

# Roadmap

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- Chi-square test
- Mutation:
  - What kinds of mutation can occur?
  - How common are they?
  - What is the long-term effect of mutation by itself?

## Chi-square test

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$$\chi^2 = \sum \frac{(\textit{observed} - \textit{expected})^2}{\textit{expected}}$$

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Genotype	Observed	Expected	$(o - e)^2 / e$
HH	750	640	18.9
Hh	100	320	151.3
hh	150	40	302.5
			472.7

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Table lookup:

df	0.10	<b>0.05</b>	0.025	0.01	0.005
1	2.706	<b>3.841</b>	5.024	6.635	7.879
2	4.605	<b>5.991</b>	7.378	9.210	10.597
3	6.251	<b>7.815</b>	9.348	11.345	12.838

## Chi-square test – degrees of freedom

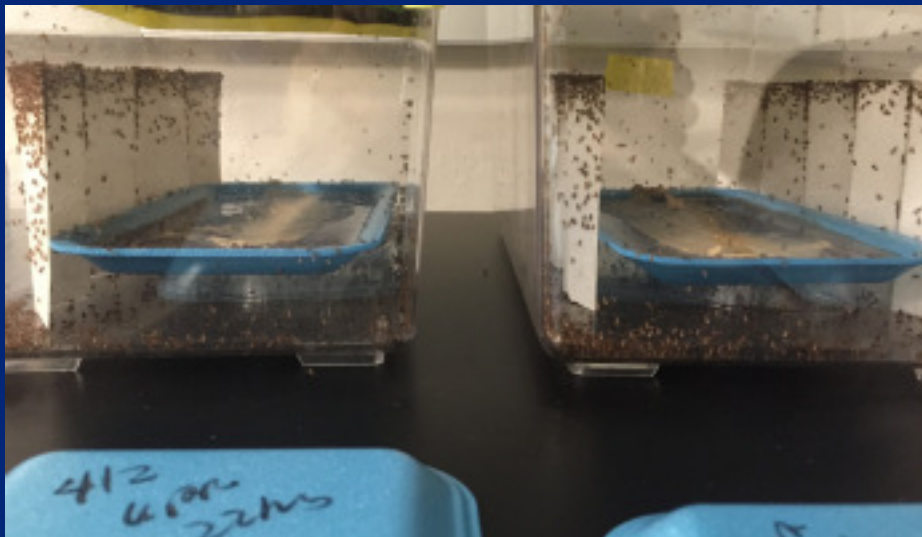
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- To test H-W with three categories:
  - Start with three observations
  - Use one up to get totals
  - Use one up to get allele frequencies
  - Left with 1 df

## Example: Dobzhansky and Levene 1948

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- Two different gene orders on chr. 3 in *D. pseudoobscura*
- Wild animals were bred in a large “population cage”
- Not in H-W: too many heterozygotes were observed
- What are some possible explanations?



## **Example: Dobzhansky and Levene 1948**

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- Females were taken from the cage and their eggs genotyped
- Eggs were in H-W for the two gene orders
- Which explanations does this rule out?

## Chi-square and degrees of freedom revisited

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- We mate 20 heterozygous red-eyed flies with 20 homozygous white-eyed flies (red is dominant)
- Offspring look like this:

Red	$Rr$	66
White	$rr$	34
- Start with 2 observations
  - Lose one for totals
  - Do NOT lose one for allele frequencies (already known)
- 1 df:  $\chi^2=10.24$ ,  $p=0.0014$ , significant



## Chi-square and degrees of freedom revisited

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- What if we had a box of random red and white eyed flies, and counted offspring?

Red $R?$	66
White $rr$	34
- Start with 2 observations
  - Lose one for totals
  - Lose one for allele frequencies
- Zero are left—*no test is possible*

## Chi-square and degrees of freedom revisited

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- Let's use snapdragons instead, where  $Rr$  is pink
- Random mix of red, white and pink parents gives us:

Red $RR$	17
Pink $Rr$	49
White $rr$	34
- Start with 3 observations
  - Lose one for totals
  - Lose one for allele frequencies
- 1 df:  $\chi^2=0.194$ ,  $p=0.9074$ , not significant

## Resources

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- Wikipedia article on Hardy-Weinberg is quite good
- Chi-square calculator at  
<http://www.graphpad.com/quickcalcs/chisquared2.cfm>

# Mutation

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- Any heritable change in the genetic material
- Provides raw material to evolution
- Without mutation, variation would be lost by:
  - natural selection
  - genetic drift (random chance)
- ...and evolution would eventually stop

# Roadmap

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- What kinds of mutations occur?
- What causes them?
- How frequent are they?
- What are their effects?
- What are the long-term implications of mutation on its own?
- Is mutation rate itself under natural selection? What rate would be optimal?

## Point mutations

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- coding changes (missense mutations)
- silent-site changes
- stop codons (nonsense mutations)
- control region changes
- changes in unused regions (“junk”)

## Other mutations

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- Insertions and deletions
  - Frameshifts—insertions or deletions that change the reading frame
- Duplications—multiple copies of a region
- Inversions—reverse gene order
- Translocations—move region elsewhere
- Transposon insertions

## Causes of Mutation

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- Replication errors
- Chemical damage—can include crosslinked bases, modified bases
- Radiation damage—often single and double-strand breaks
- Transposition
- Viral insertion
- Unequal crossing-over



## Mutation Rates

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Table taken from Farnsworth 1978. These are rates per locus, not per site; they were estimated by observing phenotypes.

E. coli	histidine auxotrophy	$2x10^{-6}$
	streptomycin sensitivity	$1x10^{-8}$
	phage T1 resistance	$2 - 3x10^{-8}$
Drosophila males	brown eyes	$3x10^{-5}$
	eyeless	$6x10^{-5}$
	yellow body	$1.2x10^{-4}$
Corn	colorless kernel	$2x10^{-6}$
	shrunk kernel	$1.2x10^{-6}$
Human	achondroplasia	$1x10^{-5}$
	aniridia	$2.9x10^{-6}$
	retinoblastoma	$6 - 7x10^{-6}$

## Some critters are sloppy

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Rates per bp per generation:

Human nuclear genome	$1 \times 10^{-9}$
mtDNA control region	$6 \times 10^{-6}$
HIV virus	$1 \times 10^{-3}$

- Difference is effort into proofreading

## The Standard Genetic Code

First Position (5' end)	Second Position				Third Position (3' end)
U	U	C	A	G	U
	UUU Phe	UCU Ser	UAU Tyr	UGU Cys	C
	UUC Phe	UCC Ser	UAC Tyr	UGC Cys	A
	UUA Leu	UCA Ser	UAA Stop	UGA Stop	G
	UUG Leu	UCG Ser	UAG Stop	UGG Trp	U
C	CUU Leu	CCU Pro	CAU His	CGU Arg	C
	CUC Leu	CCC Pro	CAC His	CGC Arg	A
	CUA Leu	CCA Pro	CAA Gln	CGA Arg	G
	CUG Leu	CCG Pro	CAG Gln	CGG Arg	U
A	AUU Ile	ACU Thr	AAU Asn	AGU Ser	C
	AUC Ile	ACC Thr	AAC Asn	AGC Ser	A
	AUA Ile	ACA Thr	AAA Lys	AGA Arg	G
	AUG Met	ACG Thr	AAG Lys	AGG Arg	U
	Start				
G	GUU Val	GCU Ala	GAU Asp	GGU Gly	C
	GUC Val	GCC Ala	GAC Asp	GGC Gly	A
	GUA Val	GCA Ala	GAA Glu	GGA Gly	G
	GUG Val	GCG Ala	GAG Glu	GGG Gly	

## Silent, coding, and control mutations

- The protein sequence is changed by:
  - Almost all 1st position changes
  - All 2nd position changes
  - Relatively few 3rd position changes
- If gene is important only via its protein, mutations which don't change the protein are unimportant
- This is not always true:
  - regulatory regions
  - splice sites
  - codon bias

# Mutation Rates

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- Silent and coding sites generally have the same underlying mutation rate
- However, many mutations at coding sites are lost
- Jargon:
  - Mutation rate: how rapidly do mutations occur?
  - Substitution rate: how rapidly do mutations accumulate?
- Silent positions generally have equal mutation rate, but higher substitution rate
- It is common but sloppy to refer to substitution rate as “mutation rate”

## Mutation without selection

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- Mutation rates at most loci are asymmetrical
- Easier to break a gene than fix it
- Mutation from  $A$  to  $a$  is  $\mu$  (mu)
- Mutation from  $a$  to  $A$  (back mutation) is  $\nu$  (nu)
- Equilibrium reached at:

$$pA = \frac{\nu}{\nu + \mu}$$

- Usually  $pA$  is very small at equilibrium.

## Mutation without selection

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- When  $\mu > \nu$  genes deteriorate without selection
- For organisms with “normal” mutation rates (around  $10^{-9}$  per bp) this process is VERY slow

## Mutation without selection

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Suppose there are 100 sites in a gene which will destroy function if they mutate, and each mutates with a probability of  $10^{-9}$ . Reverse mutation has to hit the same site, and has to restore the old base pair.

$$\mu = 10^{-7}$$

$$\nu = 0.33 \times 10^{-9}$$

What happens in one generation?

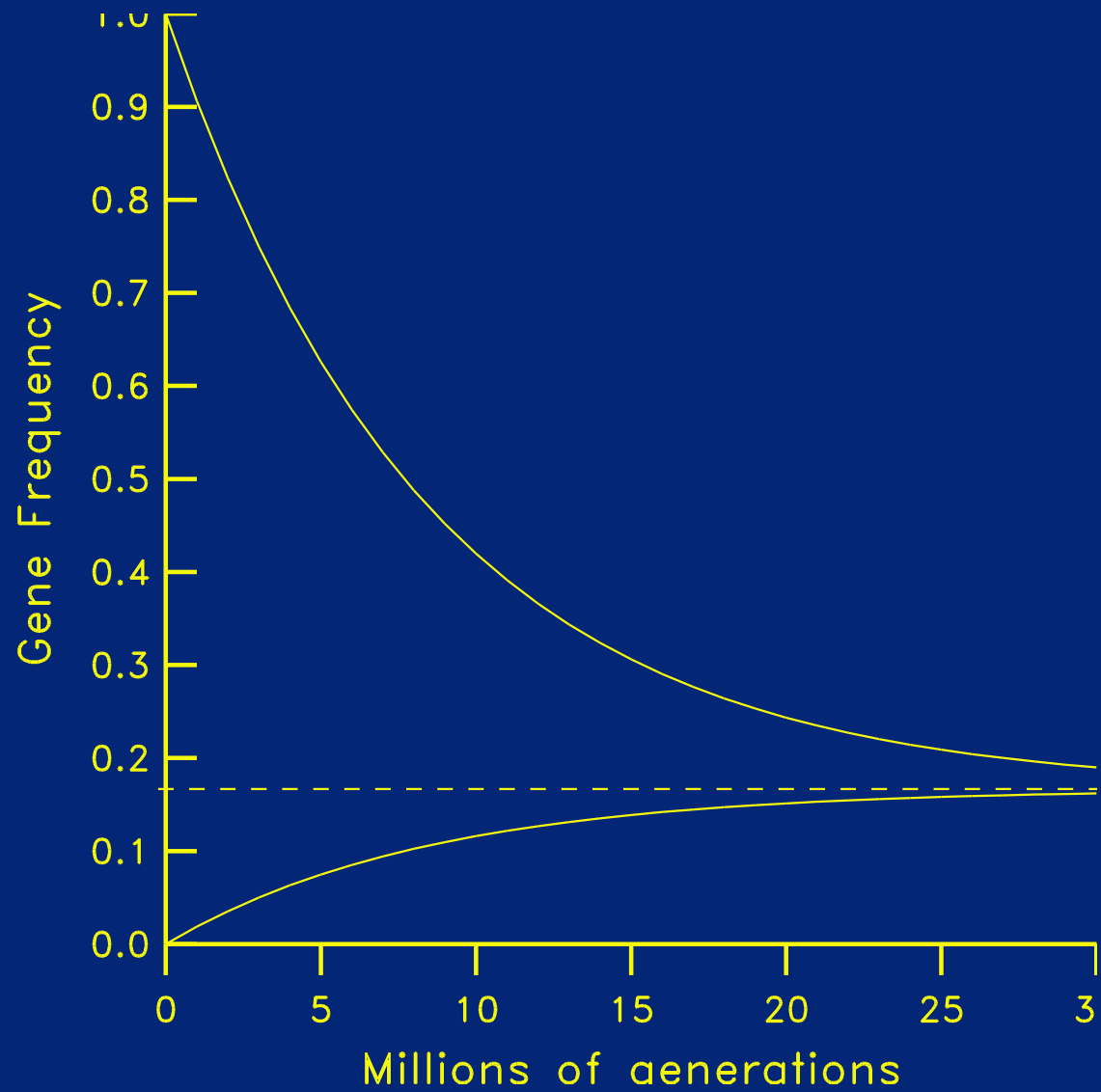
Allele	A	a
Frequency before mutation	0.9	0.1
Frequency after mutation	0.899999991	0.100000009

(The effect of reverse mutation is too tiny to see!)



## Mutation without selection

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## Genomic deterioration

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- Note the millions of generations in previous slide
- If we remove selection from a genetic disease:
  - Gene will eventually deteriorate
  - 1 million human generations = 20 million years
  - Human cultures and institutions aren't stable on this time scale....
- A bigger concern is alleles that are favorable with medicine but unfavorable without it

## Genomic deterioration—Practice problem

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- HIV-1 virus mutation rate of 0.001 per base per generation
- Assume 100 critical bp in the *env* gene
- A reverse mutation has to restore original sequence
- What is  $p_A$  (frequency of healthy allele) after 1 generation?
- (Ignore chance of multiple hits to the same virus)

## Genomic deterioration—Practice problem

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- HIV-1 virus mutation rate of 0.001 per base per generation
- Assume 100 critical bp in the *env* gene
- A reverse mutation has to restore original sequence
- What is  $pA$  (frequency of healthy allele) after 1 generation?
- (Ignore chance of multiple hits to the same virus)
- $\mu = 0.001 * 100 = 0.1$
- $\nu = 0.001/3 = 0.00033$
- $pA = 0.9$

## Genomic deterioration—Practice problem

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$$pA = \frac{\nu}{\nu + \mu}$$

- What is the equilibrium  $pA$ ?
- What would happen to this gene if it were not under selection?

## Genomic deterioration—Practice problem

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$$pA = \frac{\nu}{\nu + \mu}$$

- At equilibrium,  $pA = \frac{\nu}{\nu + \mu} = \frac{0.00033}{0.10033} = 0.0032$
- Without natural selection, mutation would rapidly destroy the HIV genome

## This equilibrium is fictional

- In reality there are always more than 2 possible alleles
- Once a gene starts deteriorating it will accumulate more mutations
- The number of functional copies will eventually drop to 0
- The equilibrium approach curve is more useful in showing early steps of this process

## Is mutation good or bad?

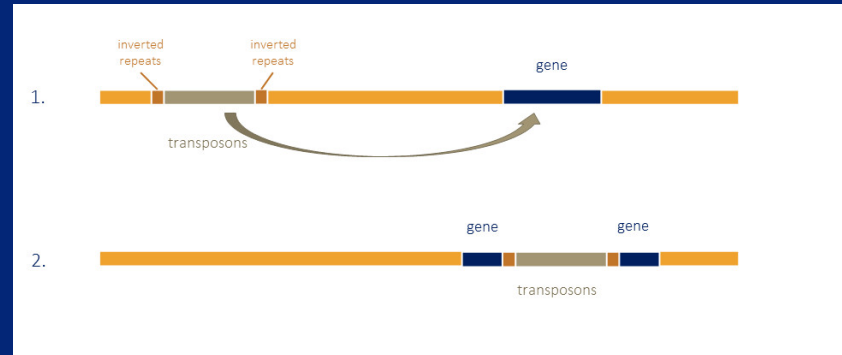
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- Most mutations have no fitness effect
- Of those that do, most are bad
- Most organisms expend significant energy trying to avoid mutations (DNA proofreading, etc)
- Are organisms trying (and failing) to reach a mutation rate of zero?
- Could there be selection in favor of a non-zero rate?



# Transposons as mutagens

- Transposons are genetic elements that can move around the genome
- This causes mutations:
  - Break up a coding sequence
  - Separate a gene from its control region
  - Introduce a new control region



## McClintock's genome shock hypothesis

- Transposition in maize increases when the plant is stressed
  - drought
  - salt
  - insects
- Transposition could be adaptive (“genome shock” theory)
  - Gives chance to fix the bad situation
- Transposition could be a symptom of illness
  - Transposons need to be kept under control
  - A sick plant can't do it

## How low can mutation rate go?

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- Discovered growing on irradiated meat
- Can withstand 1000x as much radiation as a human cell:
  - Chromosomes broken into about 100 pieces
  - Growth stops while chromosomes are repaired
  - Very few mutations result



*Deinococcus  
radiodurans*

## Very good replication fidelity is possible

- *D. radiodurans* has 4 copies of its genome (redundant backups)
- Natural environment sunny, salty, and hot
- All three can damage DNA
- Engineered *D. radiodurans* may be useful in biodegrading radioactive chemical waste

## Very good replication fidelity is possible

Presumably other cells could repair as well as *D. radiodurans*, but they don't.

- Redundant backups are expensive
- Repair machinery is expensive
- Mutations are expensive too (many are bad)
- Too-low mutation rate might inhibit adaptation
  - Hard to test this: it's a long-term effect

## Mutation rates in perspective

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- Human genome has  $6 \times 10^9$  bp.
- Point mutation rate around  $1 \times 10^{-9}$  per bp per generation
- Human population around 7 billion
- Every point mutation compatible with life exists somewhere
- Every human has several new point mutations

## Can I join the X-Men?

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- Most of these mutations are not in genes, and have little to no effect
- Many of the remaining ones are silent
- Most of the coding mutations are harmful
  - Most harmful mutations are recessive
  - Problem for your offspring, not for you....
- New beneficial mutations are rare
- Very different from Hollywood image of “mutants”

## One-minute responses

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- Tear off a half-sheet of paper
- Write one line about the lecture:
  - Was anything unclear?
  - Did anything work particularly well?
  - What could be better?
- Leave at the back on your way out