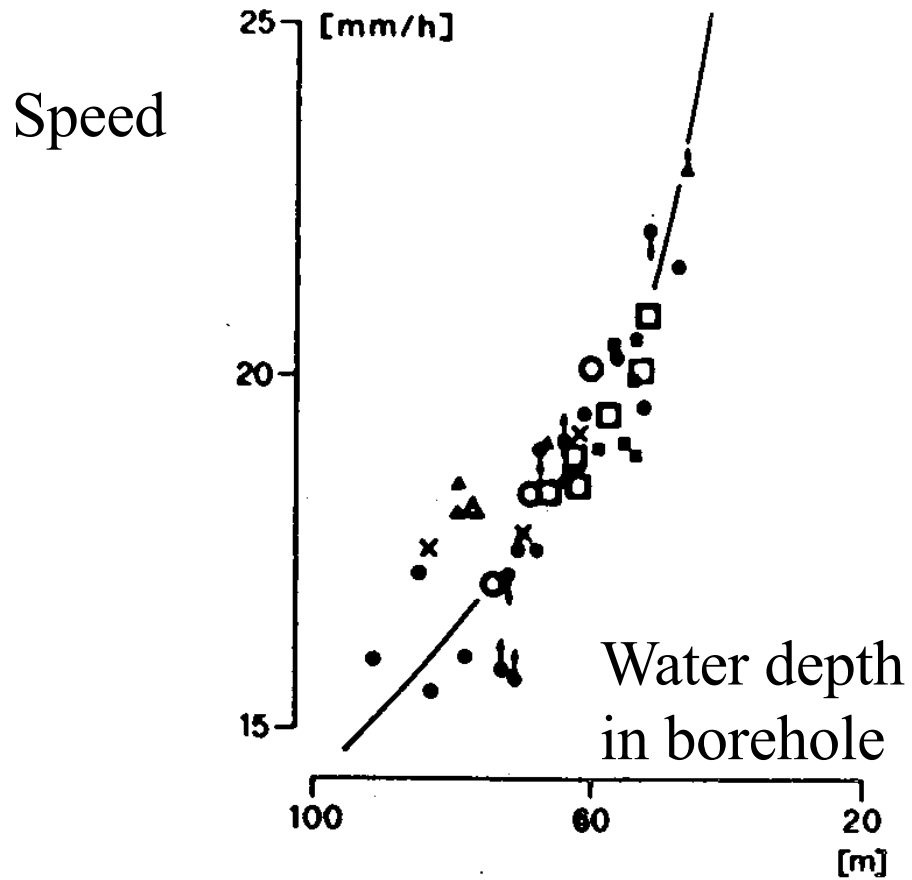
$$P_w < P_{sep}$$

- $S = 0$
- Cavities cannot form

$$P_w > P_{sep}$$

- $S > 0$
- Cavities can open

Sliding and Water Pressure



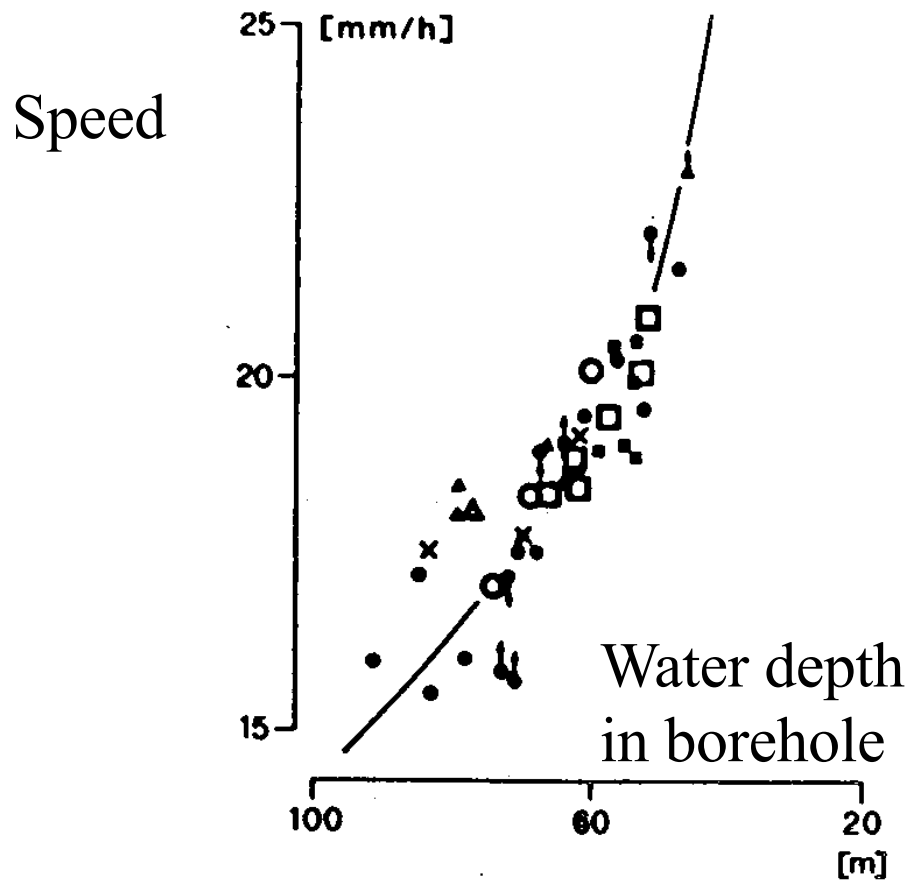
Glacier moves faster
when water level
rises in a hole to
bedrock

- Why?

- 15 - 30 May 1982
- ▲ 30 May - 4 June 1982
- 4 - 20 June 1982
- x 1980

(Almut Iken)

Sliding and Water Pressure



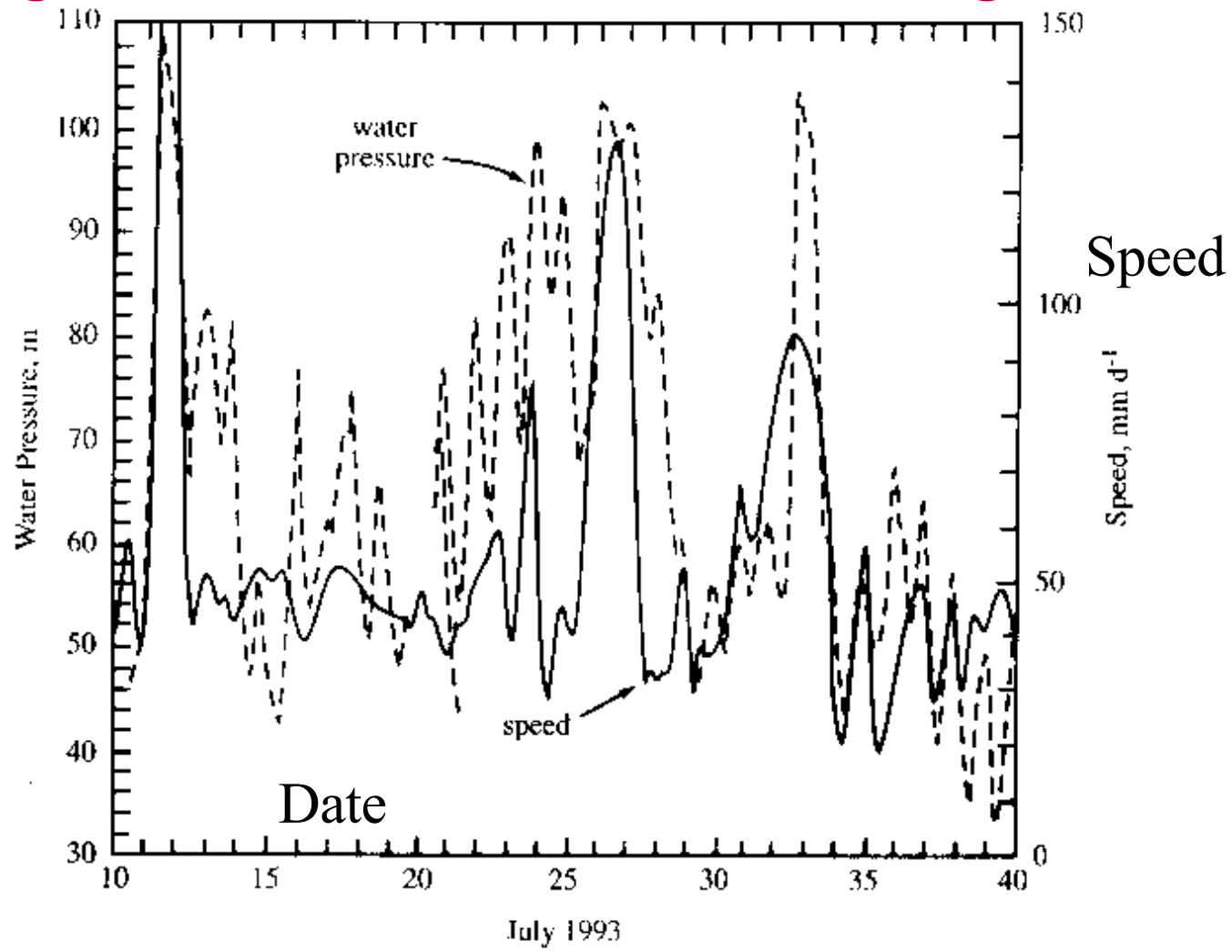
Glacier moves faster
when water level
rises in a hole to
bedrock

- Borehole is acting as a manometer; water level tells us about water pressure at the base of the glacier

(Almut Iken)

Sliding and Water Pressure - Storglaciaren

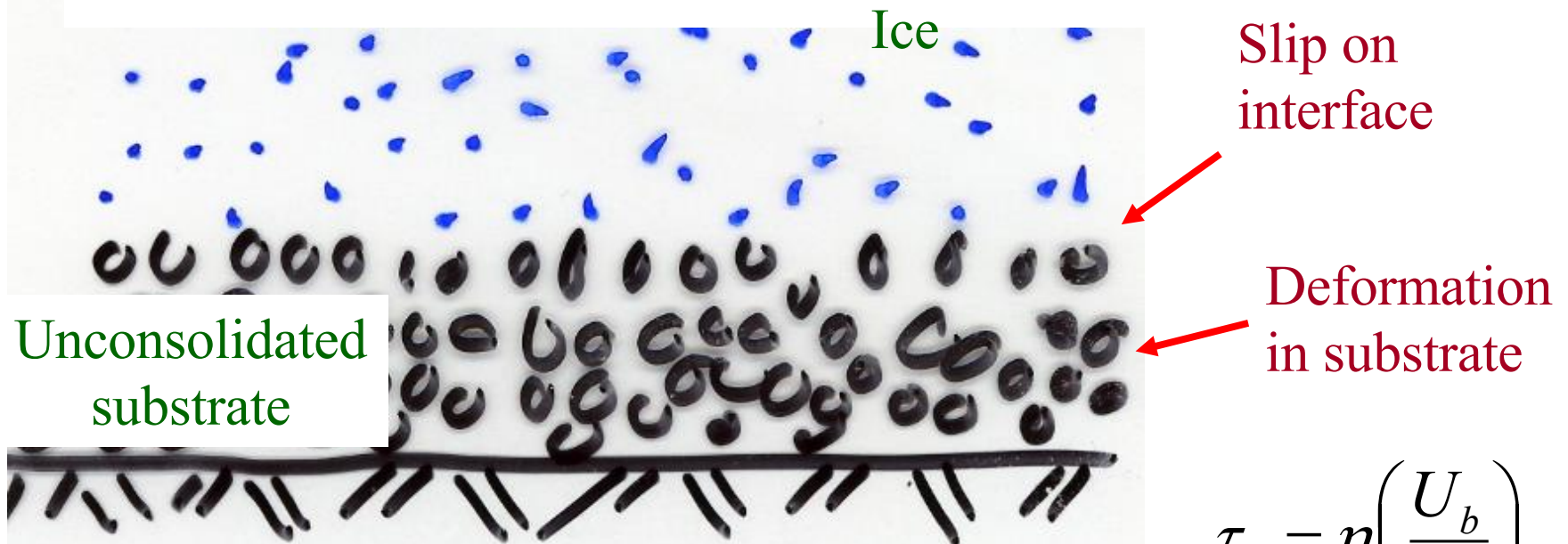
Water pressure



Only major pressure oscillations are clearly related to sliding changes

(Hanson et al., 1998. *J. Glaciol.* 44(147) 359)

Sliding and Soft Beds



Unconsolidated
substrate

Slip on
interface

Deformation
in substrate

$$\tau_b = \eta \left(\frac{U_b}{h} \right)$$

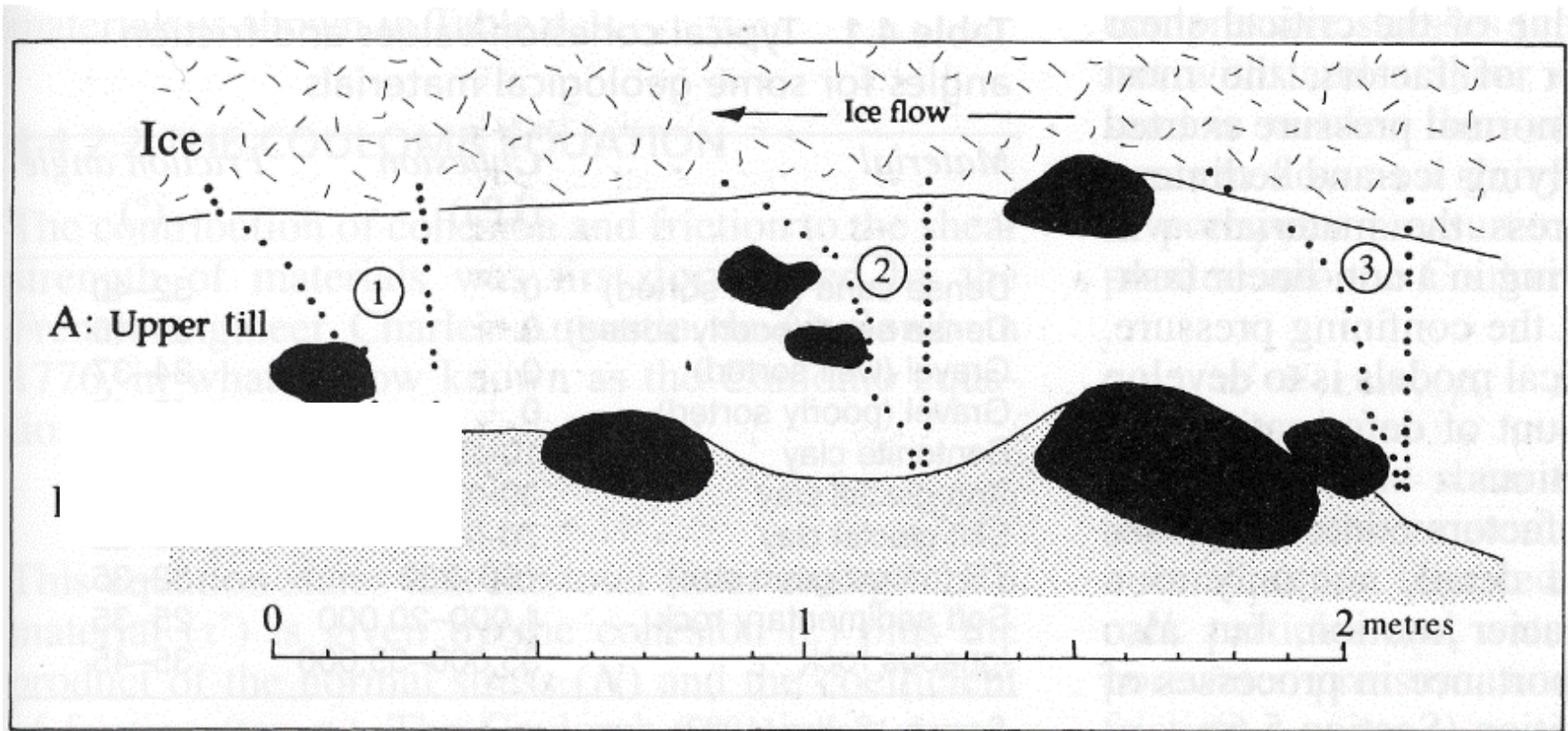
Factors:

- Thickness h and composition of material (till viscosity η)
- Pore-pressure distribution

$$U_b = \frac{h}{\eta} \tau_b$$

But ... what is viscosity η ???

Deformable Bed in Iceland



Breiðamerkerjökull, Iceland

- Segmented rods left in subglacial till were moved forward by glacier over 10 day interval.

(Benn and Evans, *Glaciers and Glaciation*, adapted from Boulton and Hindmarsh)

Rock Friction

Rocks
pressed
against bed

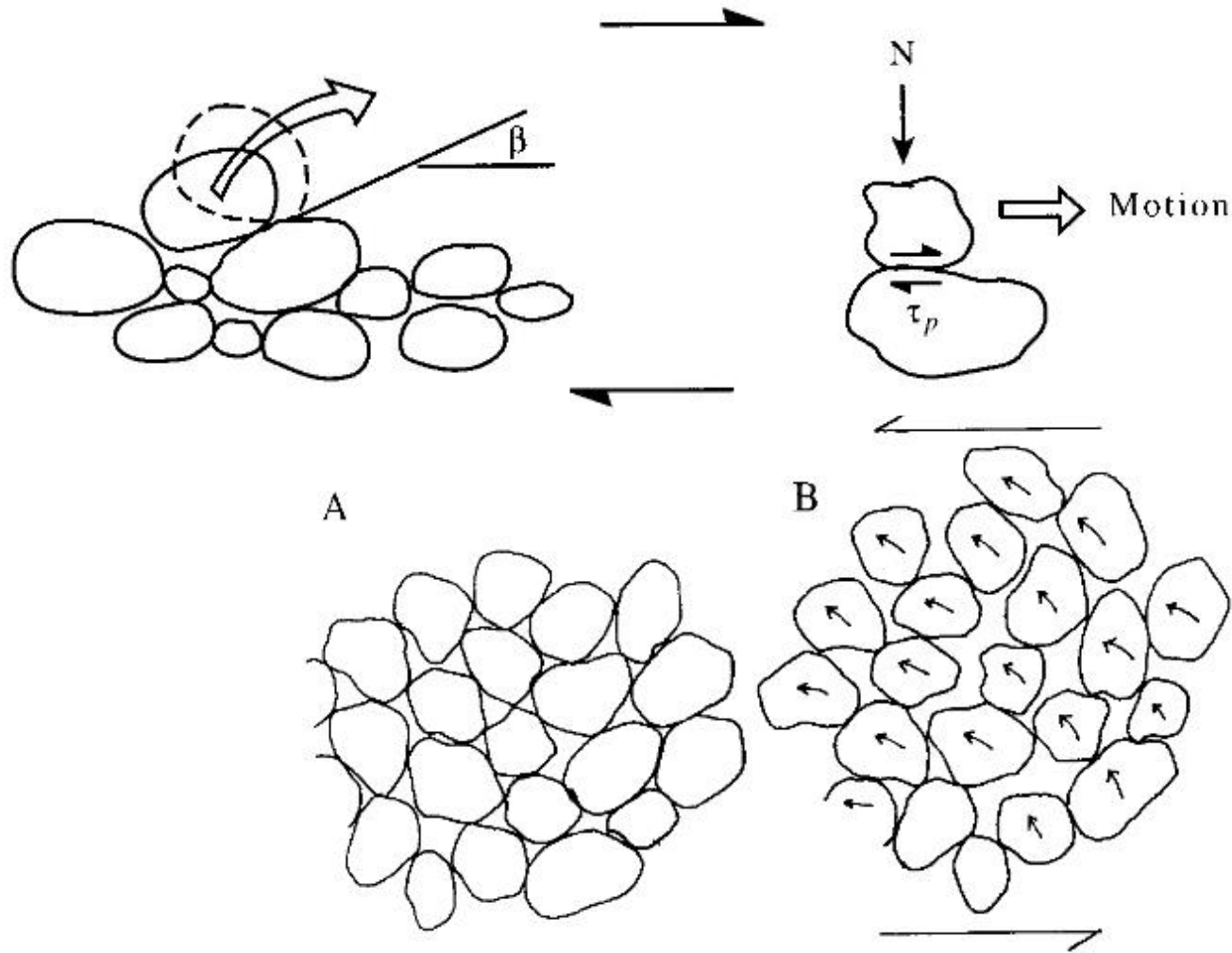


Pressure
difference

Water pressure
reduces rock-to-rock
friction

Geothermal
flux

Rock Friction – Till Dilation



- Till must swell so that clasts can move past one another

- Water at high pressure helps to dilate till

(Hooke, *Fundamentals of Glacier Mechanics*;
Benn and Evans, *Glaciers and Glaciation*)

Questions, Questions, Questions ...

1. Can speed U_d due to internal deformation change rapidly?

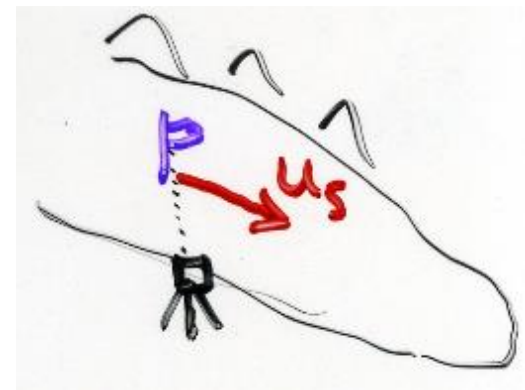
- Consider hours, days, seasons.

2. Can sliding speed U_b change rapidly, e.g. in a few hours?

- Consider Tombstone model, Deforming-till model, (others?)

3. You are measuring the surface speed U_s of a pole in the center of a glacier in the Cascades. You just had the hottest 3 days of the summer.

What might happen to U_s ?



Today's Objectives:

Basal Sliding:

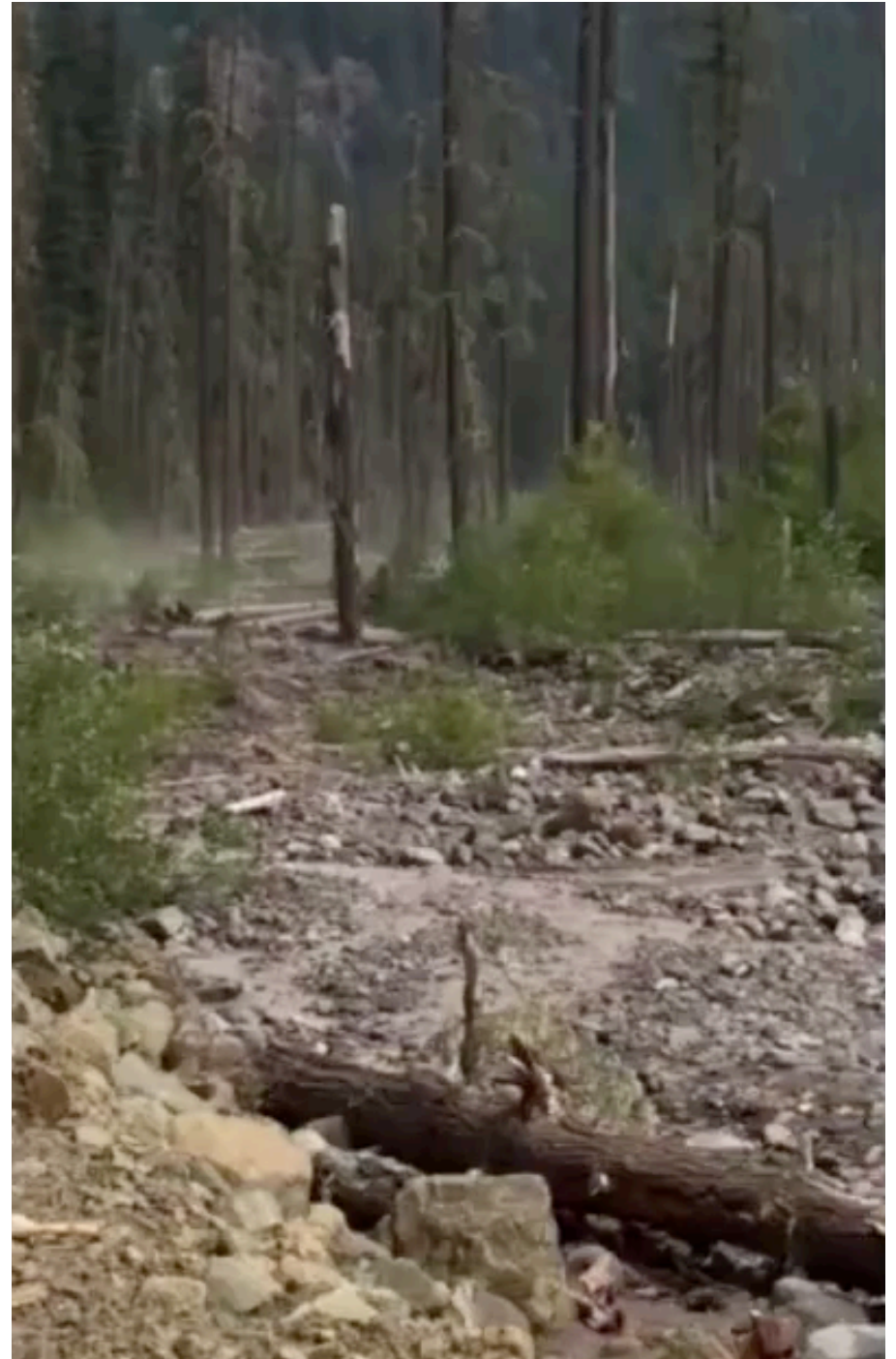
- What are the controls on basal sliding? How do they compare with the physics of internal deformation?
- What are the two dominant processes that allow sliding past bed features? What is the role of water in each process?

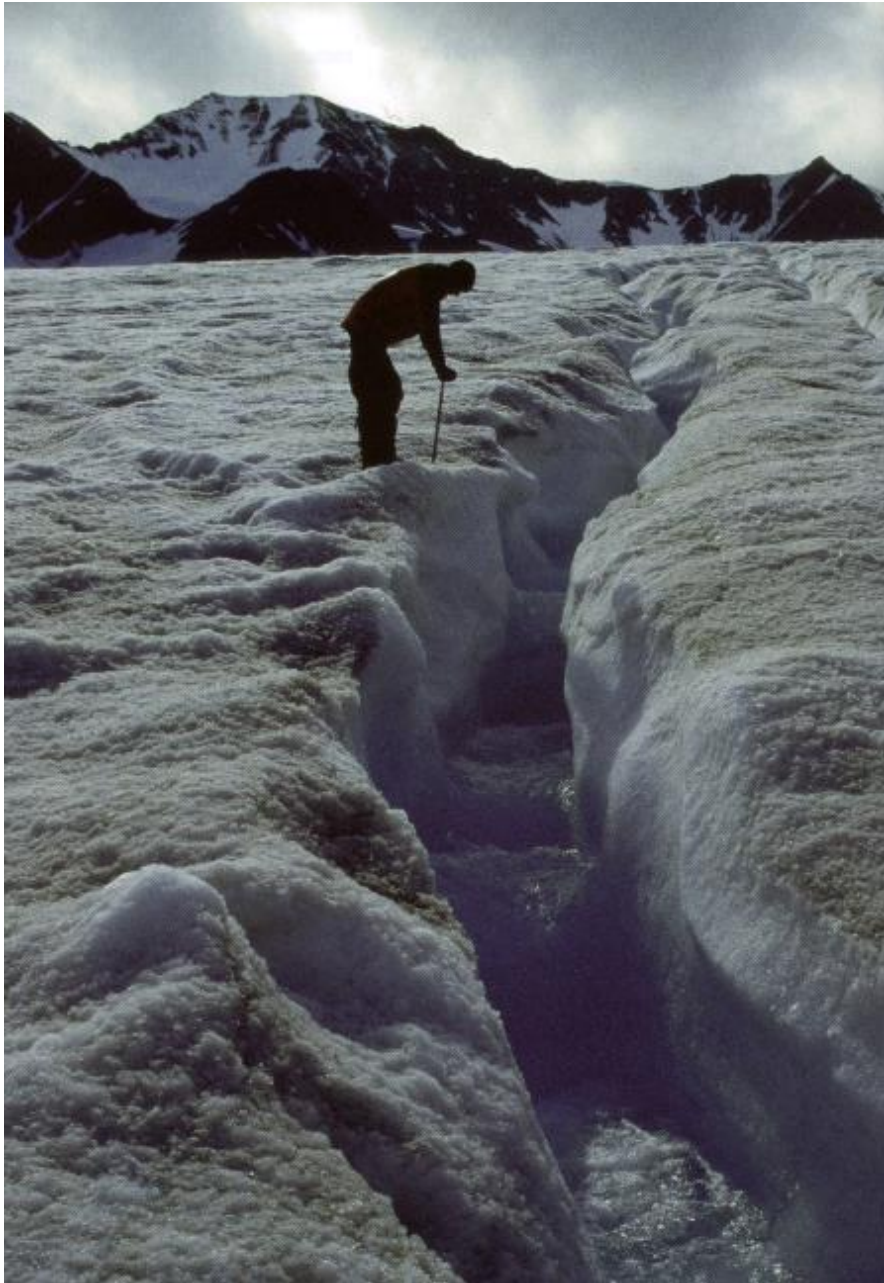
Hydrology:

- How is water transported in a glacial system?
- How does the amount of water in the system affect the water transport regime?

Glacial Outburst Flooding

- South Tahoma Glacier, Mount Rainer, WA, USA
- Since 1985, over 30 have occurred





Streams on Glaciers

Water can melt channels into glacier ice

- Lower albedo than ice
- Dissipating potential energy as it loses elevation

Austre Lovenbreen, Spitsbergen
Hambrey and Alean. *Glaciers*.

Rivers on the Greenland Ice Sheet

Vibeke Gletscher,
East Greenland

An opportunity to
go rafting?
Not a good idea...



← ~300 m →

40

Hambrey and Alean, *Glaciers*.

Moulins

Water will find a way to move down into a glacier

- a supraglacial stream will typically flow into a crevasse









Tunnels



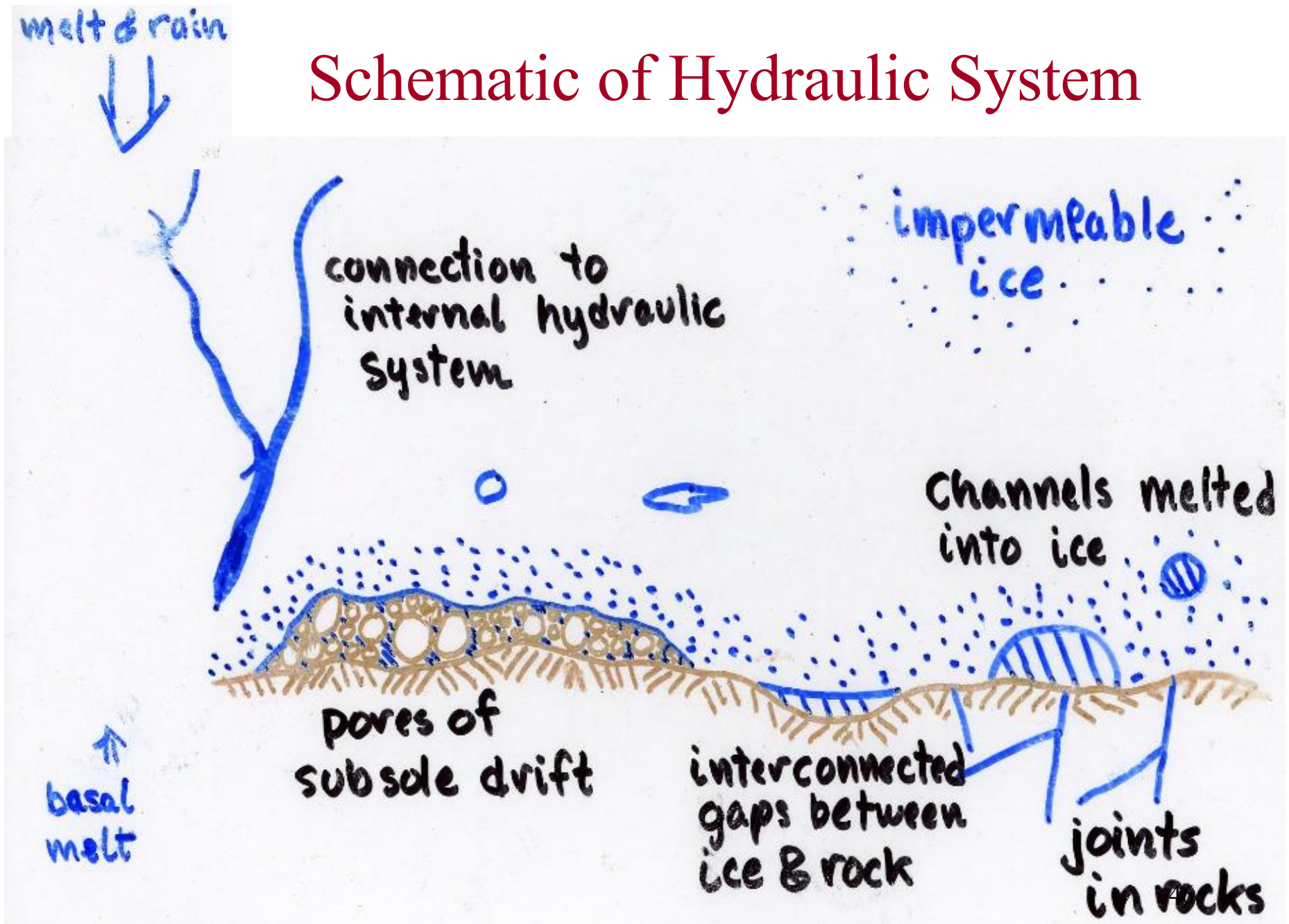
We can see the water coming out at a glacier terminus

- But where has it been?

Fox Glacier, NZ.

Hambrey and Alean. *Glaciers*.

Schematic of Hydraulic System



Tunnels in Winter

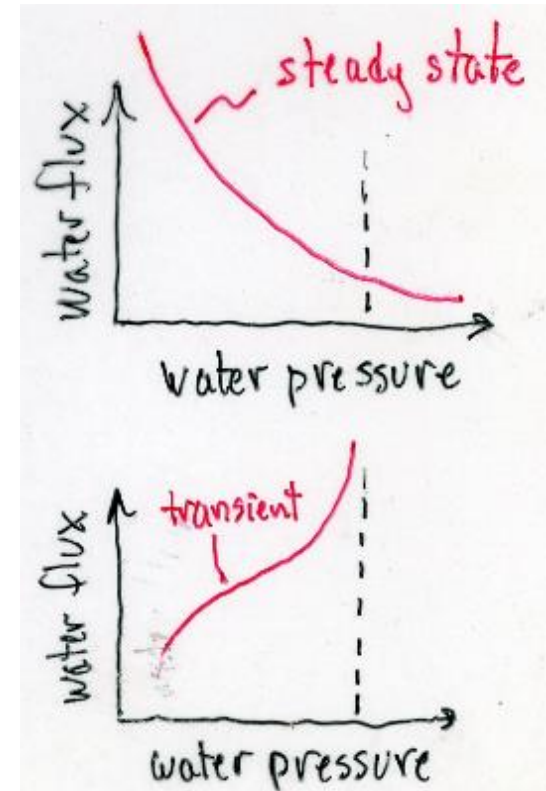
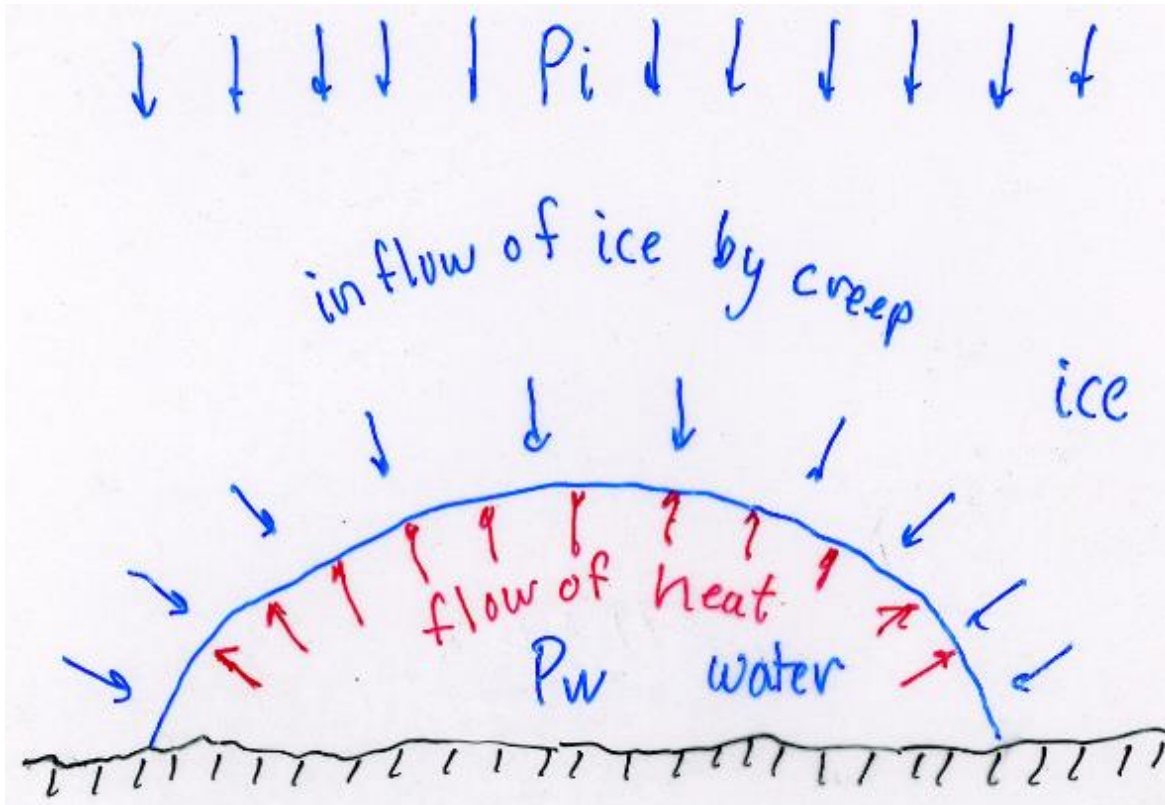


Water can stop flowing in winter

- where does a tunnel lead?
- What happens over the winter?

Matanuska Glacier.
Andersen and Borns.
Ice Age World. 47

Tunnels Transporting Water



Rothlisberger (1972)
Nye (1976)

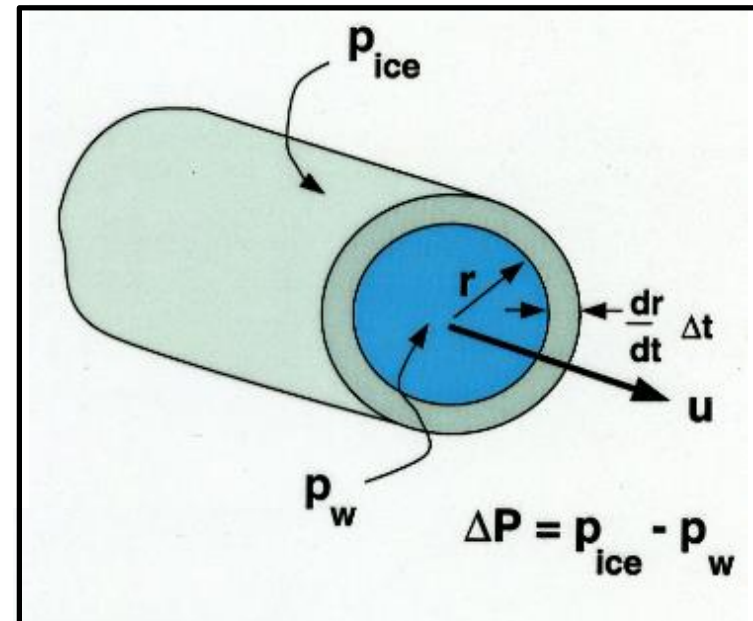
In steady state, higher water pressure \leftrightarrow lower water flux (in smaller tunnel)

Pressure in Steady Tunnels

Two competing influences:

- Creep closure of the tunnel, through ice deformation
- Tunnel growth, through melting from turbulent heat transfer

Creep Closure:



Pressure in Steady Tunnels

Two competing influences:

- Creep closure of the tunnel, through ice deformation
- Tunnel growth, through melting from turbulent heat transfer

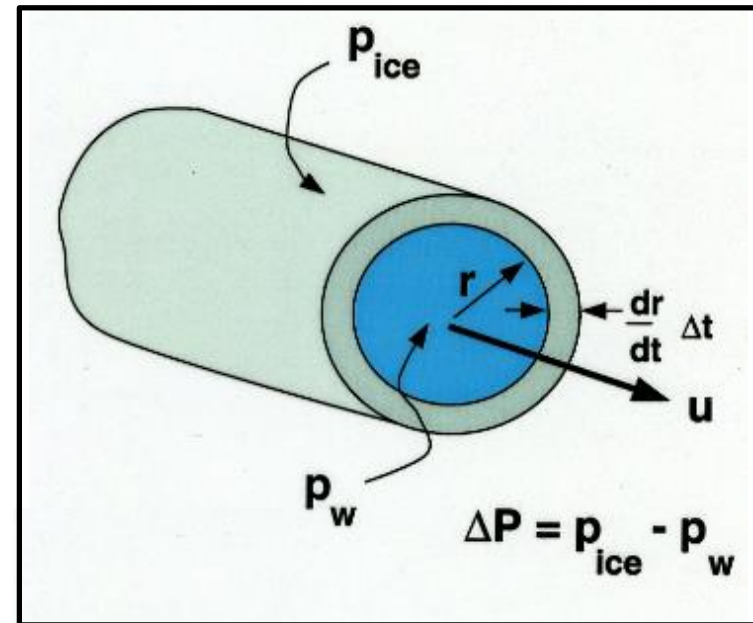
Creep Closure:

$$\dot{\epsilon} = A\sigma^3$$

$$\hookrightarrow \frac{1}{r} \frac{\Delta r}{\Delta t} \approx A[p_i - p_w]^3$$

$$\hookrightarrow \frac{\Delta r}{\Delta t} \propto \Delta p^3$$

$$\boxed{\frac{\Delta V}{\Delta t} \propto 2\pi r \Delta p^3}$$



Pressure in Steady Tunnels

Two competing influences:

- Creep closure of the tunnel, through ice deformation
- Tunnel growth, through melting from turbulent heat transfer

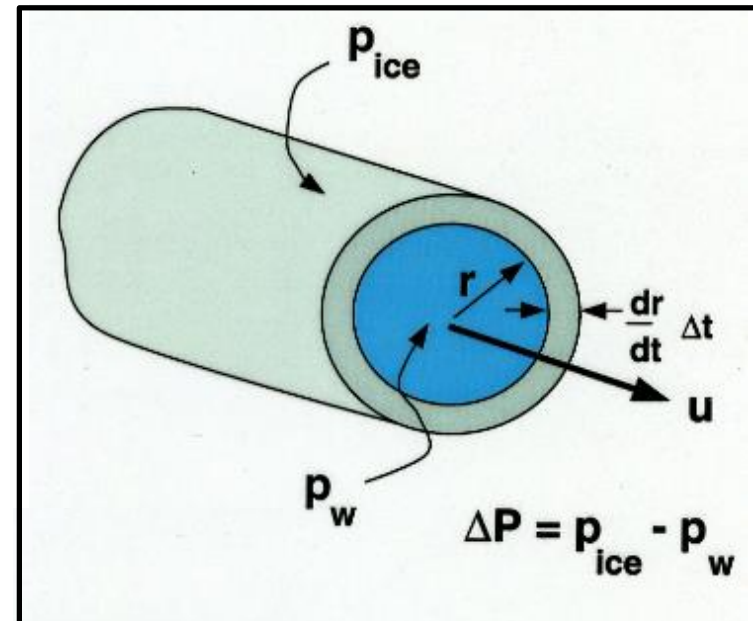
Turbulent Melting:

$$\frac{\Delta V}{\Delta t} \propto \frac{\Delta E}{\Delta t} \propto Q$$

$$Q = \pi r^2 u$$

$$u \propto r^{2/3} \text{ - (pipe flow theory)}$$

$$\frac{\Delta V}{\Delta t} \propto r^{8/3}$$



Pressure in Steady Tunnels

Two competing influences:

- Creep closure of the tunnel, through ice deformation
- Tunnel growth, through melting from turbulent heat transfer

Creep

$$\frac{\Delta V}{\Delta t} \propto r \Delta p^3$$

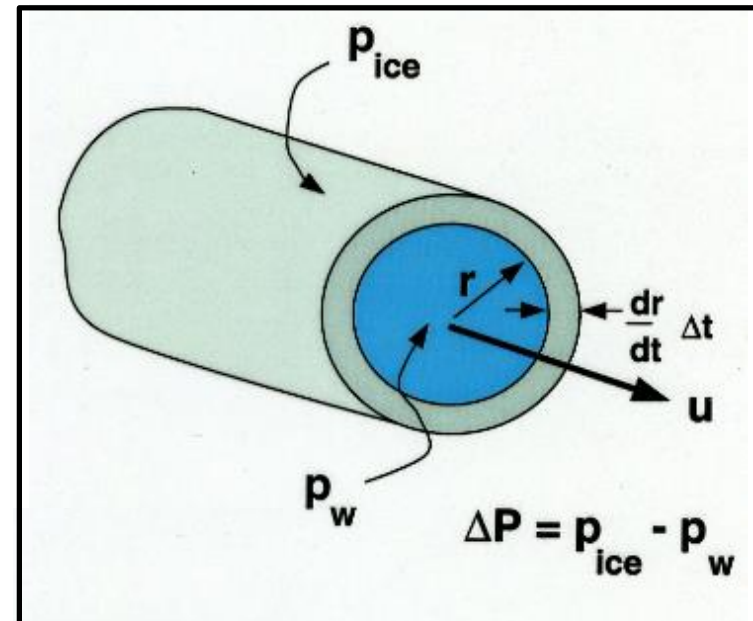
$$\Delta p \propto r^{2/9}$$

Melt

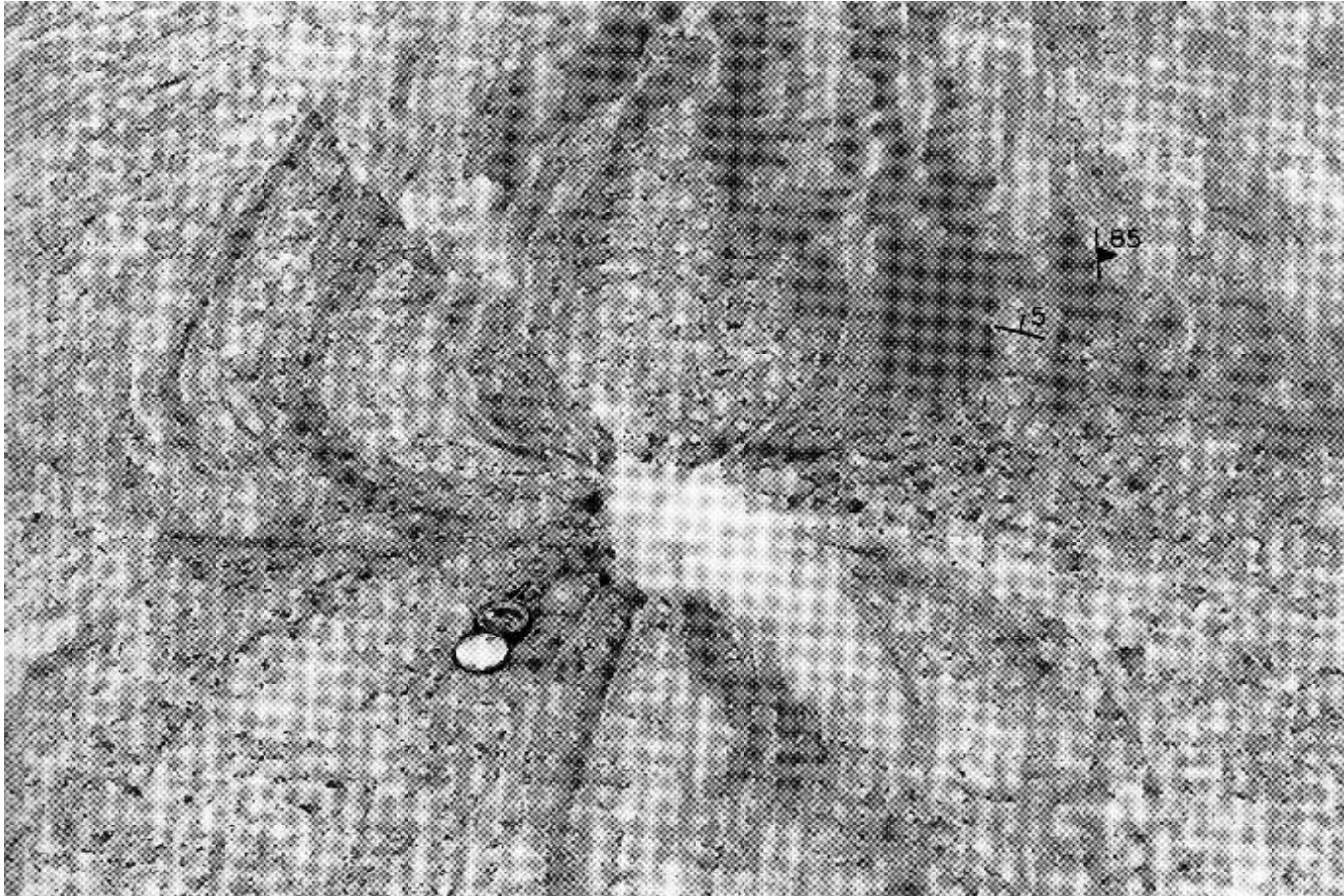
$$\frac{\Delta V}{\Delta t} \propto r^{8/3}$$

$$\Delta p \propto Q^{1/12}$$

As radius grows, Δp grows,
 p_w falls



Under-pressurized conduit

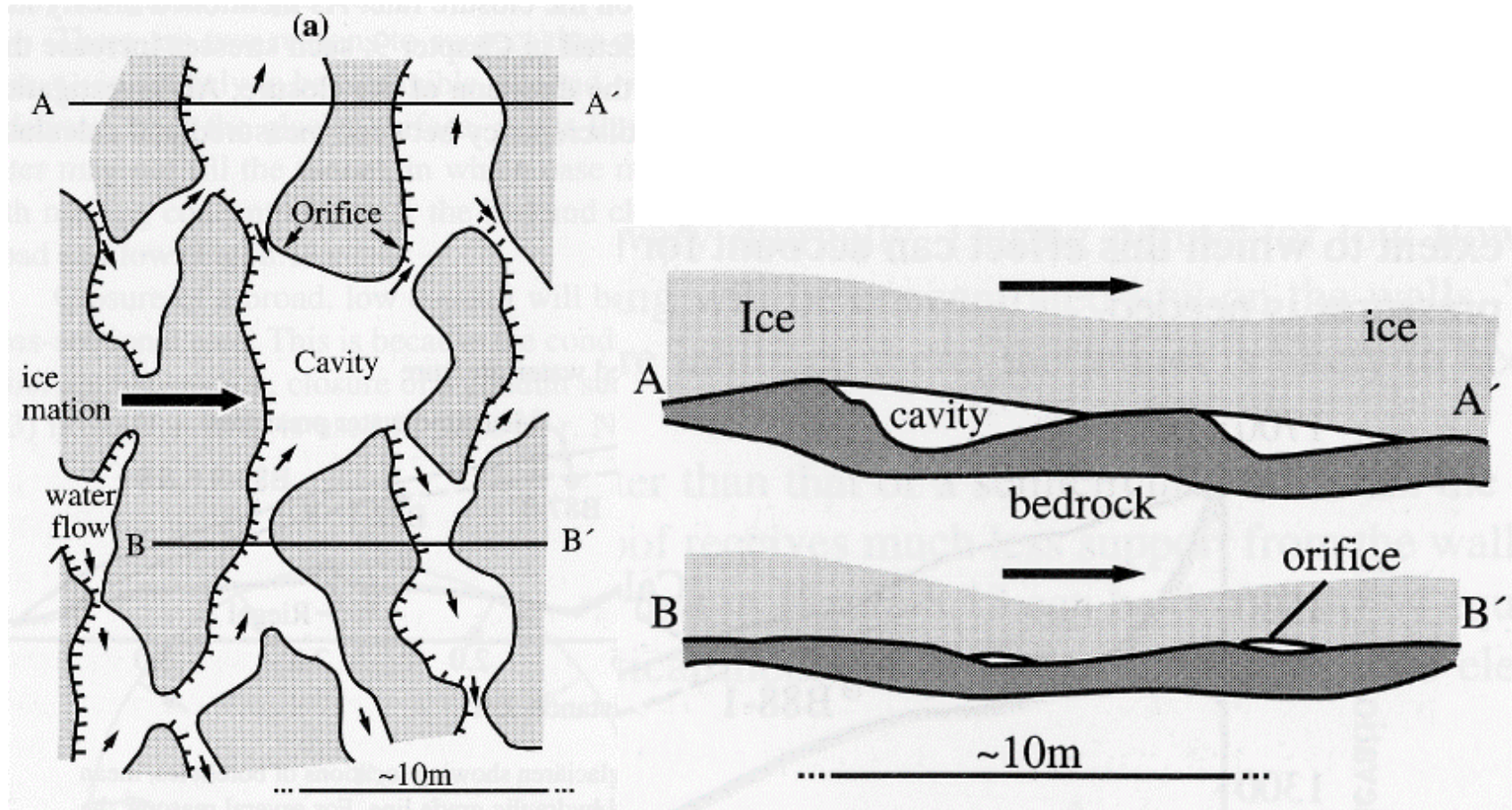


Brunton
compass
for scale

It did not survive when water flow stopped ...

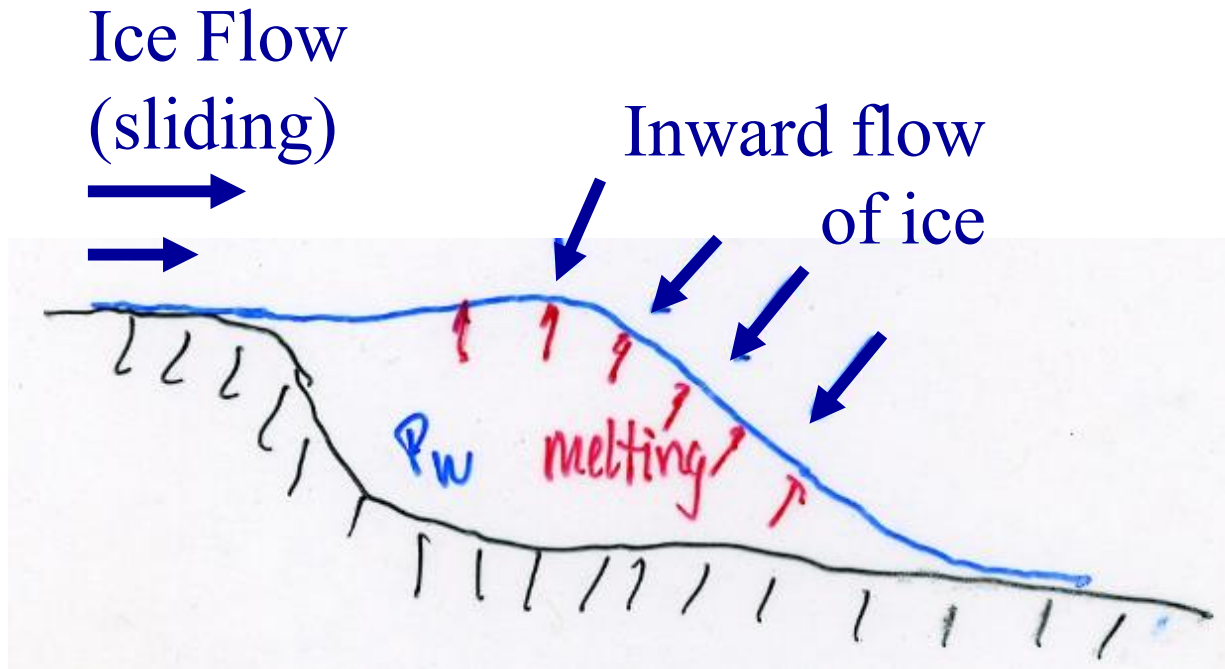
(Hooke, *Fundamentals of Glacier Mechanics*)

Linked Cavities

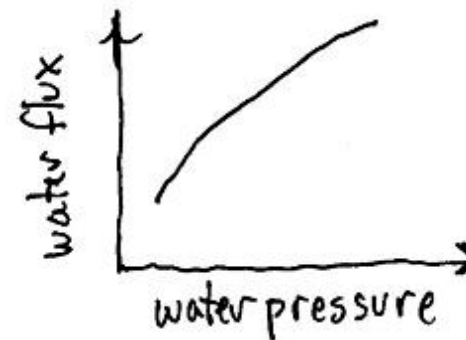


(Hooke, *Fundamentals of Glacier Mechanics*⁵⁴)

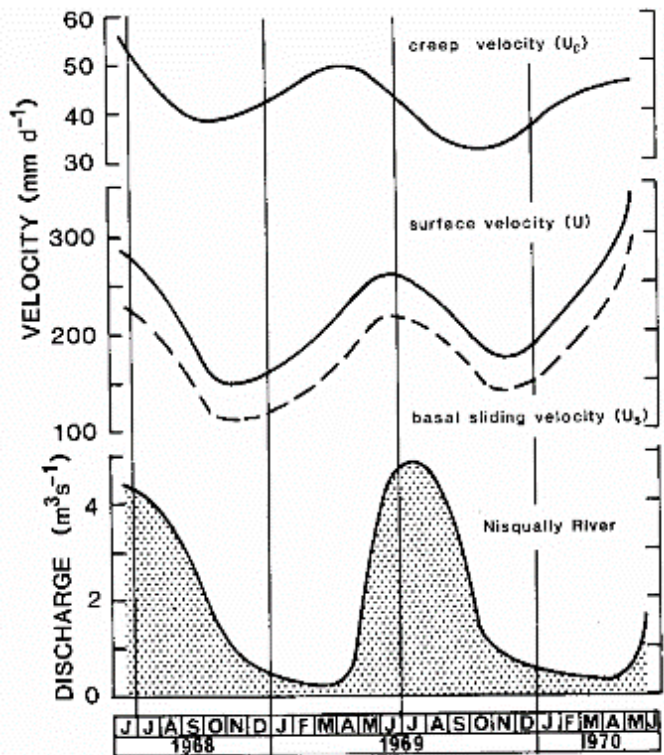
Water in Linked Cavities



Higher water pressure
↔ higher water flux (transport)



Seasonal Water Cycle



Early winter: little meltwater, low water pressure

- Tunnels close, linked cavities survive

Late winter: seepage, basal melt

- water pressure rises slowly
- Sliding increases slowly

Spring: high meltwater flux enters cavities

- Water pressure rises
- Sliding increases slowly

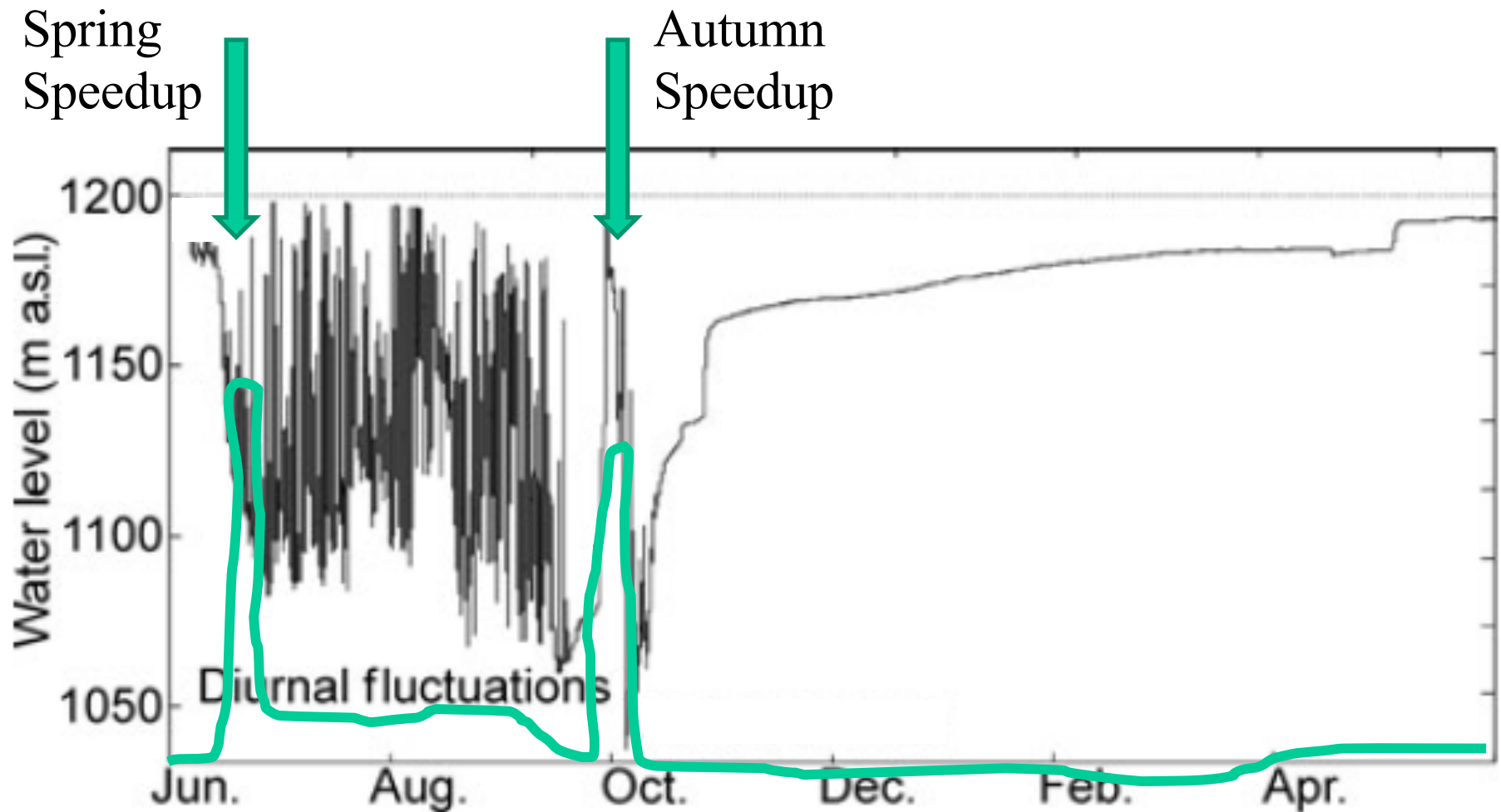
Early summer: too much water overloads cavities

- Surface rises
- Cavities join, tunnels start to form
- Sliding hits its peak

Mid-summer: water flows in low-pressure tunnels

- Basal water drains
- Sliding slows down

Seasonal Water Cycle

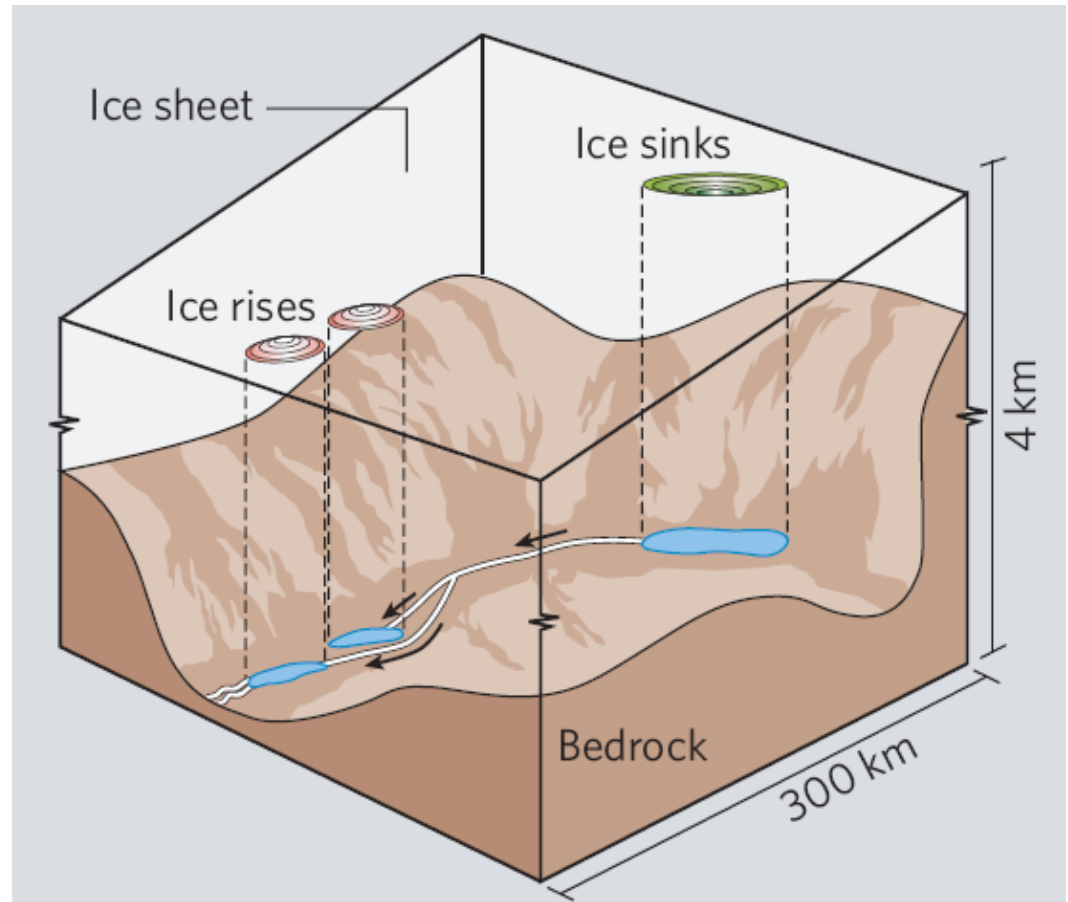


Water Pressure Variations on Bench Glacier, Alaska, 2002-2003 (Fudge et al, 2008)

Water moving in Antarctica

Recent work suggests large volumes of transient water can move under the ice.

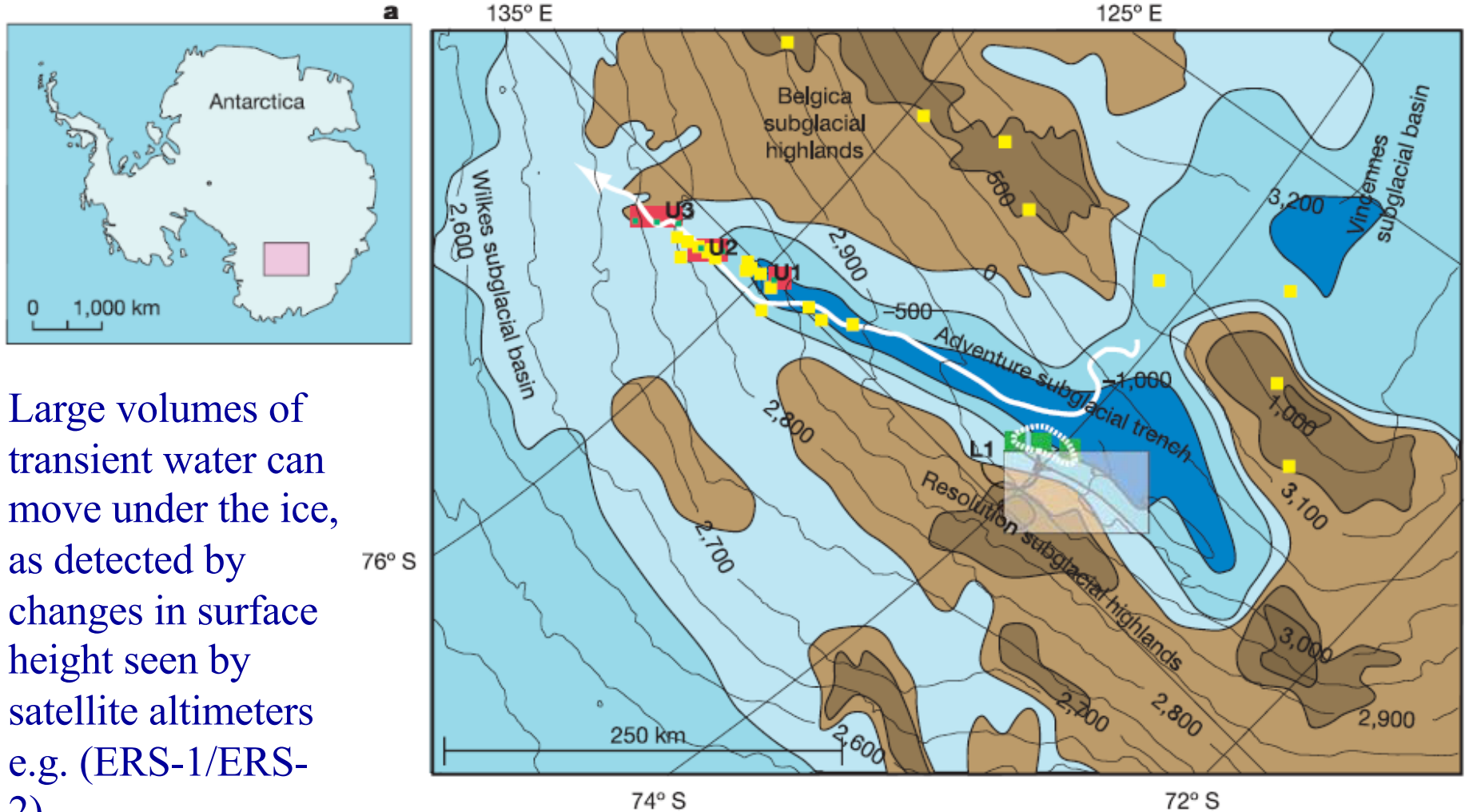
- $\sim 2 \text{ km}^3$ moved $\sim 300 \text{ km}$ beneath the ice sheet between 1996 and 1999.



Satellite data showed ice sinking above one subglacial lake, while rising at two spots 290 km away.

The researchers conclude that water must have flowed from the first lake into two others downstream. 58

Water moving in Antarctica



Large volumes of transient water can move under the ice, as detected by changes in surface height seen by satellite altimeters e.g. (ERS-1/ERS-2).

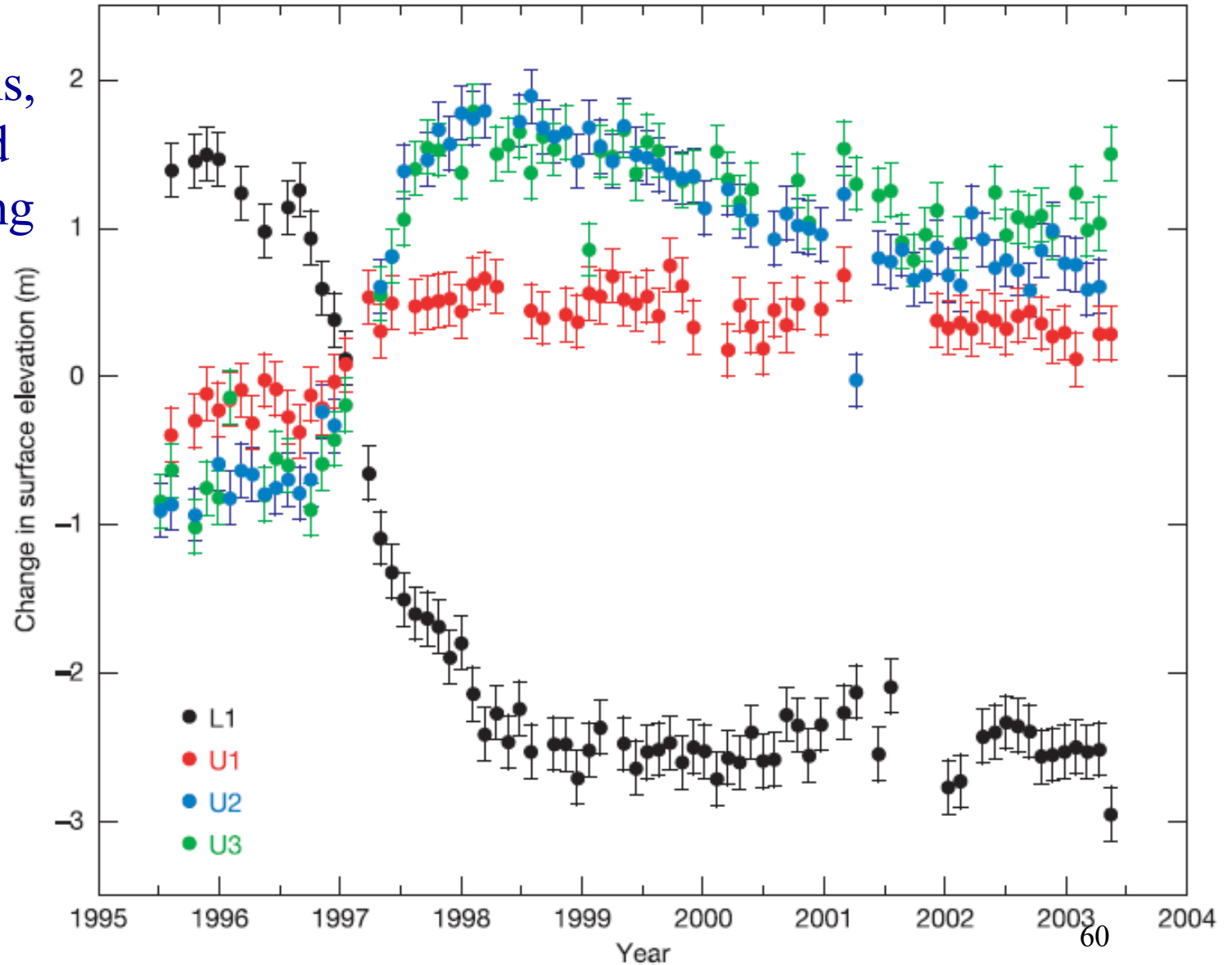
Wingham et al. (2006)
Nature **440**, 1033.

subglacial lakes - Yellow dots
- white dashes

L sites –lowering
U sites - rising

Surface Height Changes over Subglacial Lakes

As L1 drains,
U1, U2, and
U3 are filling
up.

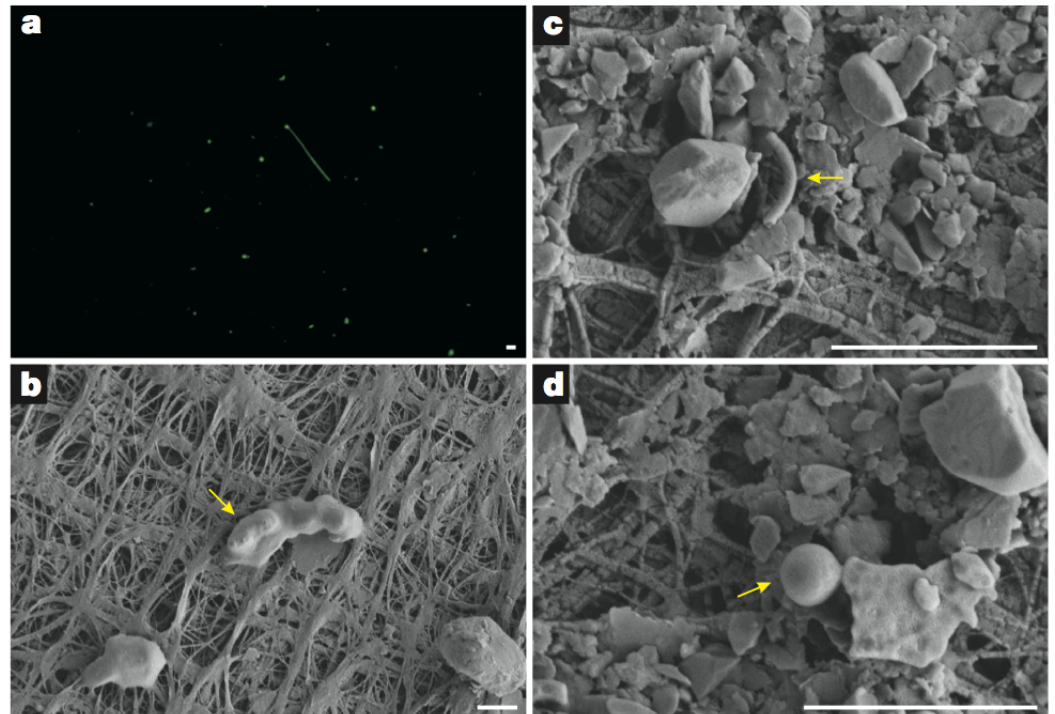
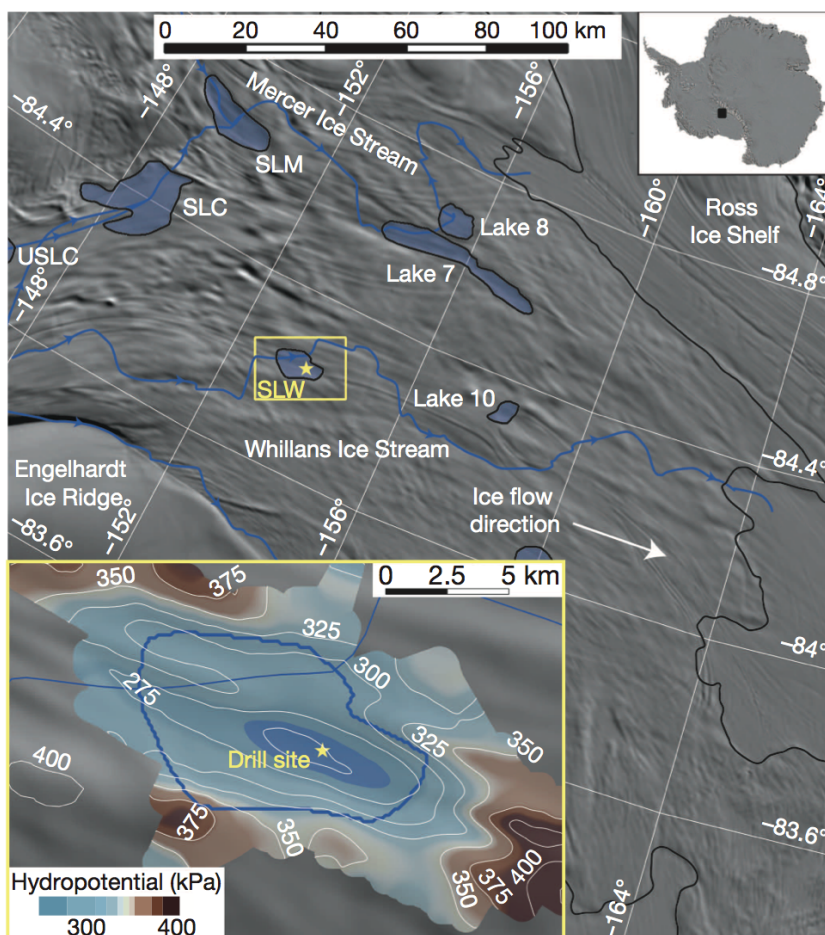


Wingham et al.
(2006) *Nature*
440, 1033.

Subglacial Lakes: Like Beneath the Ice

A microbial ecosystem beneath the West Antarctic ice sheet

Brent C. Christner¹, John C. Prisco², Amanda M. Achberger¹, Carlo Barbante³, Sasha P. Carter⁴, Knut Christianson⁵†, Alexander B. Michaud², Jill A. Mikucki⁶, Andrew C. Mitchell⁷, Mark L. Skidmore⁸, Trista J. Vick-Majors² & the WISSARD Science Team‡



Christner et al. (2014), *Nature* **512**, 310.

Christianson et al. (2012), *EPSL* **331-332**, 237.

Horgan et al. (2012), *EPSL* **331-332**, 201. ⁶¹

Sliding Summary

- Negligible sliding if base is cold
- Sliding is typically comparable to internal deformation in temperate valley glaciers
but
- Sliding can be up to 500-1000 m a⁻¹ over slippery beds of large glaciers (e.g. West Antarctic Ice Streams)

Sliding depends on water

- Lubrication
- Regelation
- Bed separation (high water pressure)

Water can flow

- Through distributed linked cavities (high-pressure system)
- Through tunnels (low-pressure system)
- Through subglacial sediments

Sliding can change rapidly with changing bed conditions

Questions, Questions, Questions ...

1. Why do some glaciers speed up in late winter or early spring before there has been much melting?

- Why do they slow down in mid-summer when melting is at its peak?

2. Describe the pressure gradient in the conduit.

- Which way does the water flow?

3. Water is bubbling out of a crack in a glacier. The water is at the melting temperature.

- Some ice crystals are swept upwards by the flow. What has been happening to them on the way up?

