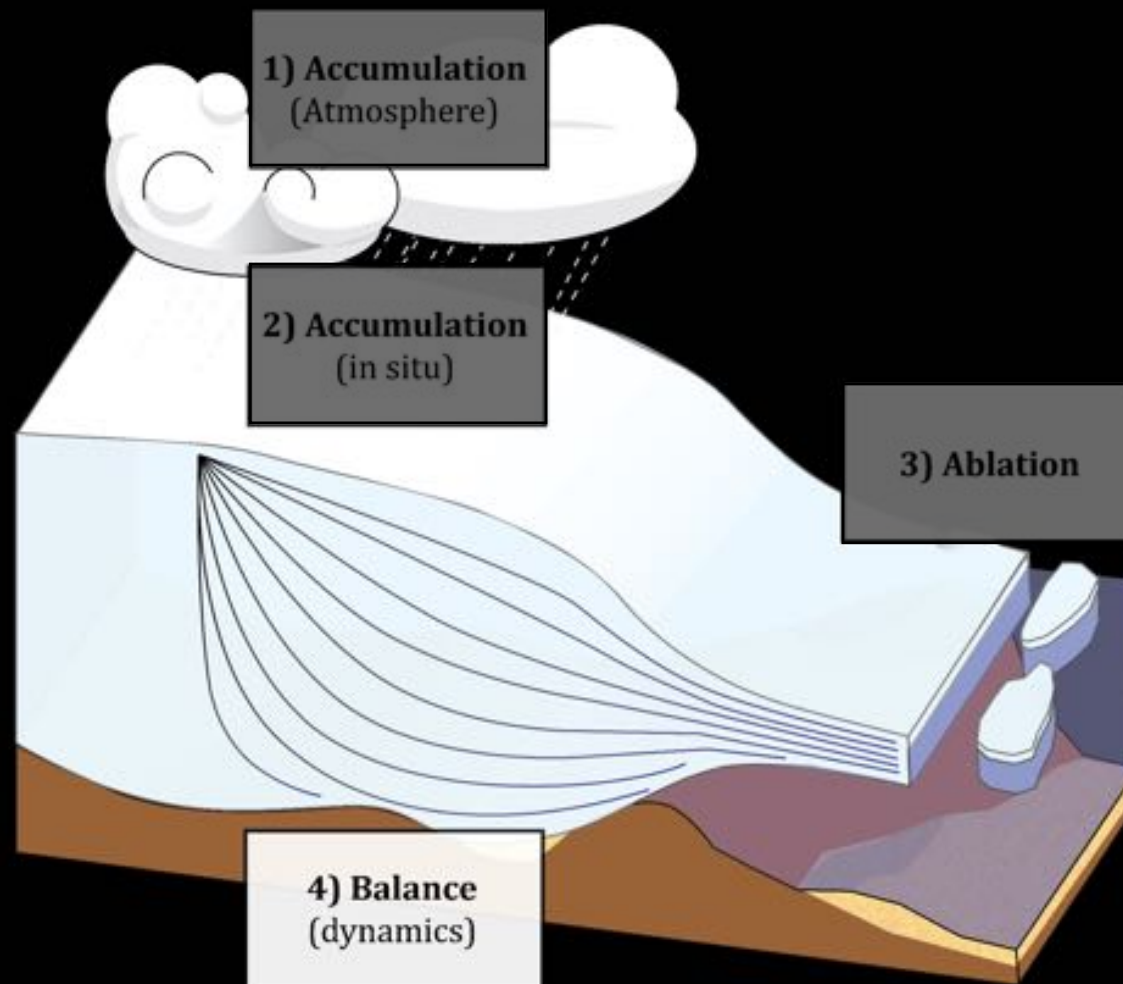


Ice Dynamics II: Glacier Sliding and Hydrology

ESS431: Principles of Glaciology

ESS505: The Cryosphere

Monday, 10/22 – Knut Christianson



Ice Avalanche

NASA Earth Observatory

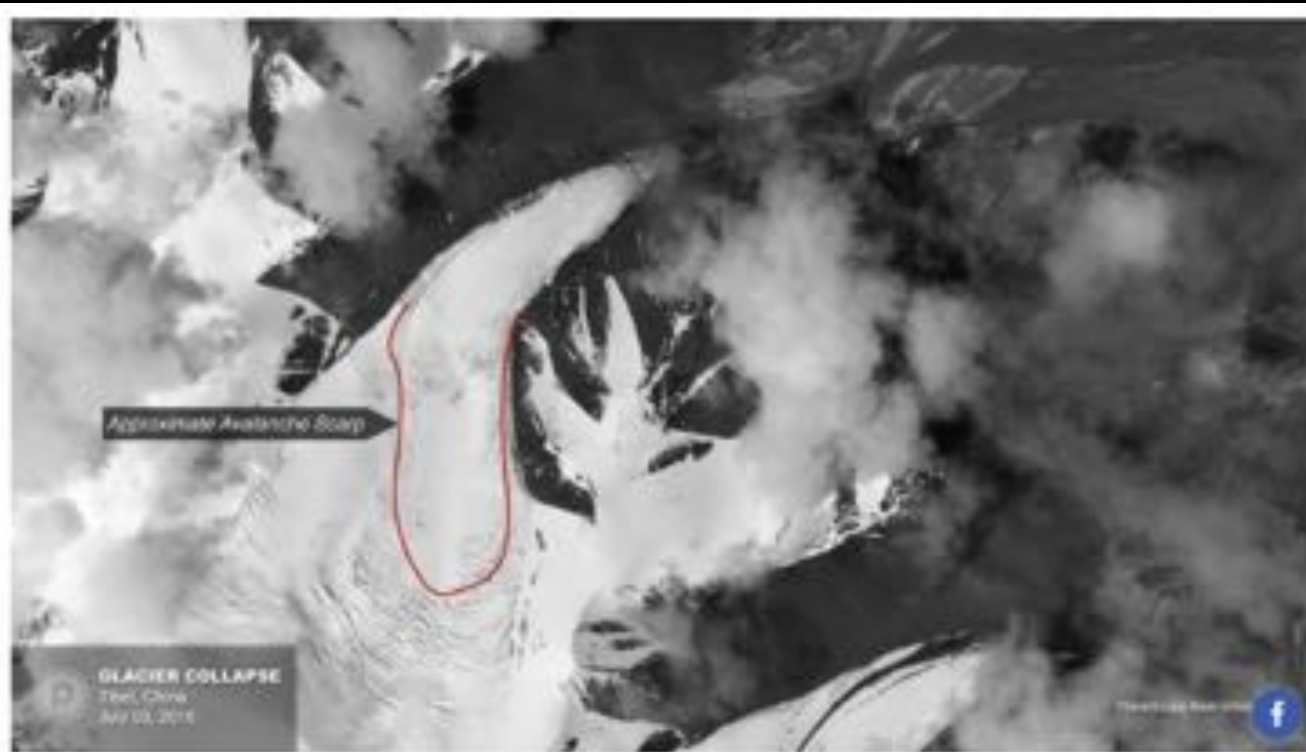


NASA Earth Observatory



September 20, 2002, North Ossetia, (Russian Caucasus)

- Part of Maili Glacier broke off and avalanched, ~100 km per hour
- 20×10^6 tonnes of ice, rock, mud swept ~16 km through Karmadon Gorge
- ~140 fatalities, village of Nizhny Karmadon destroyed



The glacier before its collapse in early July. Some crevasses, a sign of imminent surging, can be seen at its base. (Planet)

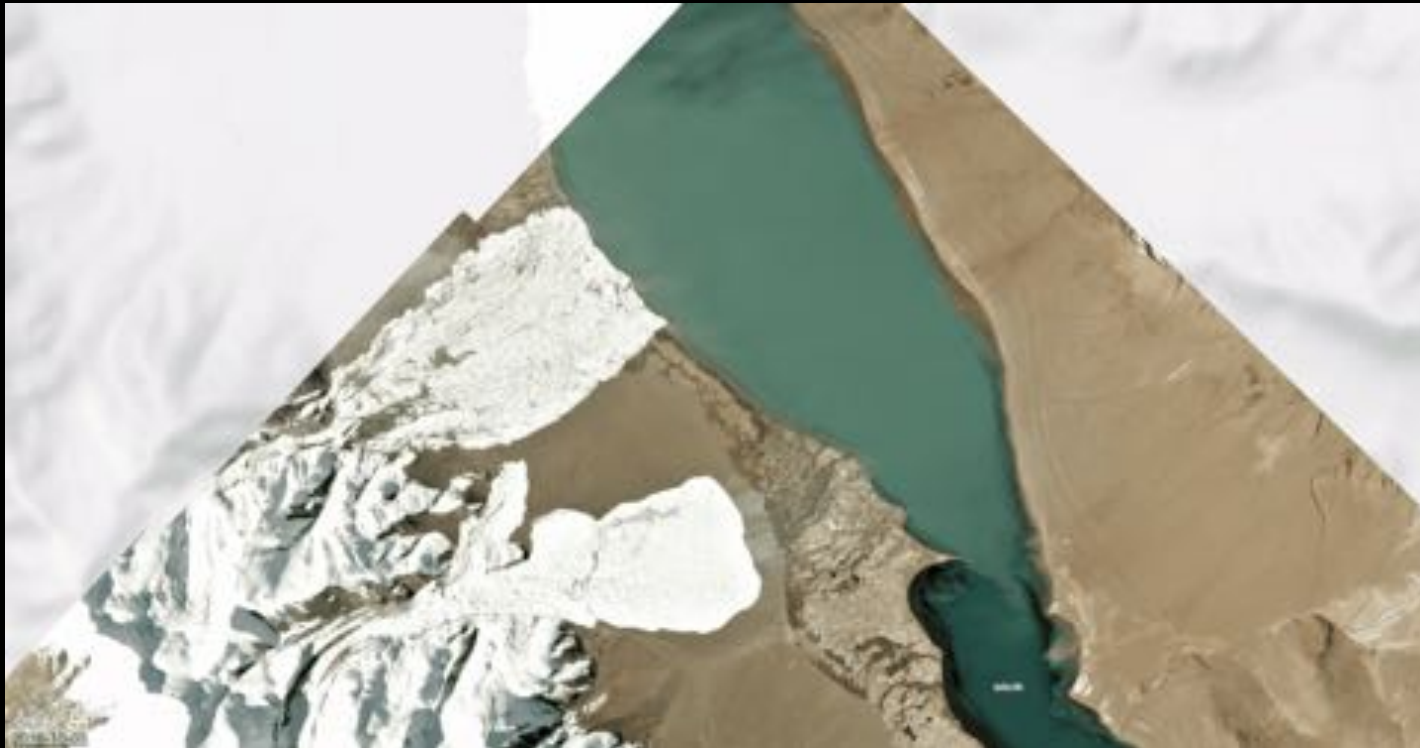
July 3rd, 2016



August 22nd, 2016







Today's Objectives:

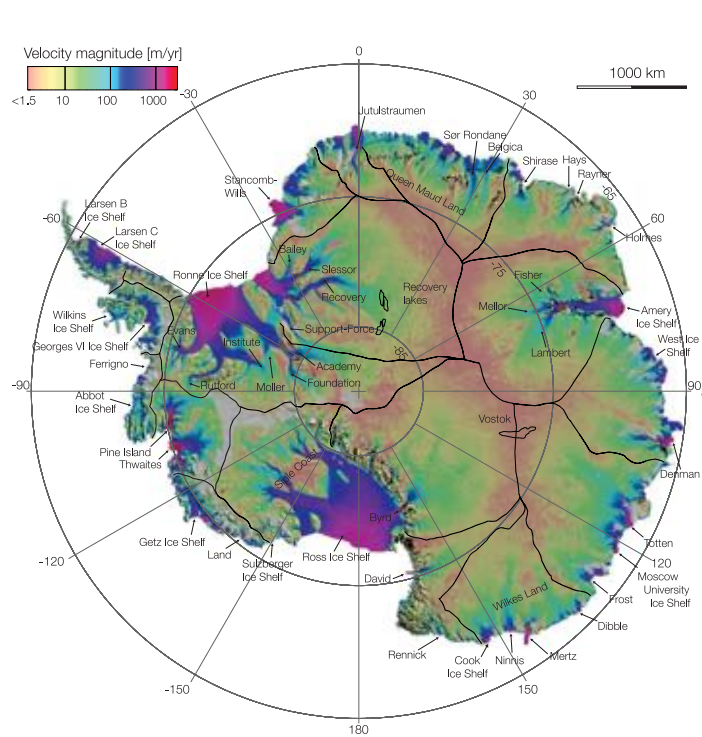
Basal Sliding:

- What are the controls on basal sliding? How do they compare with the physics of internal deformation?
- What are the two fundamental processes that allow sliding past bedrock obstacles? What is the role of water in each process?

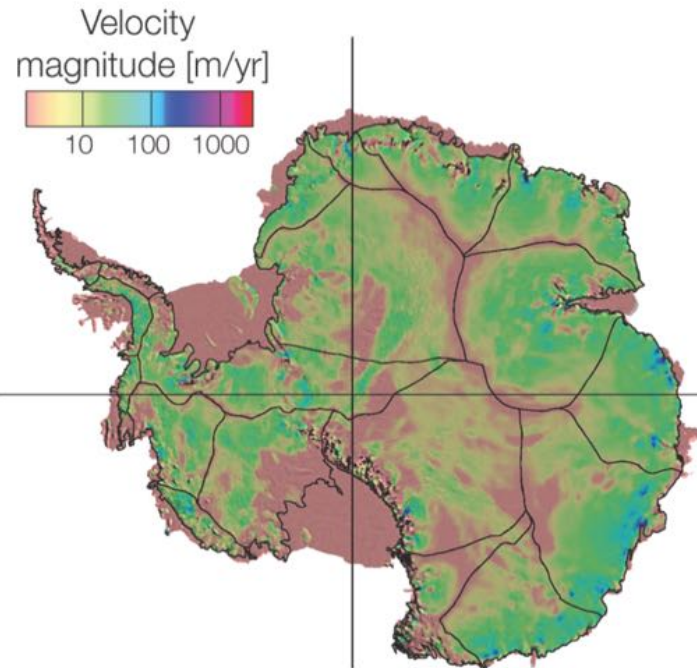
Hydrology:

- How is water transported in a glacial system?
- How does the amount of water in the system affect the water transport regime?

Importance of Sliding



Observed Surface Speed



Deformation Speed Only

Importance of Sliding

Internal deformation u_d is always present

Sliding contribution to ice transport:

$u_s = 0 \times u_d$ e.g. frozen bed

$u_s = 10^N \times u_d$ e.g. glacier surges and ice streams

N can be as high as ~ 3

In “typical” temperate mountain glaciers, it is commonly supposed that

$$\begin{array}{ccc} \text{Ice transport} & & \text{Ice transport due to} \\ \text{due to sliding} & \approx & \text{internal deformation} \end{array}$$

What's it like under a glacier?

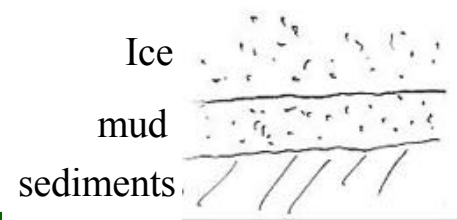
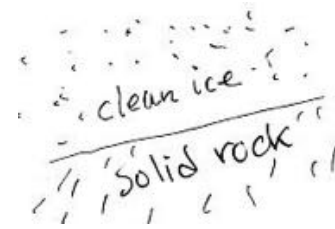
Smooth clean bedrock

Frozen ground (tundra, gravel, till)

Soft marine mud

Glacial till – unsorted gravel, mud

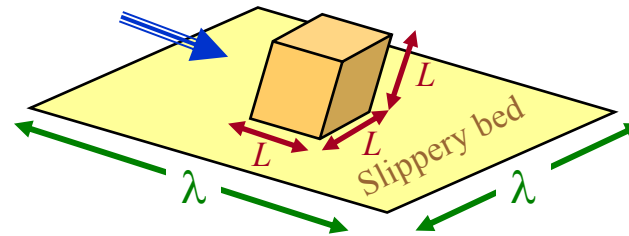
- Soft, wet deformable
- Hard, overconsolidated
- Wet, thawing (geothermal flux, frictional heat)
- Wet, freezing (ice fingers into pores)



Tombstone Model

(J. Weertman, 1957)

A simple starting model
for sliding



1) Regelation

2) Enhanced Deformation

Weertman, J. (1957), *J. Glac.* **3**, 33.

ON THE SLIDING OF GLACIERS

By J. WEERTMAN

(Naval Research Laboratory, Washington, D.C.)

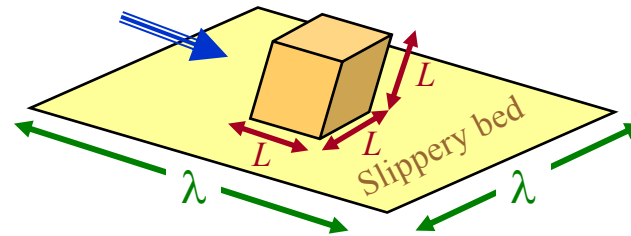
ABSTRACT. A model is proposed to explain the sliding of any glacier whose bottom surface is at the pressure melting point. Two mechanisms are considered. One is pressure melting and the other is creep rate enhancement through stress concentrations. Neither of the mechanisms operating alone is sufficient to explain sliding. If both mechanisms operate together appreciable sliding can occur.

Regelation

Tombstone Model

(J. Weertman, 1957)

A simple starting model
for sliding



If ice is not accelerating off the mountain (i.e. an ice avalanche), then there must be a restraining force to balance the down-slope driving shear stress

$\tau = \rho g h \sin(\theta)$ acting on area $\lambda \times \lambda$.

h = ice thickness

θ = surface slope

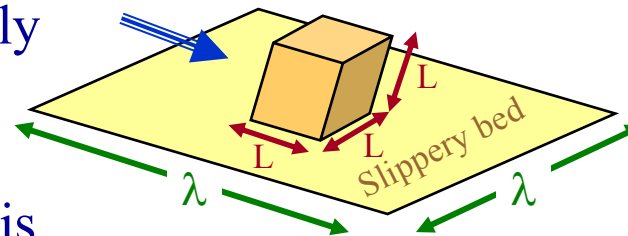
Force = stress \times Area on area $\lambda \times \lambda$:

$$F = \tau \lambda^2$$

- But there is no basal shear stress on slippery bed ...

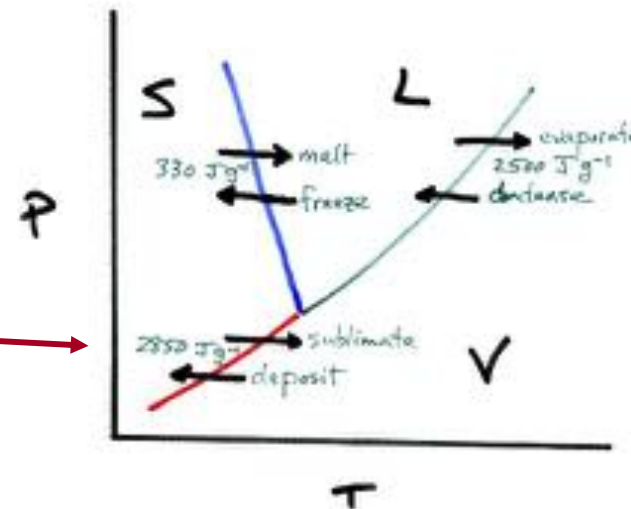
Tombstone face

- Force $\tau \lambda^2$ is supported entirely by uphill face of bump
- This face has area L^2
- Pressure (stress) on that face is $P = \tau \lambda^2 / L^2$ (force/Area)



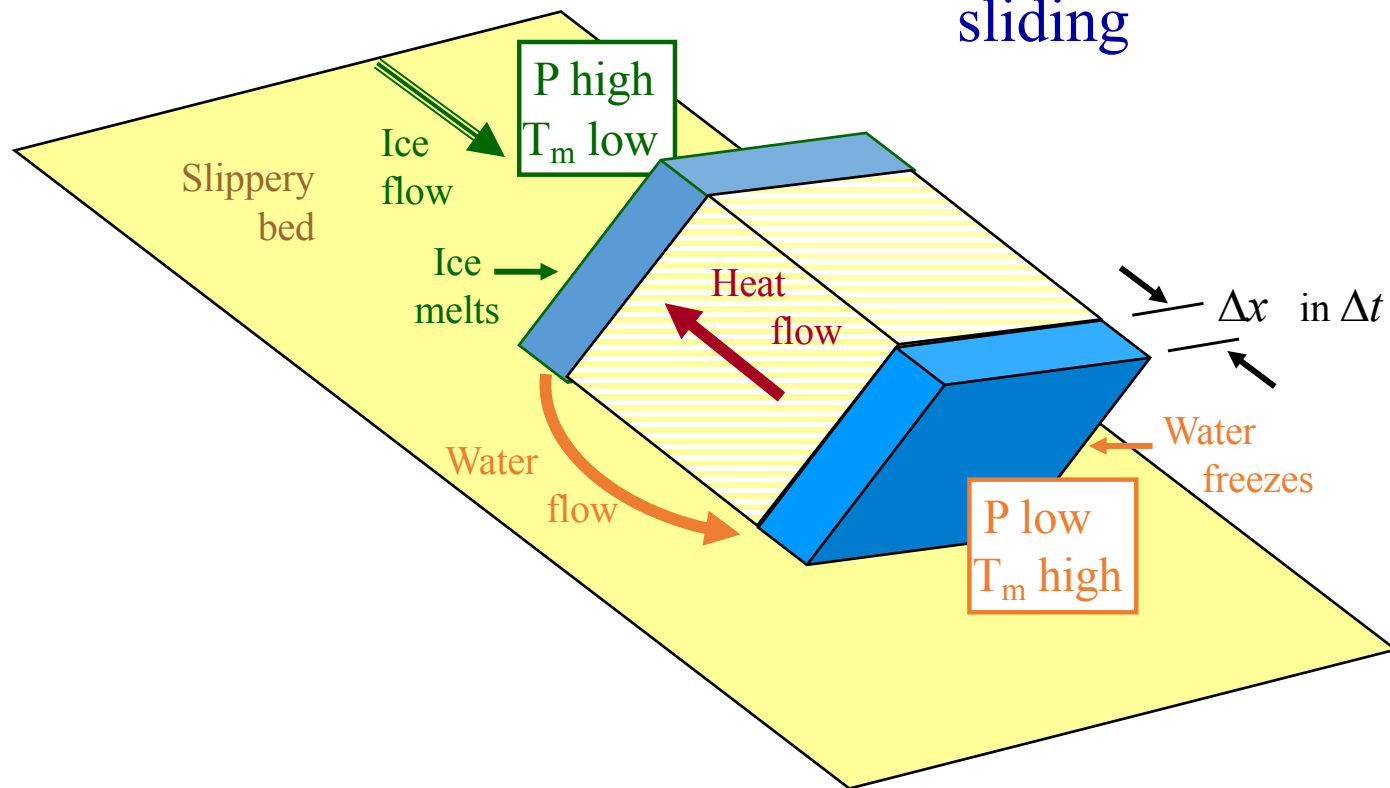
High pressure depresses freezing point

- $\Delta T = c P$
- $c = -7 \times 10^{-8} \text{ } ^\circ\text{C Pa}^{-1}$ (slope on phase boundary)

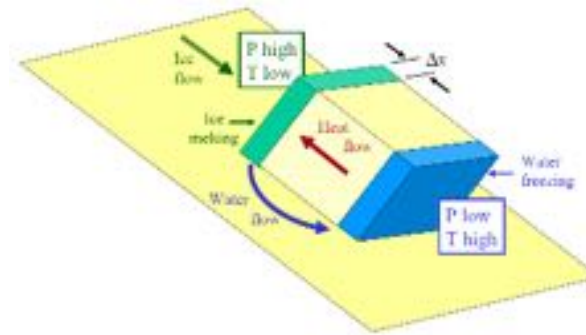


$$\Delta T = c \tau \lambda^2 / L^2$$

Regelation sliding



Can ice slide past a Bump?



- How fast ice can move past bump depends on how fast heat can get back through bump.
- Heat flux Q depends on temperature gradient $\Delta T/L$ (Fourier's Law).

$$Q = -K \Delta T / L$$

K = rock conductivity $\cong 2 \text{ W m}^{-1} \text{ deg}^{-1}$

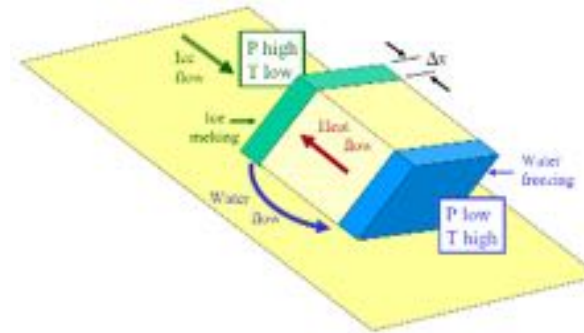
L = rock scale length (m)

$$\Delta T = c \tau \lambda^2 / L^2$$

$$Q = - \left(\frac{Kc\tau}{L} \right) \left(\frac{\lambda^2}{L^2} \right)$$

Sliding Speed by Regelation

In time Δt , heat flux Q (W m^{-2}) delivered to Area $= L^2$ of rock face can melt a volume V of ice given by: $V = L^2 \times \Delta x$ (1)



$$V = (\text{energy delivered}) / (\text{energy to melt } 1 \text{ m}^3)$$

$$V = (Q \times L^2 \times \Delta t) / (\rho H) \quad (2)$$

H = heat of fusion = 331 kJ/kg

ρ = ice density = 900 kg/m³

Equating (1) and (2) and using

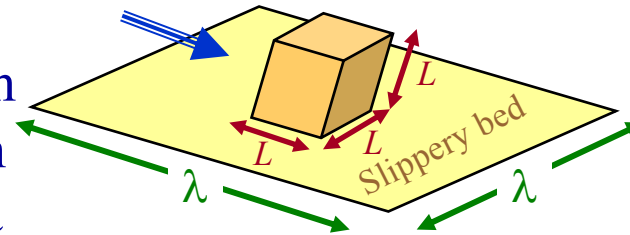
$$Q = - \left(\frac{Kc\tau}{L} \right) \left(\frac{\lambda^2}{L^2} \right)$$

$$U_{slide} = \frac{\Delta x}{\Delta t} = \frac{Kc\tau}{\rho HL} \frac{\lambda^2}{L^2}$$

Example of sliding speed

$$U_{slide} = \frac{Kc\tau}{\rho HL} \frac{\lambda^2}{L^2}$$

If $L = 0.02 \text{ m}$
 $\lambda = 0.2 \text{ m}$
 $\tau = 10^5 \text{ Pa}$



$$U_{slide} = \frac{2W \text{ m}^{-1} \text{ deg}^{-1} 7 \times 10^{-8} \text{ deg Pa}^{-1} 10^5 \text{ Pa}}{900 \text{ kg m}^{-3} 3.3 \times 10^5 \text{ J kg}^{-1} 0.02 \text{ m}} \frac{0.2^2 \text{ m}^2}{0.02^2 \text{ m}^2}$$

$$\approx 2 \times 10^{-7} \text{ m s}^{-1}$$

$$\approx 2 \times 10^{-7} \text{ m s}^{-1} \times 3 \times 10^7 \text{ s yr}^{-1} \approx 6 \text{ m yr}^{-1}$$

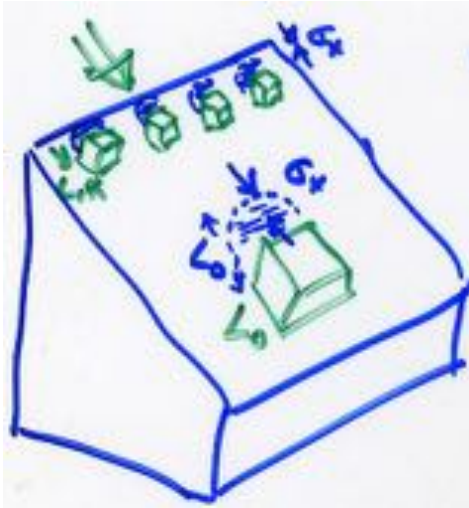
How will sliding speed change if bumps are bigger?

Regelation Demonstration – on Friday



Enhanced Creep

Can ice flow around bumps?



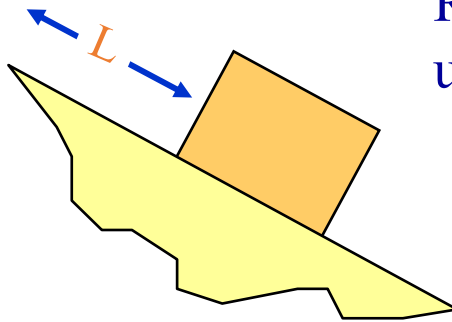
σ_x is compressive stress in ice upstream of bump

- Ice “knows” that bump is there for a distance $\sim L_0$ upstream
- one large bump stresses a bigger volume of ice compared to many smaller faces with the same total restraining face area (as required for force balance)

Ice deforms in response to stress
(Glen Flow Law)

$$\dot{\epsilon}_x = A \sigma_x^3$$

Strain near bumps



Rate of shortening of a line
upstream from bump

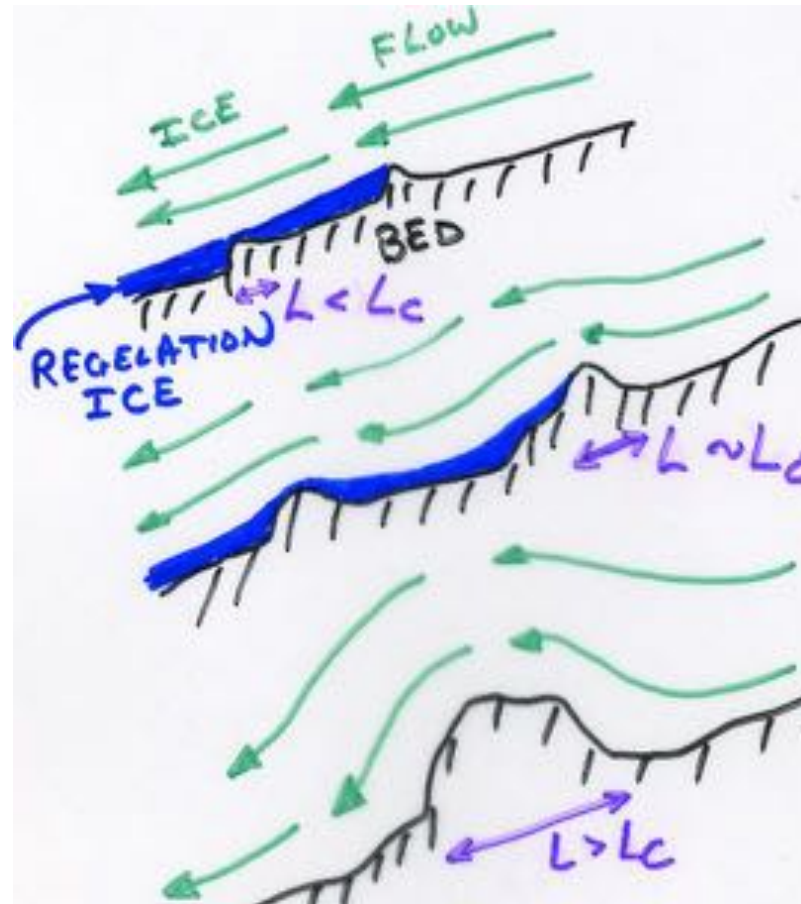
$$\dot{\epsilon}_x = \left(\frac{\Delta L}{L} \right) \frac{1}{\Delta t}$$

$$U_{slide} = \frac{\Delta L}{\Delta t} = L \dot{\epsilon}_x = LA \sigma_x^3 \quad \text{We used Glen flow law:}$$

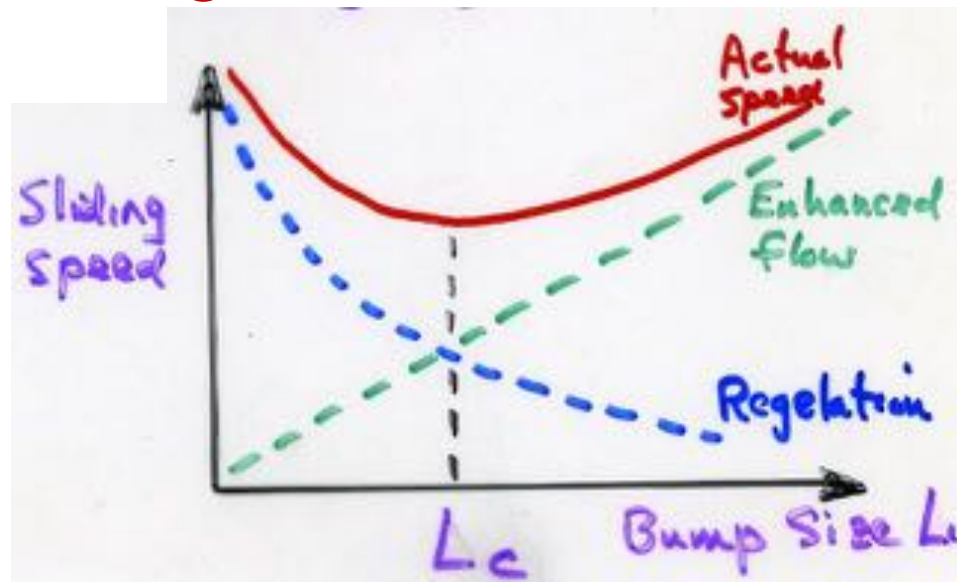
Ice can move faster around larger bumps

Regelation- Deformation Tradeoff

- Regelation allows ice to slide past small bumps easily.
- Enhanced strain gets ice past large bumps easily.
- At some intermediate scale $L=L_c$, both processes are equally effective (or ineffective).



Controlling-Obstacle Size



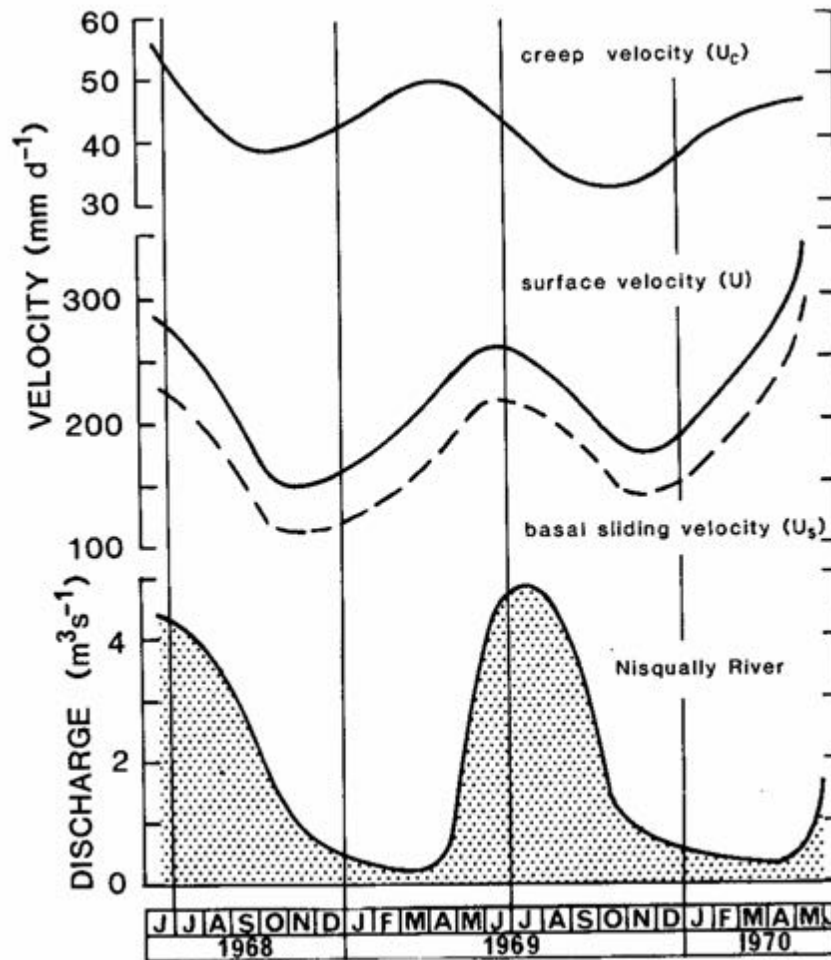
- Actual sliding speed is sum of 2 processes
- At $L=L_c$, U_{slide} is minimum
- Bedrock bumps with size L_c control sliding speed.

What assumptions are built into this concept?

Flow on Nisqually Glacier

Can Tombstone Model explain these data?

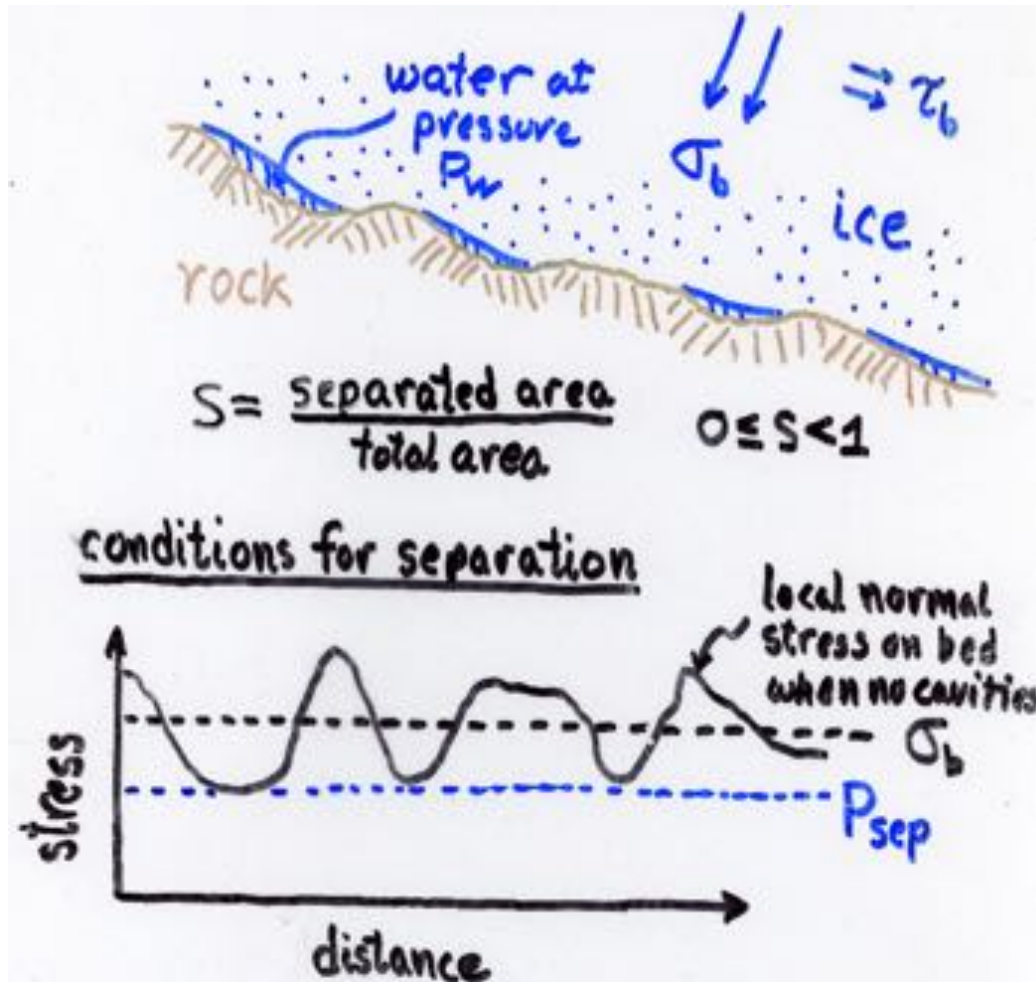
Based on Hodge, S.M. 1974
J. Glaciol. 13(69) 349-369.



Water is very important

- Meltwater from surface
- Meltwater from the bed
- Drainage through till?
- What does water do in a glacier?

Bed Separation and Sliding



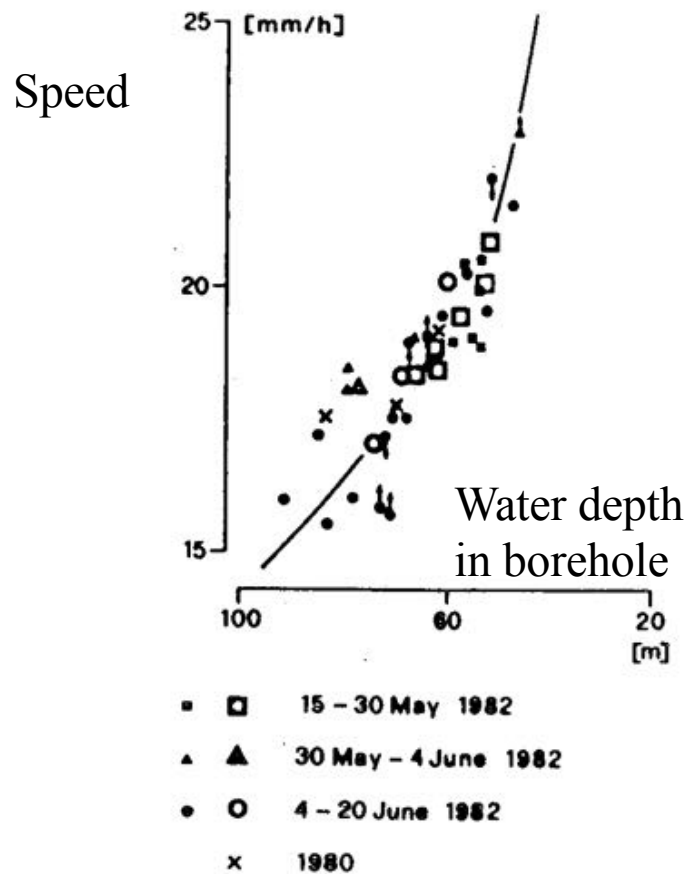
$$P_w < P_{sep}$$

- $S = 0$
- Cavities cannot form

$$P_w > P_{sep}$$

- $S > 0$
- Cavities can open

Sliding and Water Pressure

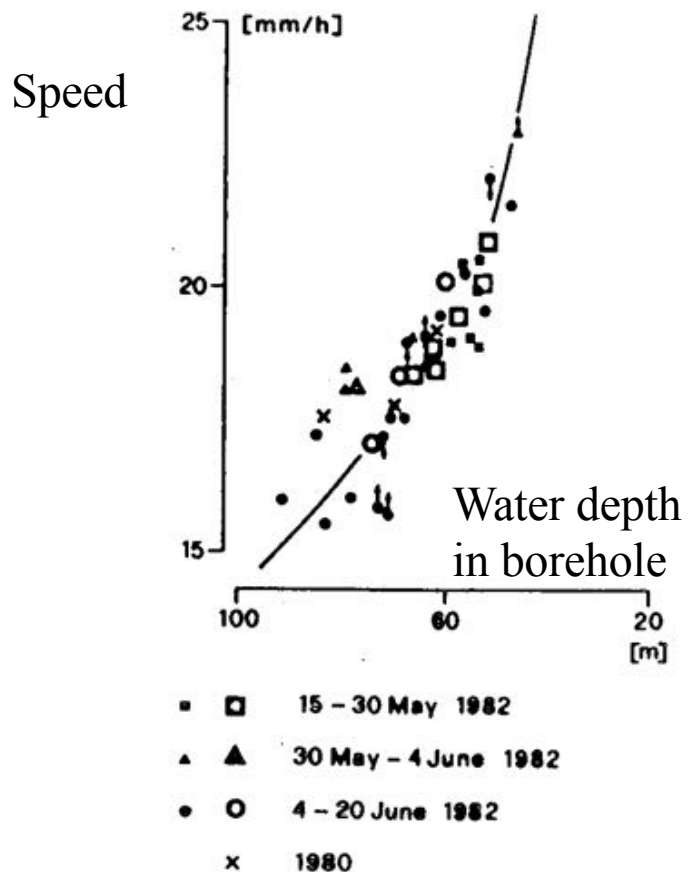


Glacier moves faster
when water level
rises in a hole to
bedrock

- Why?

(Almut Iken)

Sliding and Water Pressure

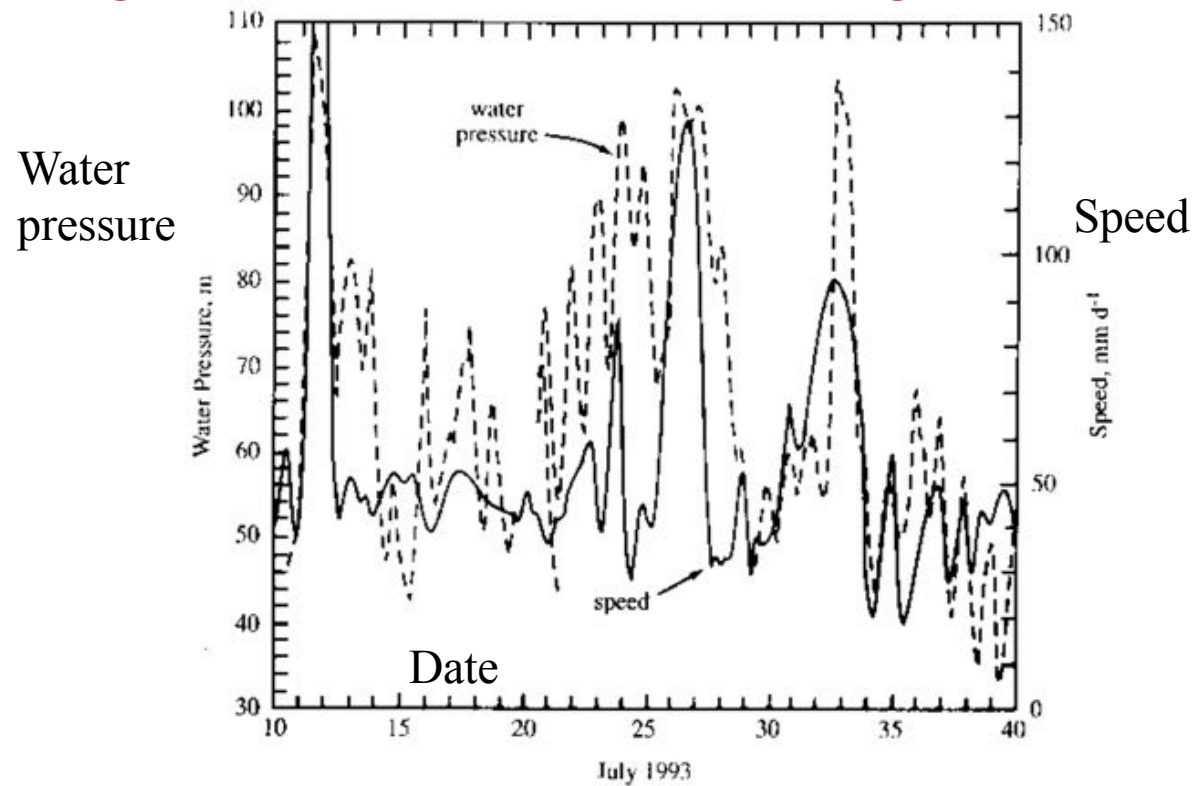


Glacier moves faster
when water level
rises in a hole to
bedrock

- Borehole is acting as a manometer; water level tells us about water pressure at the base of the glacier

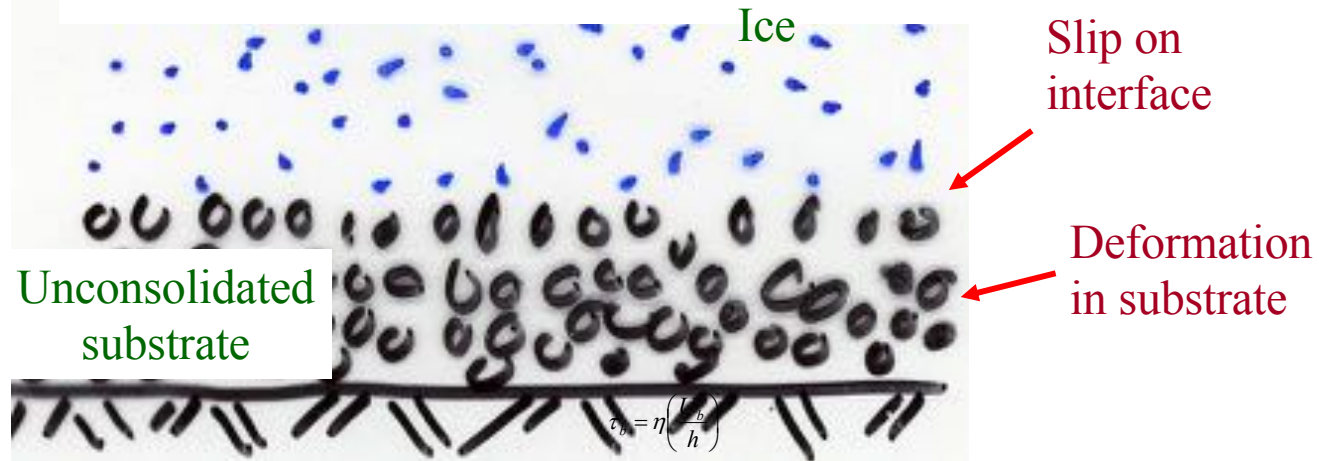
(Almut Iken)

Sliding and Water Pressure - Storglaciaren



(Hanson et al., 1998. *J. Glaciol.* 44(147) 359)

Sliding and Soft Beds



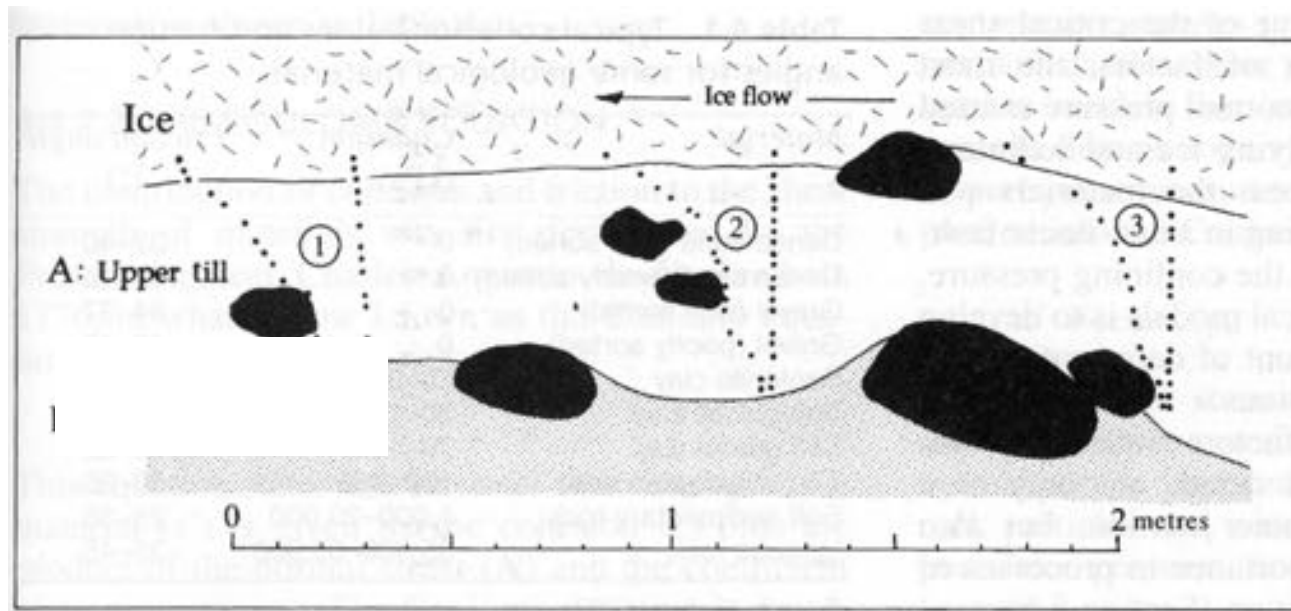
Factors:

- Thickness h and composition of material (till viscosity η)
- Pore-pressure distribution

$$U_b = \frac{h}{\eta} \tau_b$$

But ... what is viscosity η ???

Deformable Bed in Iceland

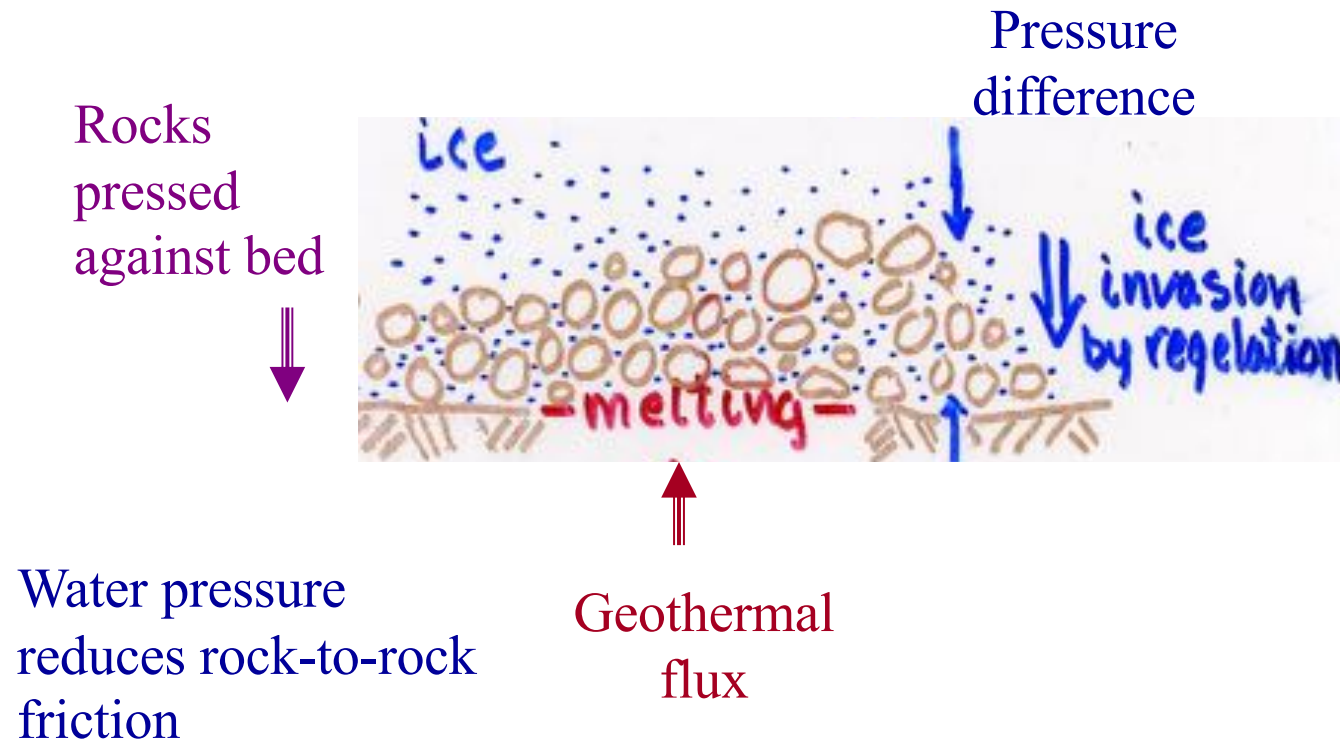


Breiðamerkerjökull, Iceland

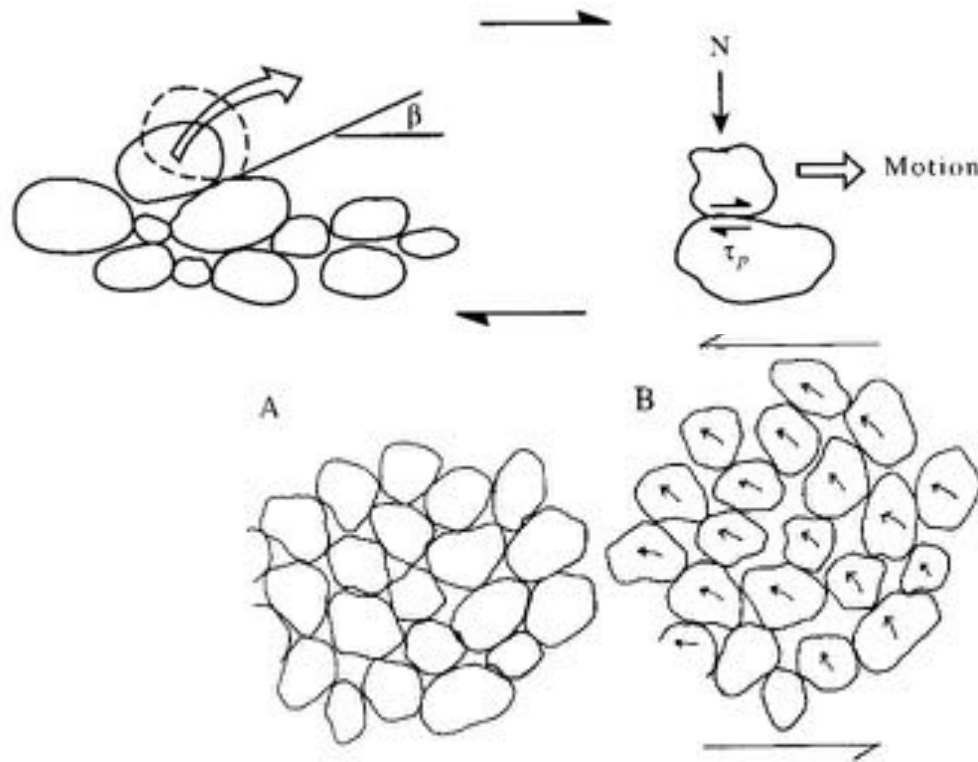
- Segmented rods left in subglacial till were moved forward by glacier over 10 day interval.

(Benn and Evans, *Glaciers and Glaciation*,
adapted from Boulton and Hindmarsh)

Rock Friction



Rock Friction – Till Dilation



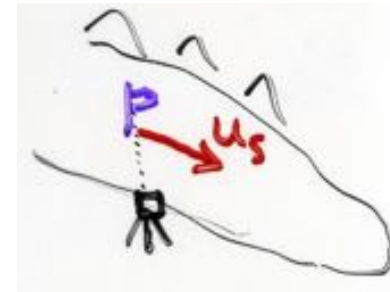
- Till must swell so that clasts can move past one another

- Water at high pressure helps to dilate till

(Hooke, *Fundamentals of Glacier Mechanics*;
Benn and Evans, *Glaciers and Glaciation*)

Questions, Questions, Questions ...

1. Can speed U_d due to internal deformation change rapidly?
 - Consider hours, days, seasons.
2. Can sliding speed U_b change rapidly, e.g. in a few hours?
 - Consider Tombstone model, Deforming-till model, (others?)
3. You are measuring the surface speed U_s of a pole in the center of a glacier in the Cascades. You just had the hottest 3 days of the summer. What might happen to U_s ?



Today's Objectives:

Basal Sliding:

- What are the controls on basal sliding? How do they compare with the physics of internal deformation?
- What are the two dominant processes that allow sliding past bed features? What is the role of water in each process?

Hydrology:

- How is water transported in a glacial system?
- How does the amount of water in the system affect the water transport regime?

Glacial Outburst Flooding

- South Tahoma Glacier, Mount Rainier, WA, USA
- Since 1985, over 30 have occurred





Streams on Glaciers

Water can melt channels
into glacier ice

- Lower albedo than ice
- Dissipating potential energy as it loses elevation

Austre Lovenbreen, Spitsbergen
Hambrey and Alean. *Glaciers*.

Rivers on the Greenland Ice Sheet

Vibeke Gletscher,
East Greenland



← ~300 m →

Hambrey and Alean, *Glaciers*.

Moulins

Water will find a way to
move down into a
glacier

- a supraglacial stream
will typically flow into a
crevasse









Tunnels

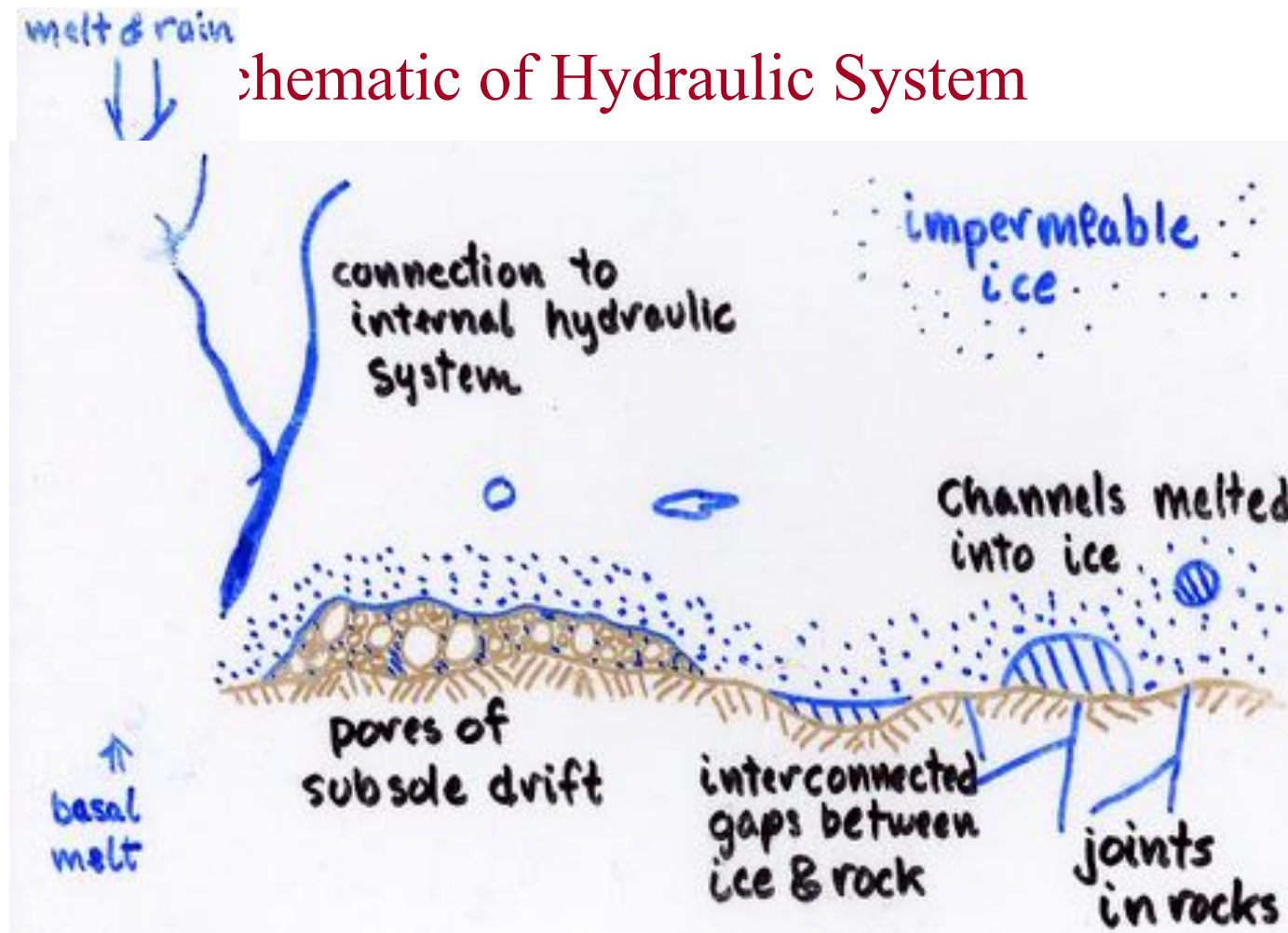


We can see the water coming out at a glacier terminus

- But where has it been?

Fox Glacier, NZ.
Hambrey and Alean. *Glaciers*.

Schematic of Hydraulic System



Tunnels in Winter

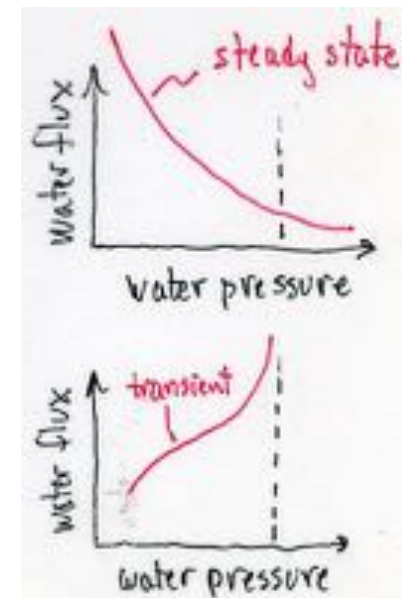
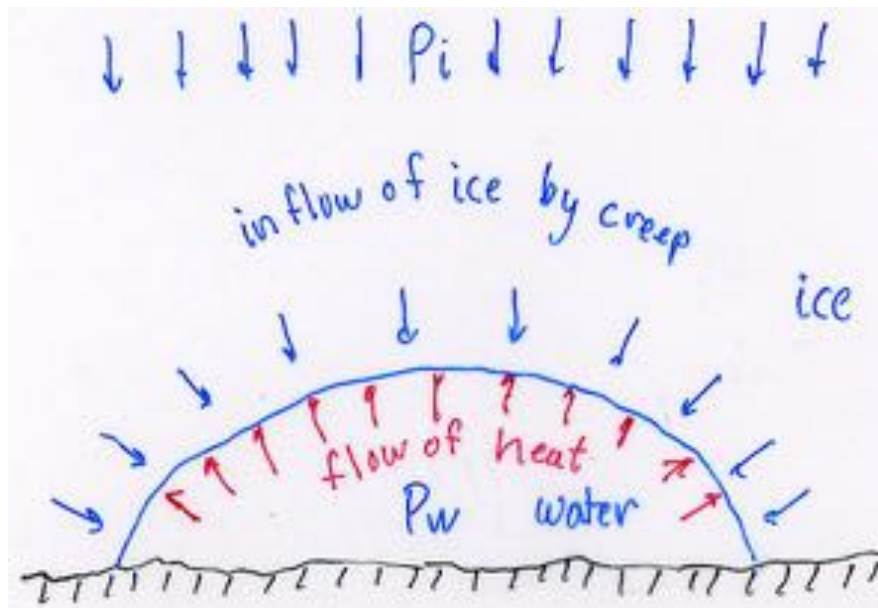


Water can stop flowing in winter

- where does a tunnel lead?
- What happens over the winter?

Matanuska Glacier.
Andersen and Borns.
Ice Age World.

Tunnels Transporting Water



Rothlisberger (1972)
Nye (1976)

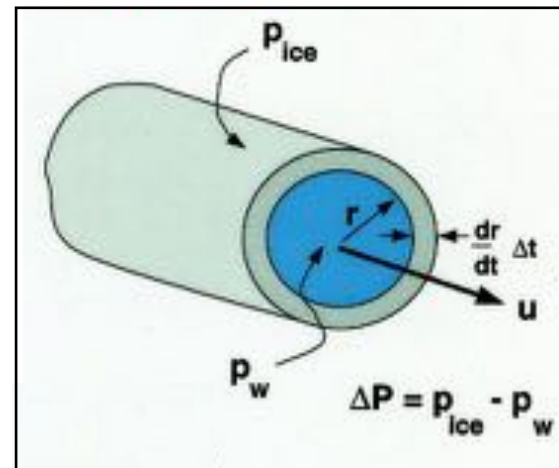
In steady state, higher water pressure \leftrightarrow lower water flux (in smaller tunnel)

Pressure in Steady Tunnels

Two competing influences:

- Creep closure of the tunnel, through ice deformation
- Tunnel growth, through melting from turbulent heat transfer

Creep Closure:



Pressure in Steady Tunnels

Two competing influences:

- Creep closure of the tunnel, through ice deformation
- Tunnel growth, through melting from turbulent heat transfer

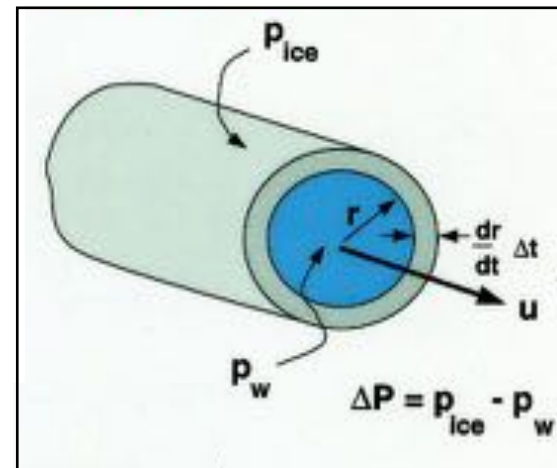
Creep Closure:

$$\dot{\epsilon} = A\sigma^3$$

$$\hookrightarrow \frac{1}{r} \frac{\Delta r}{\Delta t} \approx A[p_i - p_w]^3$$

$$\hookrightarrow \frac{\Delta r}{\Delta t} \propto \Delta p^3$$

$$\frac{\Delta V}{\Delta t} \propto 2\pi r * r \Delta p^3$$



Pressure in Steady Tunnels

Two competing influences:

- Creep closure of the tunnel, through ice deformation
- Tunnel growth, through melting from turbulent heat transfer

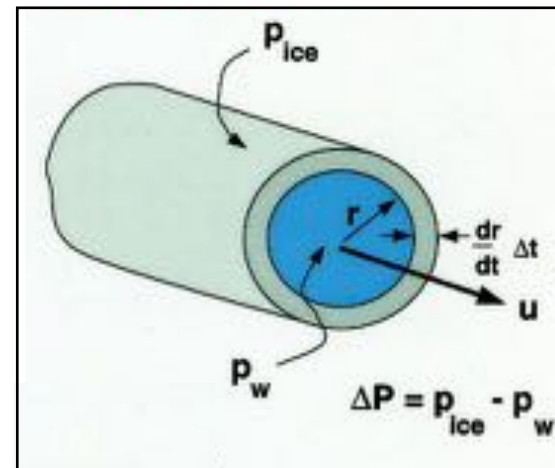
Turbulent Melting:

$$\frac{\Delta V}{\Delta t} \propto \frac{\Delta E}{\Delta t} \propto Q_w$$

$$Q_w = \pi r^2 u$$

$$u \propto r^{2/3} \text{ - (pipe flow theory)}$$

$$\frac{\Delta V}{\Delta t} \propto r^{8/3}$$



Pressure in Steady Tunnels

Two competing influences:

- Creep closure of the tunnel, through ice deformation
- Tunnel growth, through melting from turbulent heat transfer

Creep

$$\frac{\Delta V}{\Delta t} \propto r^2 \Delta p^3$$

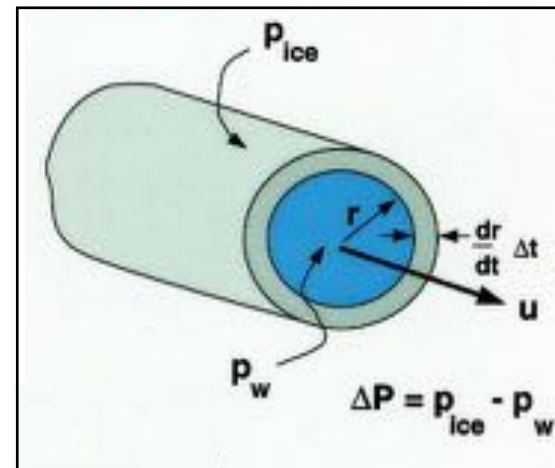
$$\Delta p \propto r^{2/9}$$

Melt

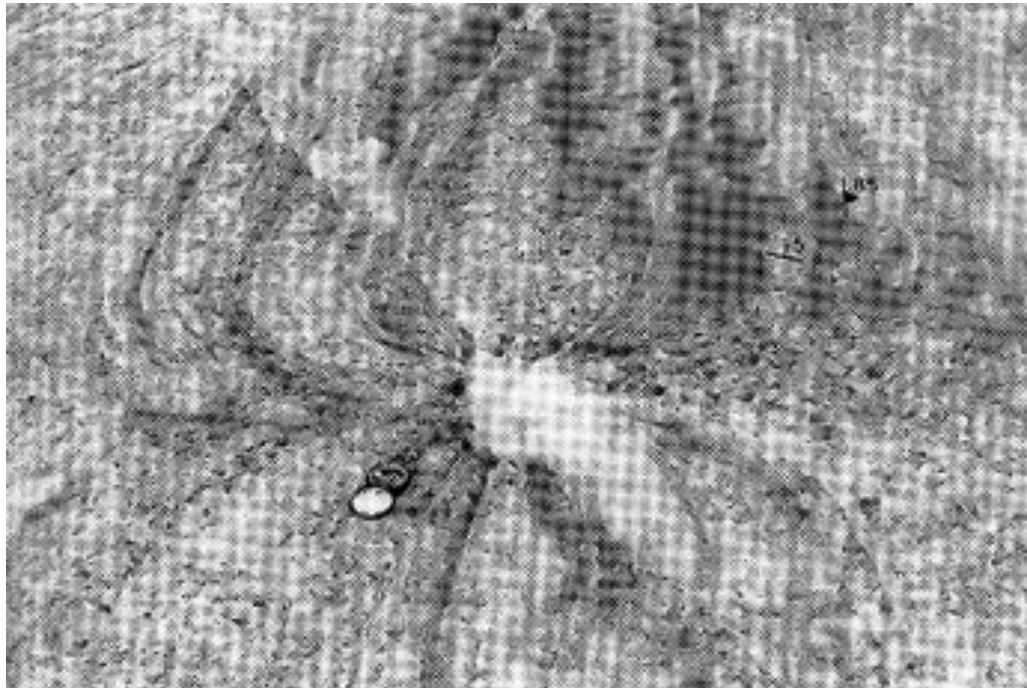
$$\frac{\Delta V}{\Delta t} \propto r^{8/3}$$

$$\Delta p \propto Q^{1/12}$$

As radius grows, Δp grows, p_w falls



Under-pressurized conduit

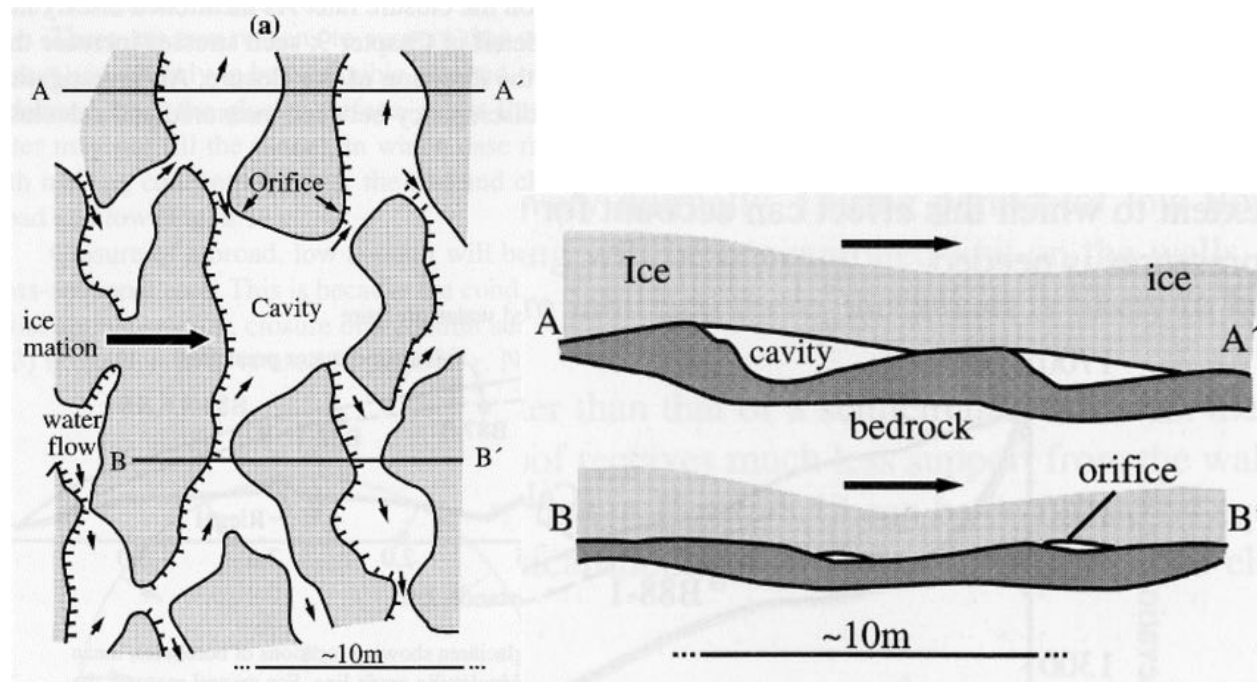


Brunton
compass
for scale

It did not survive when water flow stopped ...

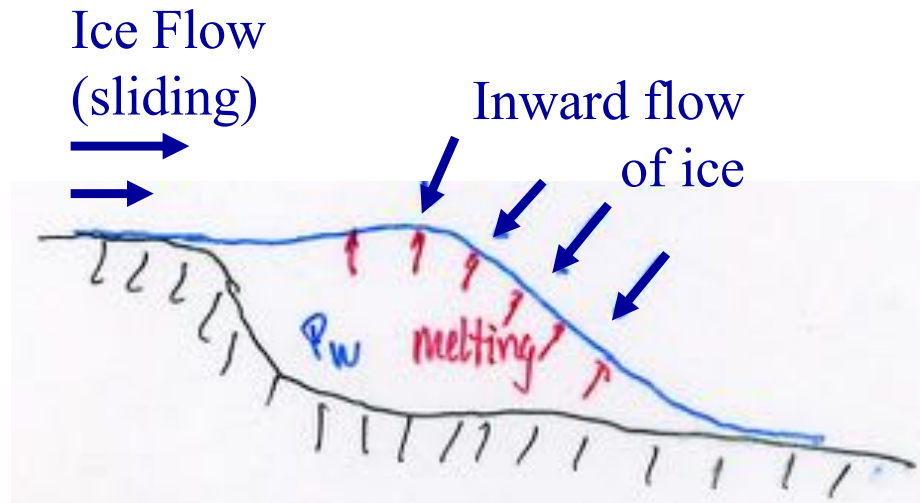
(Hooke, *Fundamentals of Glacier Mechanics*)

Linked Cavities

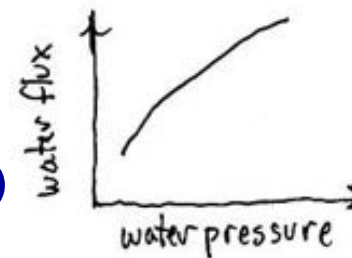


(Hooke, *Fundamentals of Glacier Mechanics*)

Water in Linked Cavities



Higher water pressure
 \leftrightarrow higher water flux (transport)



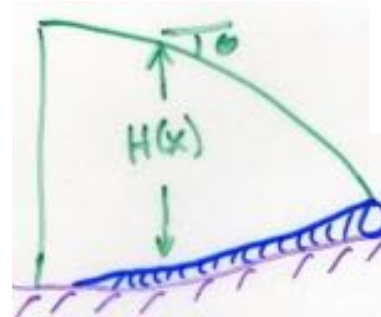
Questions, Questions, Questions ...

1. Why do some glaciers speed up in late winter or early spring before there has been much melting?

- Why do they slow down in mid-summer when melting is at its peak?

2. Describe the pressure gradient in the conduit.

- Which way does the water flow?

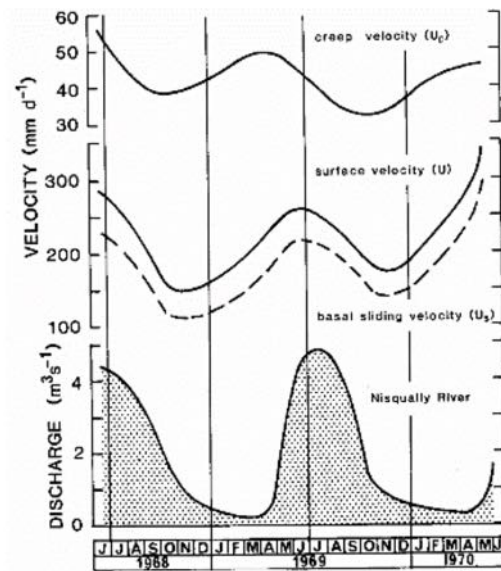


3. Water is bubbling out of a crack in a glacier. The water is at the melting temperature.

- Some ice crystals are swept upwards by the flow. What has been happening to them on the way up?



Seasonal Water Cycle



Early winter: little meltwater, low water pressure

- Tunnels close, linked cavities survive

Late winter: seepage, basal melt

- water pressure rises slowly
- Sliding increases slowly

Spring: high meltwater flux enters cavities

- Water pressure rises
- Sliding increases slowly

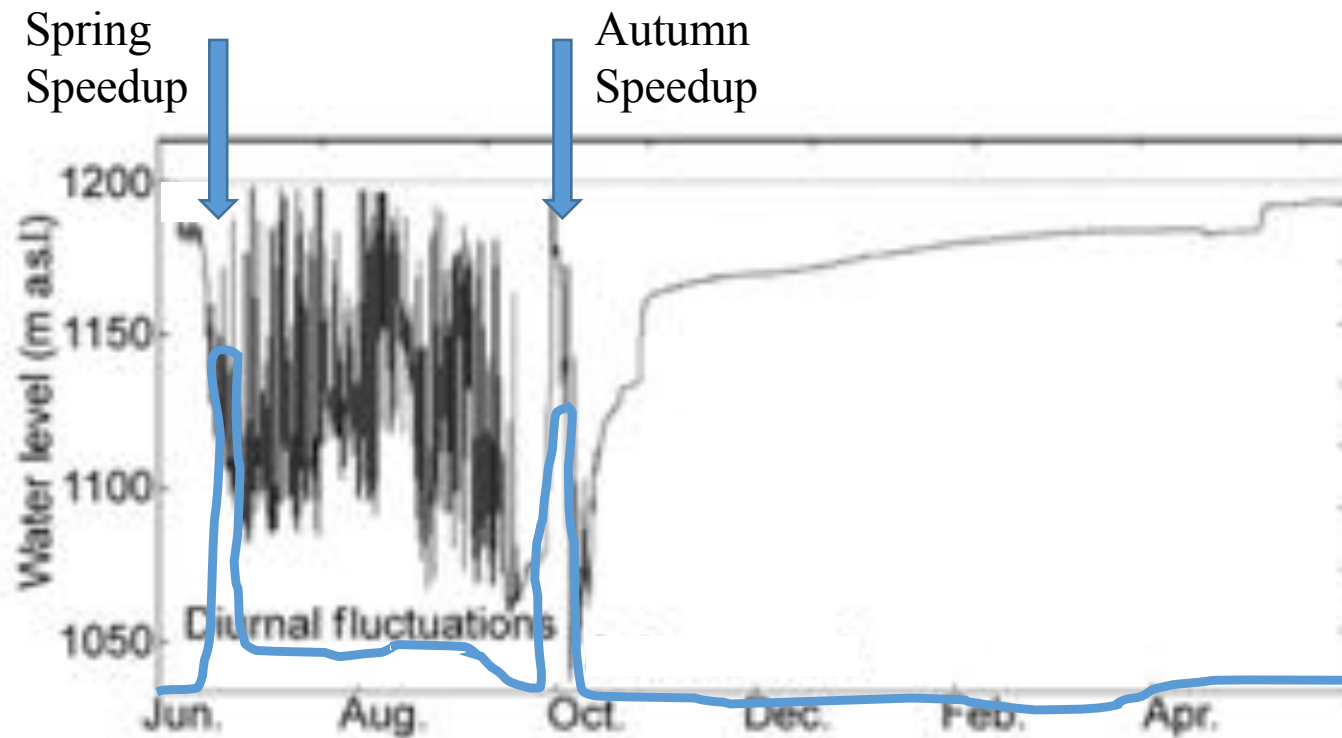
Early summer: too much water overloads cavities

- Surface rises
- Cavities join, tunnels start to form
- Sliding hits its peak

Mid-summer: water flows in low-pressure tunnels

- Basal water drains
- Sliding slows down

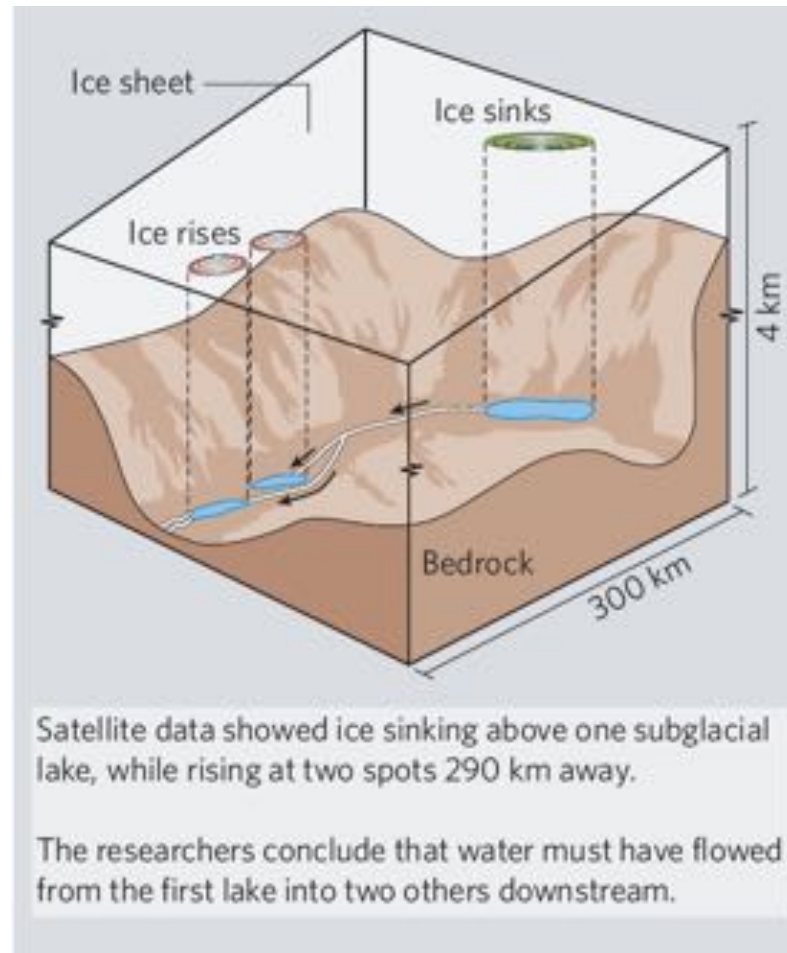
Seasonal Water Cycle



Water Pressure Variations on Bench Glacier, Alaska, 2002-2003 (Fudge et al, 2008)

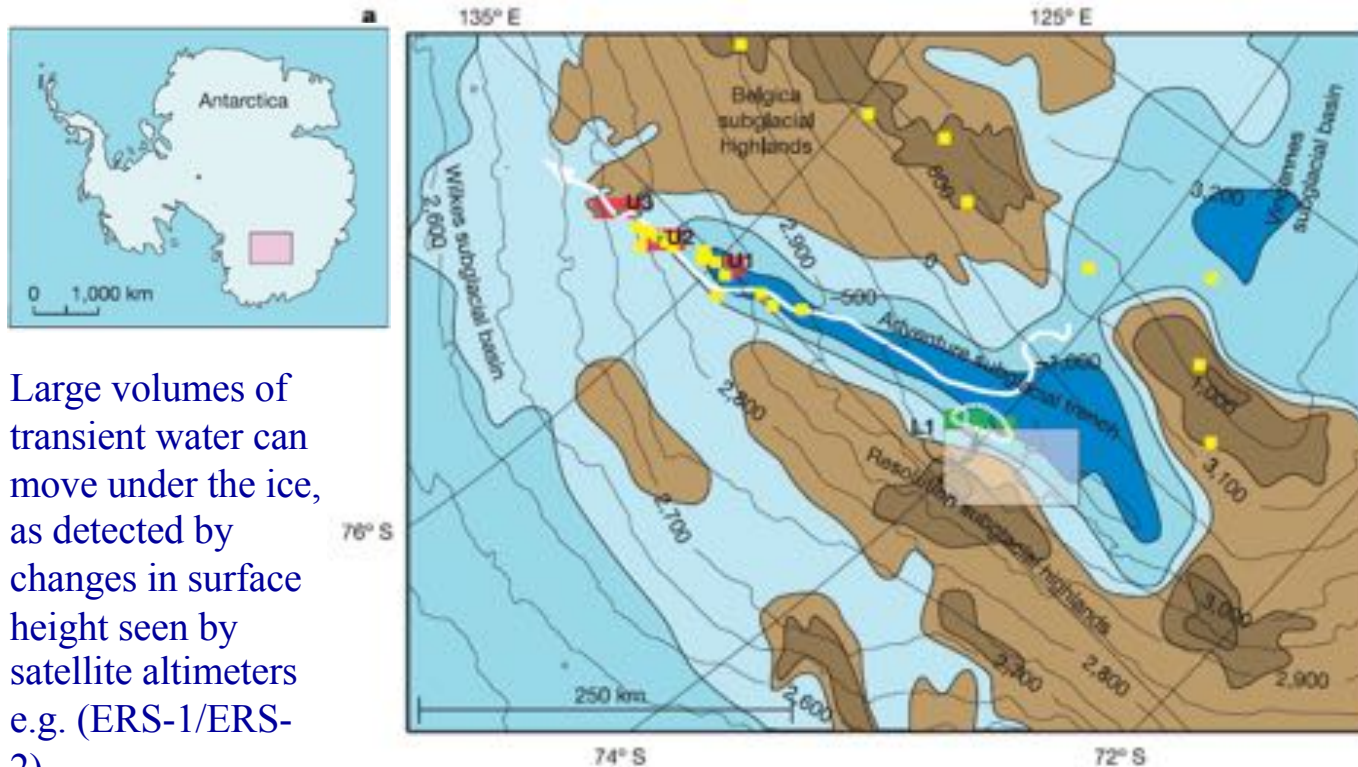
Water moving in Antarctica

- Recent work suggests large volumes of transient water can move under the ice.
- $\sim 2 \text{ km}^3$ moved $\sim 300 \text{ km}$ beneath the ice sheet between 1996 and 1999.



J. Giles 2006 *Nature* **440**, 977

Water moving in Antarctica



Large volumes of transient water can move under the ice, as detected by changes in surface height seen by satellite altimeters e.g. (ERS-1/ERS-2).

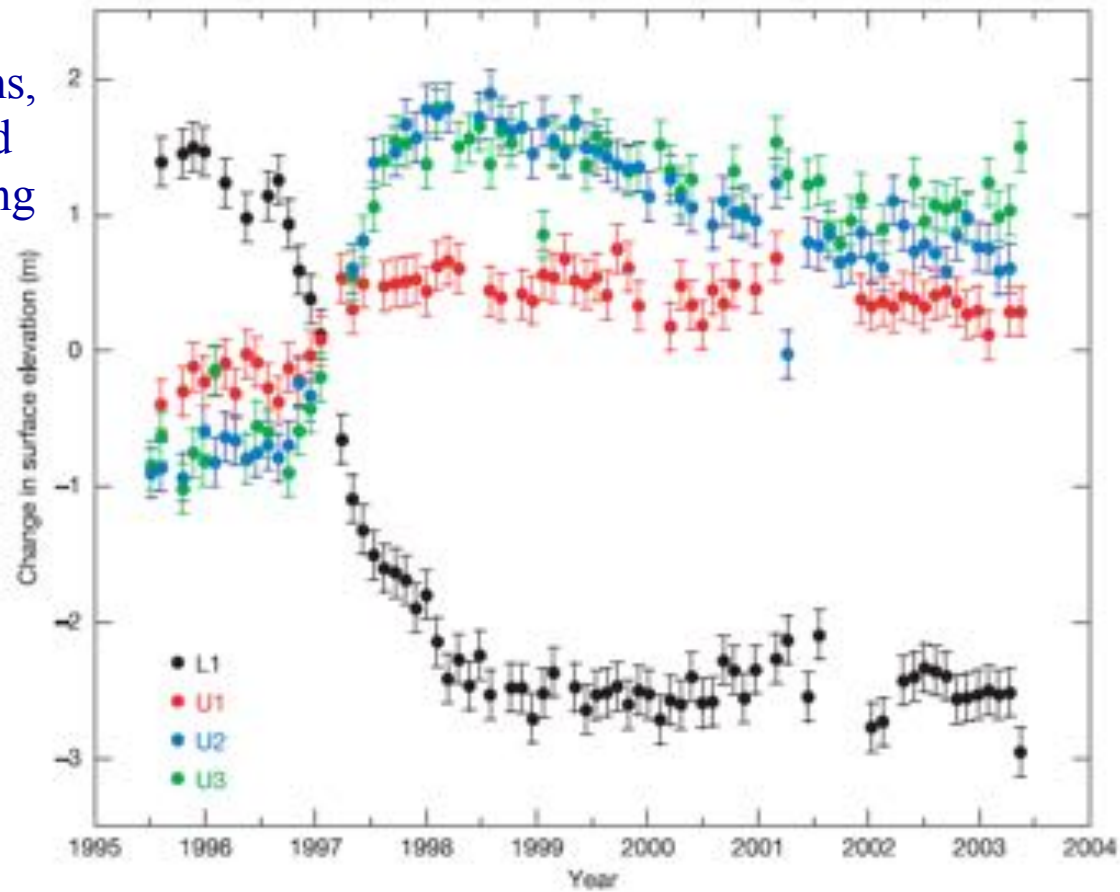
Wingham et al. (2006)
Nature **440**, 1033.

subglacial lakes - Yellow dots
- white dashes

L sites –lowering
U sites - rising

Surface Height Changes over Subglacial Lakes

As L1 drains,
U1, U2, and
U3 are filling
up.

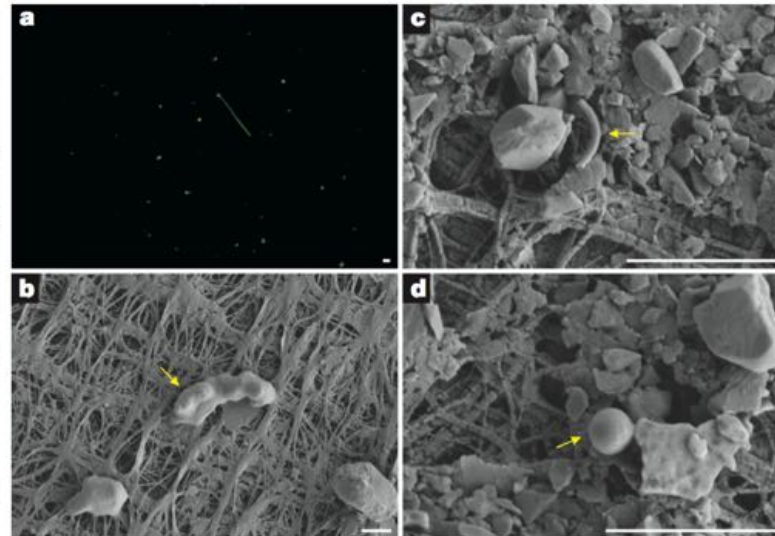
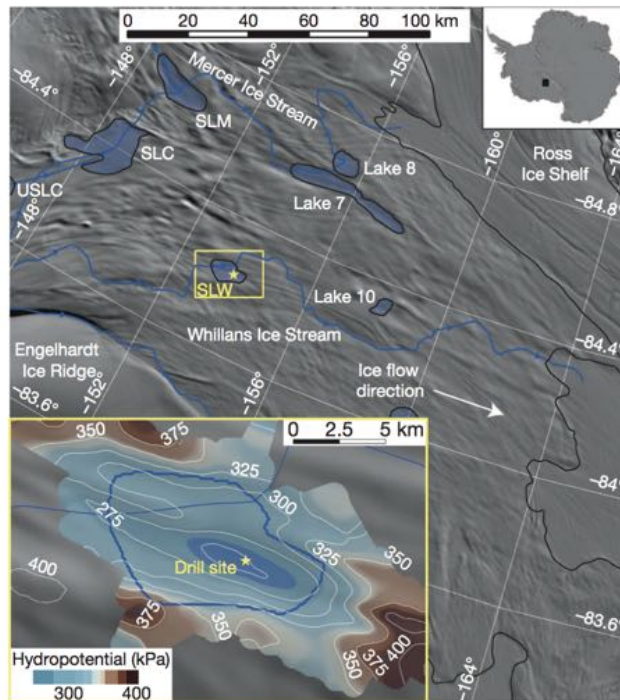


Wingham et al.
(2006) *Nature*
440, 1033.

Subglacial Lakes: Like Beneath the Ice

A microbial ecosystem beneath the West Antarctic ice sheet

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Sliding Summary

- Negligible sliding if base is cold
- Sliding is typically comparable to internal deformation in temperate valley glaciers
but
- Sliding can be up to 500-1000 m a⁻¹ over slippery beds of large glaciers (e.g. West Antarctic Ice Streams)

Sliding depends on water

- Lubrication
- Regelation
- Bed separation (high water pressure)

Water can flow

- Through distributed linked cavities (high-pressure system)
- Through tunnels (low-pressure system)
- Through subglacial sediments

Sliding can change rapidly with changing bed conditions