# **Topics**

- Homework
- A bit more about phylogenies
- Coalescent theory
  - What is it good for?
  - How does it work?

#### A homework comment

- The Inland birds differ from all others by genome rearrangements
- How could that happen?
  - Genome rearrangements usually underdominant
  - Natural selection tends to weed them out
- Could be strong selection for the inversions?

#### A homework comment

- Easist explanation is tiny population size:
  - Genetic drift is strong
  - Mating among close relatives could produce homozygotes quickly
- Thus, speciation was probably peripatric (though could have been allopatric with a later bottleneck)

#### **Student question**

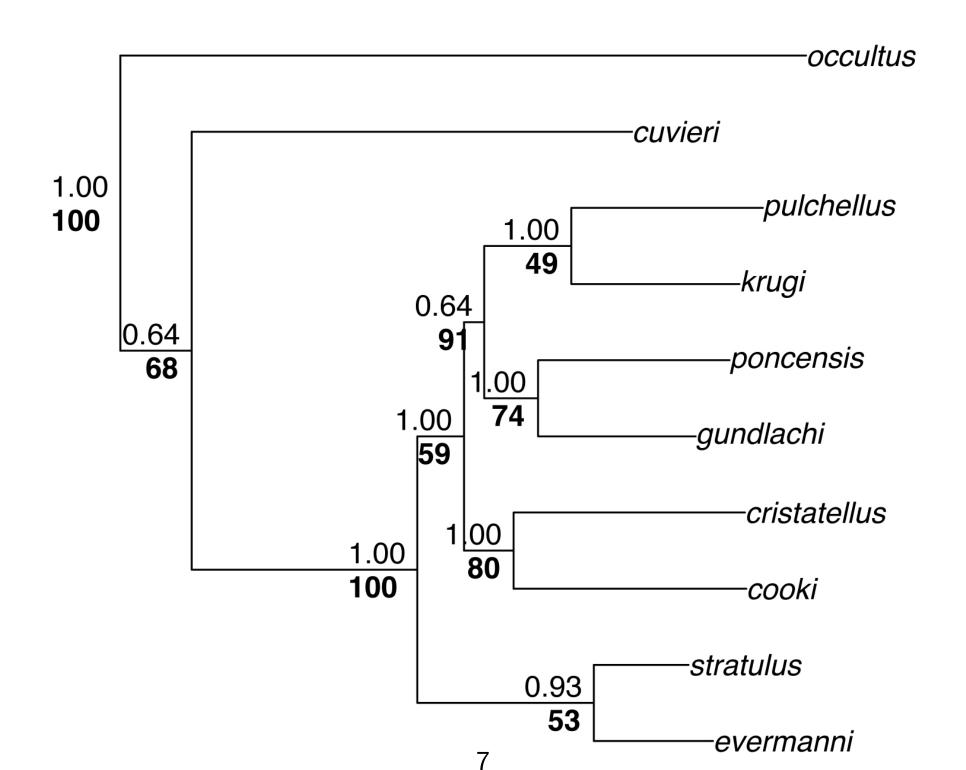
- Q: Which phylogeny methods should we be able to do by hand?
- A: Parsimony and UPGMA
  - Exam problems would be similar to HW9 problems
  - Impossible to do likelihood or Bayesian computations by hand....
  - Questions about these methods would be general/conceptual only

#### Phylogeny validation: likelihood

- Maximum likelihood algorithms come with built-in estimates of confidence
- Unfortunately these are only approximate for finite sized data sets
- Many researchers present bootstraps instead because they are more generally understood

#### Phylogeny validation: Bayesian methods

- Bayesian "cloud of trees" can be treated like a bootstrap sample
- They answer different questions:
  - Bootstrap: would a slightly different data set prefer a different tree?
  - Bayesian support: would a slightly different tree fit this data set almost as well?
- It is easier to see that these are different than to understand how to use each one appropriately!
- If "cloud" is too small, results will be overly certain



#### Garbage in, garbage out

- No sensible tree exists when:
  - A species arose by hybridization of two other species
  - Genes have been exchanged between distantly related species
  - Different genes in the genome have different histories due to recombination and reassortment
- The programs will still run and a tree will be produced!
- Hybrids often move toward the bottom of the tree, or may cluster with one or the other parent
- Ideally we'd infer a tangled graph, but this problem is HARD

#### Coalescence

- Definition
- Gray whale example
- Within-population trees
- Coalescence time depends on population size
- Coalescent-based algorithms:
  - Summary statistic approaches
  - Many-tree approaches

### **Coalescent Theory**

- Timing and pattern of common ancestry within a population reflects past population size
- It can also be perturbed by:
  - Population growth/shrinkage
  - Gene flow (migration)
  - Recombination
  - Natural selection
- If we can detect these patterns we can infer past population history



Alter et al. (2007) DNA evidence for historic population size and past ecosystem impacts of gray whales. PNAS 104: 15162-15167.

- How many gray whales pre-whaling?
- Whaling ship records not conclusive
- Recent slowing of the observed growth rate may suggest recovery
- Molecular data an alternative source of information

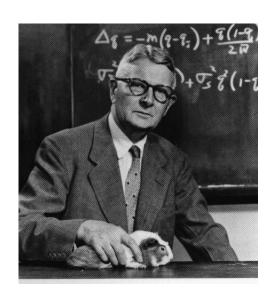


- 10 loci:
  - 7 autosomal
  - 2 X-linked
  - 1 mtDNA
- Complex mutational model with rate variation among loci
- Complex population model with subdivision and copy number
- ullet Complex demographic model relating  $N_{census}$  to  $N_e$

	Locus	n	Estimated N
Aut	ACTA	72	162,625
	BTN	72	76,369
	CP	76	77,319
	ESO	72	272,320
	FGG	72	180,730
	LACTAL	72	44,410
	WT1	80	51,972
X	G6PD	30	2,769
	PLP	52	92,655
mtDNA	Cytb	42	107,778
	All data		96,400 (78,500-117,700)
	Current census		18,000-29,000
	Previous models		19,480-35,430

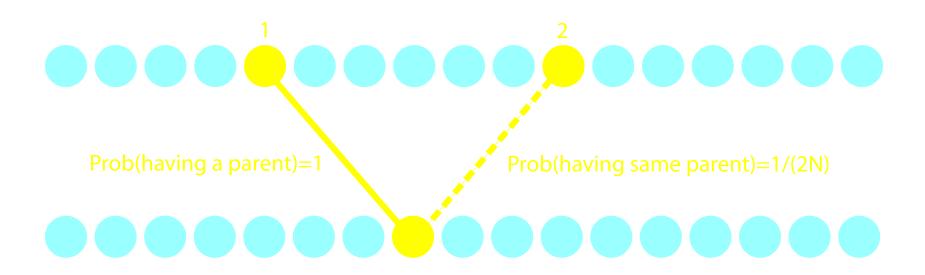
- Important conservation implications
- Effect on ecosystem significant:
  - Resuspension of up to 700 million cubic meters sediment
  - (12 Yukon Rivers worth)
  - Food for 1 million sea birds
- If accepted, result suggests halving gray whale kill rate
- Broadly similar results for minke, humpback, and fin whales

## Wright-Fisher population model



Sewall Wright showed that the probability that 2 gene copies come from the same gene copy in the preceding generation is

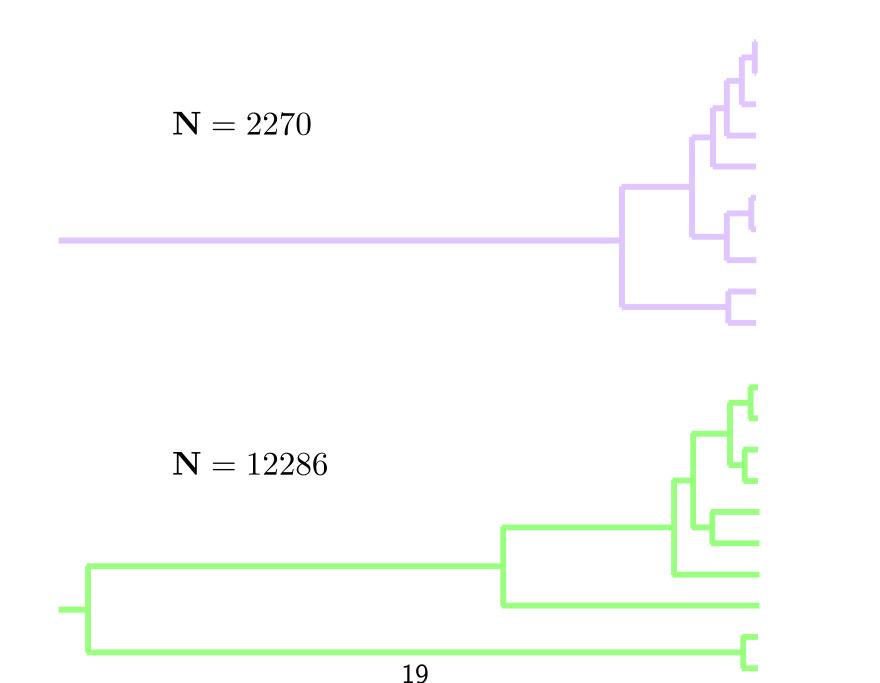
Prob (two genes share a parent) = 
$$\frac{1}{2N}$$



### Coalescence time depends on population size

- ullet Time back until a coalescence depends on population size N
- ullet For k lines, the expected time (backwards) until a coalescence is k(k-1)/2N
- The time back to the second, third, etc. has the same type of distribution
- We can estimate N by collecting information about coalescence times
- The bigger N is, the longer the coalescence times

# Coalescence time depends on population size



#### This would be great if....

- If we knew the tree, including its times, we would have a powerful estimator of population size
- Unfortunately this is difficult to infer
- Within-population variation too low for accurate phylogeny estimation
- We also have a problem with times:
  - All we observe (except with viruses or fossil DNA) is mutational differences
  - Need to know mutation rate  $\mu$  to get times

# The variable $\Theta$ (Theta)

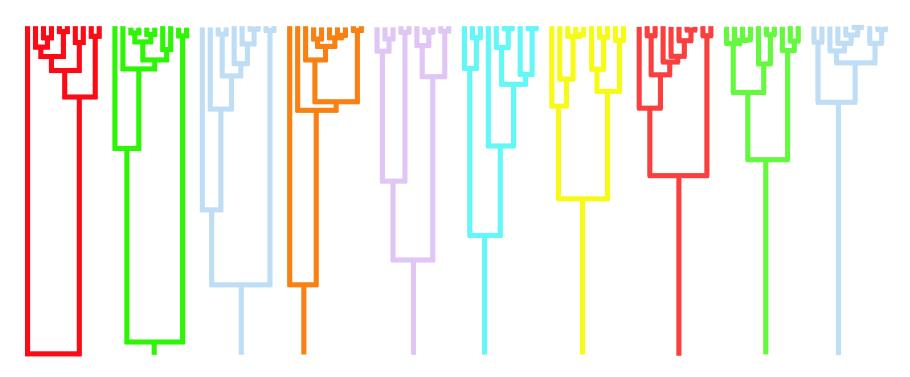
- ullet We estimate the compound parameter  $4N_e\mu$  also called  $\Theta$
- ullet One factor of 2 comes from each individual having two gene copies (so the number of gene copies is 2N)
- The other comes from mutations accumulating on both branches of the tree, so in 1 unit of time we accumulate 2 units of mutations

# The variable $\Theta$ (Theta)

- ullet Disappointing not to get  $N_e$  directly
- ullet If we can measure  $\mu$  experimentally we can convert  $\Theta$  to  $N_e$
- $\bullet$  Even if we can't,  $\Theta$  is interesting:
  - Comparing populations with similar mutation rate
  - Expected "carrying capacity" of genetic diversity
- Examples:
  - Estimated  $\Theta$  higher in Africans than other humans (expected)
  - Estimated  $\Theta$  higher in chimps than humans (not expected: bottleneck in humans?)

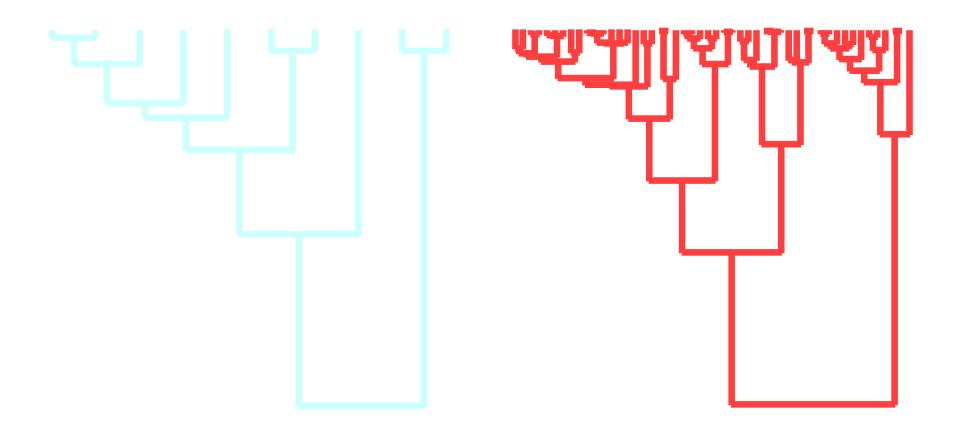
### Variability of the coalescent

A single gene can give a misleading answer:



10 coalescent trees generated with N = 10,000

# Does sampling more individuals help? (No)

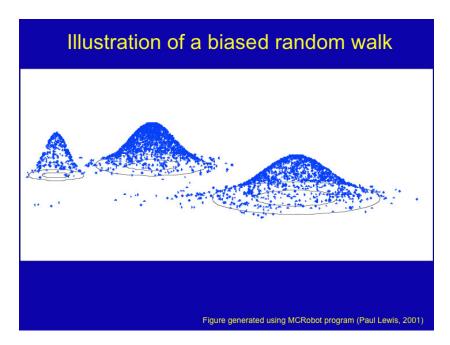


### **Summary-statistic approaches**

- Summary statistics look at the bulk properties of coalescent trees.
- They often require a simplified model of mutation.
- Watterson's estimator of  $\Theta$  counts variable sites
- We know how many variable sites to expect for various values of  $\Theta$ , sequence length and number of sequences
- This approach discards much of the information in the data

#### Many-tree approaches

- My lab tries to estimate Θ
  by considering many possible trees
- We write sampling algorithms which visit mainly the most likely trees
- Similar to Bayesian phylogenetic algorithm



#### Variants and extension of the coalescent

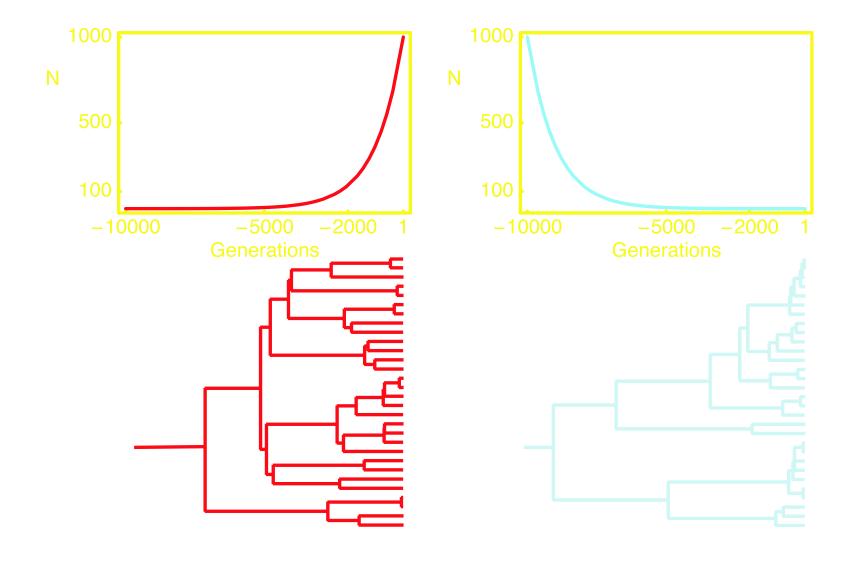
- Population growth/shrinkage over time
- Migration between populations
- Recombination
- Divergence of populations
- Selection (someday!)

#### Variable population size

- In a small population lineages coalesce quickly
- In a large population lineages coalesce slowly

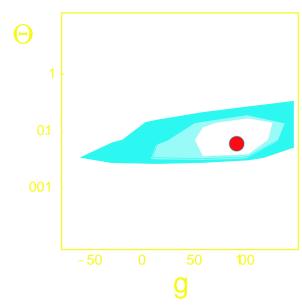
This leaves a signature in the data. We can exploit this and estimate the population growth rate g jointly with the population size  $\Theta$ .

# Exponential population size expansion or shrinkage



# Water frog data: easier to estimate $\Theta$ than g



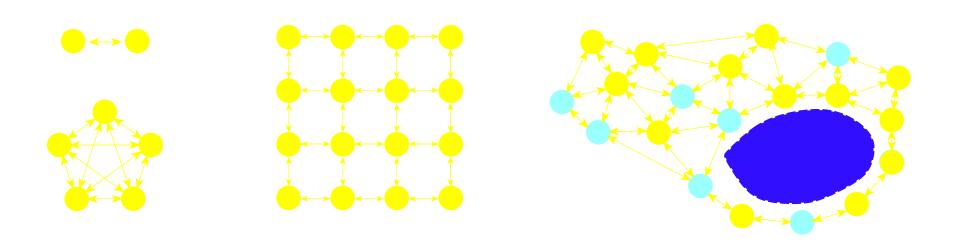


Mutation Rate

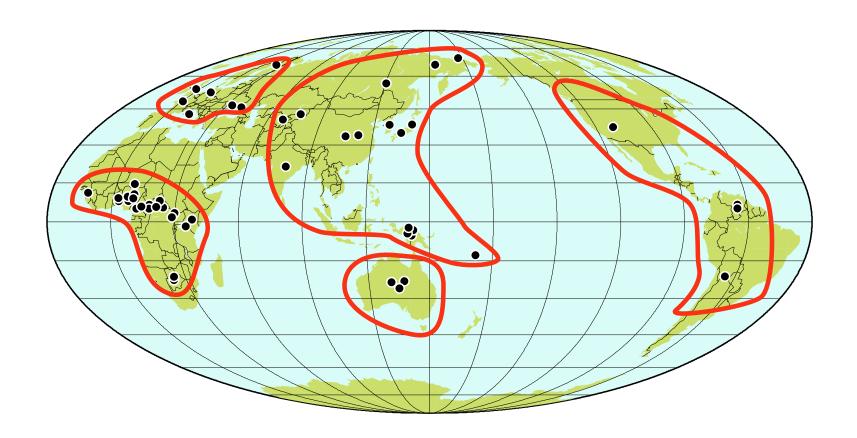
Population sizes

	-10000 generations	Present
$10^{-8}$	8,300,000	8,360,000
$10^{-7}$	780,000	836,000
$10^{-6}$	40,500	83,600

# Gene flow

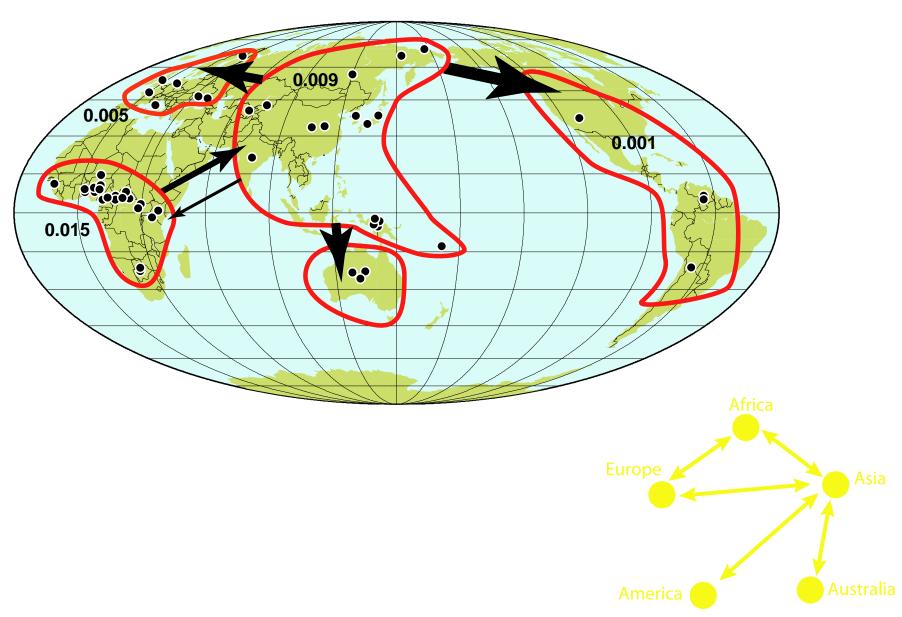


## Complete mtDNA from 5 human "populations"



A total of 53 complete mtDNA sequences ( $\sim$  16 kb): Africa: 22, Asia: 17, Australia: 3, America: 4, Europe: 7.

# Restricted model: only migration into neighbors allowed



Turner, Wares, and Gold (2002)

Genetic effective size is three orders of magnitude smaller than adult census size in an abundant, estuarine-dependent marine fish

Genetics 162:1329-1339



Red Drum, Sciaenops ocellatus

- Census population size: 3,400,000
- Effective population size: ?
- Data set:
  - 8 microsatellite loci
  - 7 populations
  - 20 individuals per population

#### Three approaches

- 1. Allele frequency fluctuation from year to year
  - Measures current population size
  - May be sensitive to short-term fluctuations
- 2. Coalescent estimate from Migrate
  - Measures long-term harmonic mean of population size
  - May reflect past bottlenecks or other long-term effects
- 3. Demographic models
  - Attempt to infer genetic size from census size
  - Vulnerable to errors in demographic model
  - Not well established for long-lived species with high reproductive variability

#### **Estimates:**

Census size (N): 3,400,000

Allele frequency method  $(N_e)$ : 3,516 (1,785-18,148)

Coalescent method  $(N_e)$ : 1,853 (317-7,226)

The demographic model can be made consistent with these only by assuming enormous variance in reproductive success among individuals.

- Allele frequency estimators measure current size
- Coalescent estimators measure long-term size
- Conclusion: population size and structure have been stable

- Effective population size at least 1000 times smaller than census
- This result was highly surprising
- Red drum has the genetic liabilities of a rare species
- Turner et al. hypothesize an "estuary lottery"
- Unless the eggs are in exactly the right place, they all die

### **Coalescent theory—summary**

- Genetic drift drives pattern of coalescences
- This embeds information about past population size in relationships among current individuals
- Various methods take advantage of this to estimate:
  - Population size, growth, shrinkage
  - Migration patterns
  - Recombination rates
  - Natural selection

### Other applications of the coalescent

- Tracking expansion of an epidemic (correlation with hospital records was amazing)
- How many humans in North America pre-Columbus?
- When did the extinct Beringian bison start to decline? Was it our fault? (Required ancient DNA samples)
- Deciding if foreign medics in Libya had brought HIV virus with them (no)

#### One-minute responses

- Tear off a half-sheet of paper
- Write one line about the lecture:
  - Was anything unclear?
  - Did anything work particularly well?
  - What could be better?
- Leave at the back on your way out