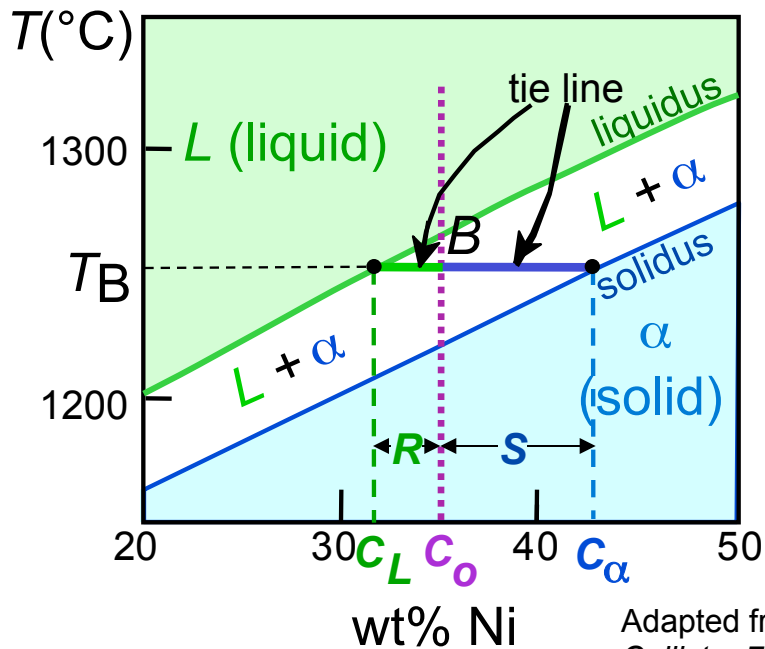


Chapter 9: Fe-C system

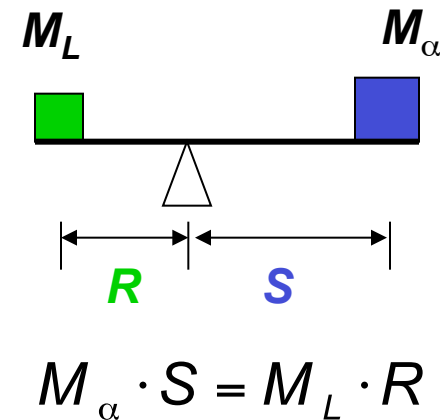
The Lever Rule

- Tie line – connects the phases in equilibrium with each other - essentially an isotherm



How much of each phase?

Think of it as a lever (teeter-totter)



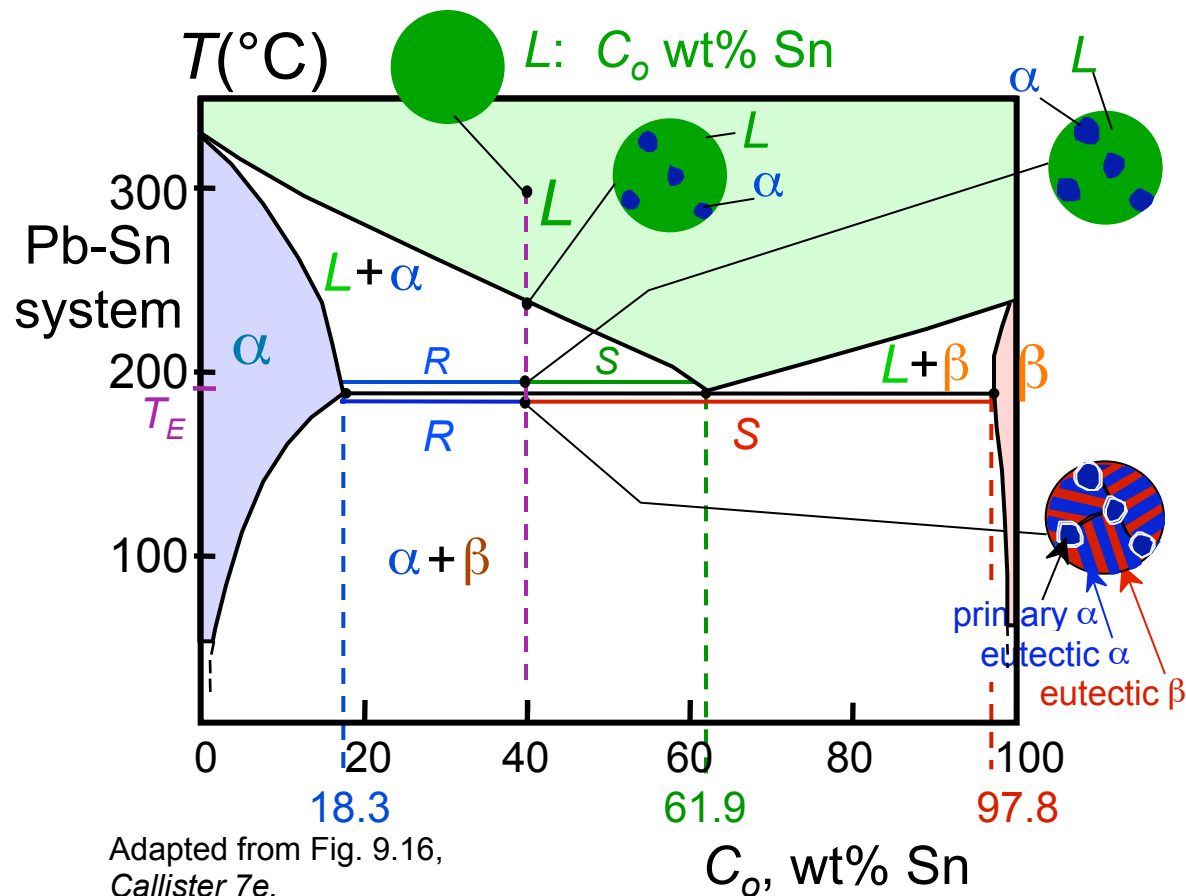
$$W_L = \frac{M_L}{M_L + M_{\alpha}} = \frac{S}{R + S} = \frac{C_{\alpha} - C_0}{C_{\alpha} - C_L}$$

$$W_{\alpha} = \frac{M_{\alpha}}{M_L + M_{\alpha}} = \frac{R}{R + S} = \frac{C_0 - C_L}{C_{\alpha} - C_L}$$



Microstructures in Eutectic Systems

- 18.3 wt% Sn < C₀ < 61.9 wt% Sn
- Result: α crystals and a eutectic microstructure



Adapted from Fig. 9.16,
Callister 7e.

- Just above T_E:
 - C_α = 18.3 wt% Sn
 - C_L = 61.9 wt% Sn
 - $W_{\alpha} = \frac{S}{R+S} = 50 \text{ wt\%}$
 - $W_L = (1 - W_{\alpha}) = 50 \text{ wt\%}$
- Just below T_E:
 - C_α = 18.3 wt% Sn
 - C_β = 97.8 wt% Sn
 - $W_{\alpha} = \frac{S}{R+S} = 73 \text{ wt\%}$
 - $W_{\beta} = 27 \text{ wt\%}$



Eutectoid & Peritectic

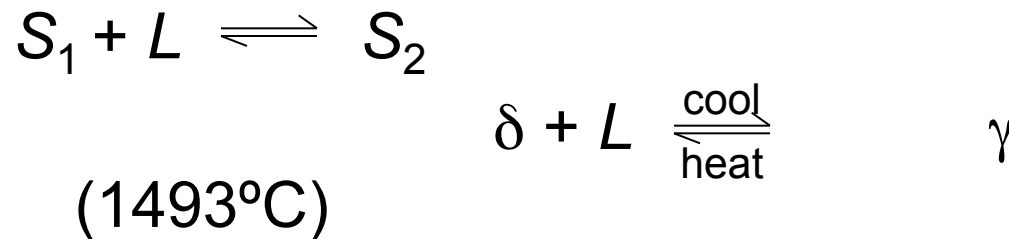
- **Eutectic** - liquid in equilibrium with two solids



- **Eutectoid** - solid phase in equilibrium with two solid phases



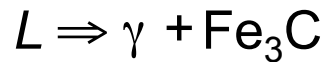
- **Peritectic** - liquid + solid 1 → solid 2 (Fig 9.21)



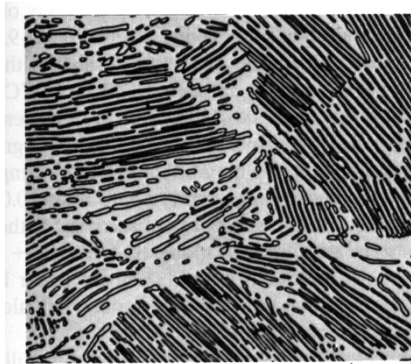
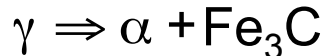
Iron-Carbon (Fe-C) Phase Diagram

- 2 important points

-Eutectic (A):



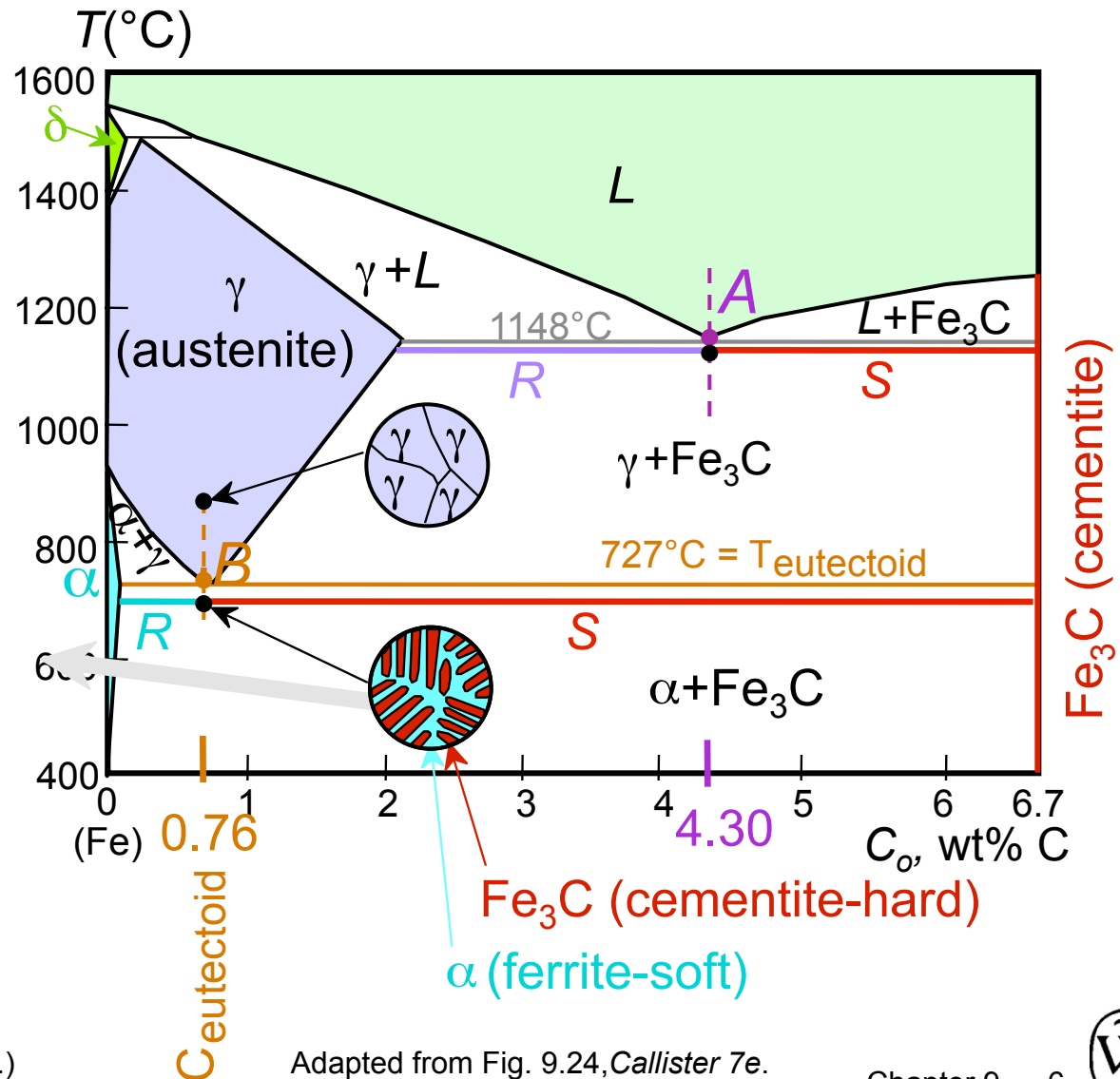
-Eutectoid (B):



120 μm

Result: Pearlite = alternating layers of α and Fe_3C phases

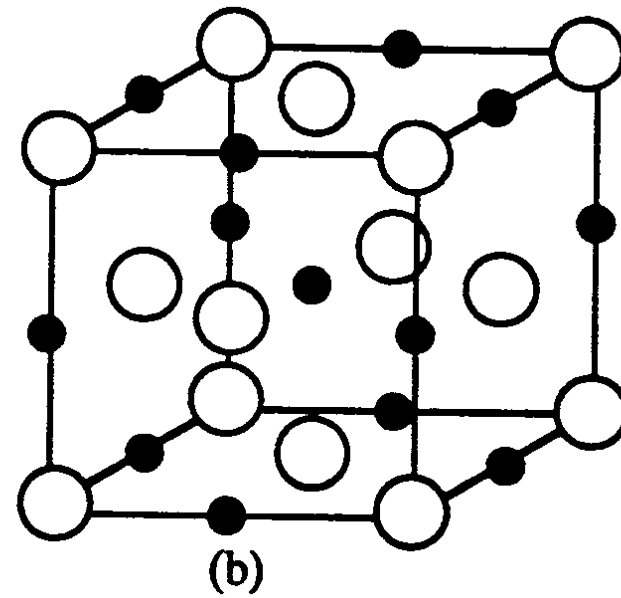
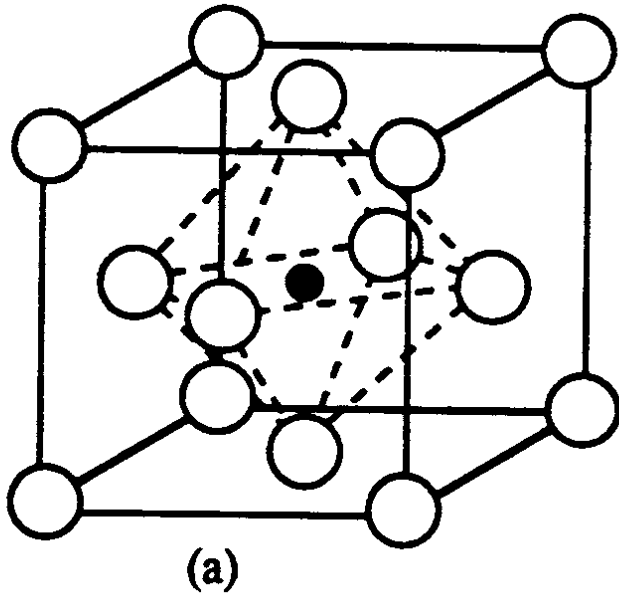
(Adapted from Fig. 9.27, Callister 7e.)



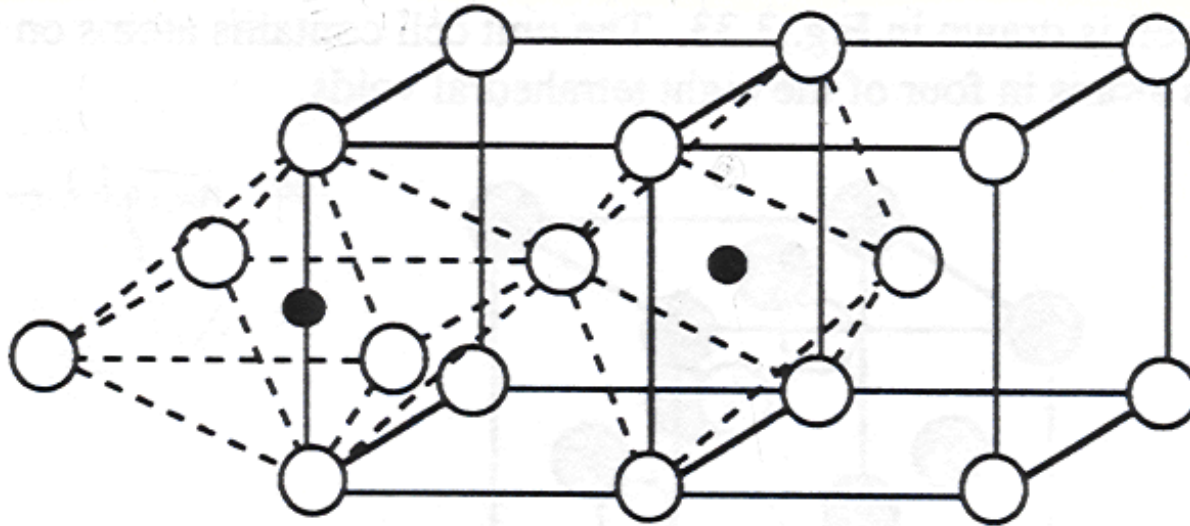
Adapted from Fig. 9.24, Callister 7e.



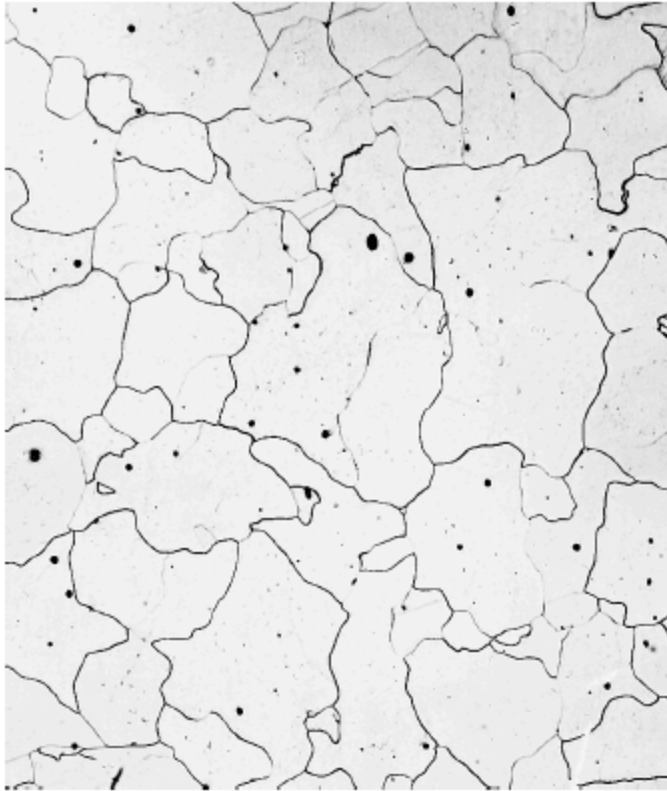
Interstitial sites of FCC



Interstitial sites of BCC

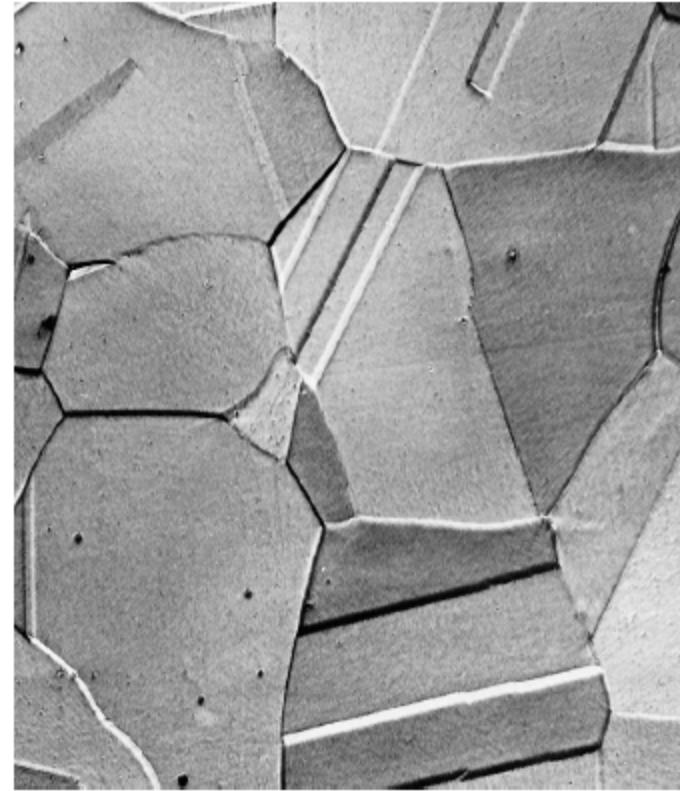


Microstructures of iron



(a)

α -ferrite

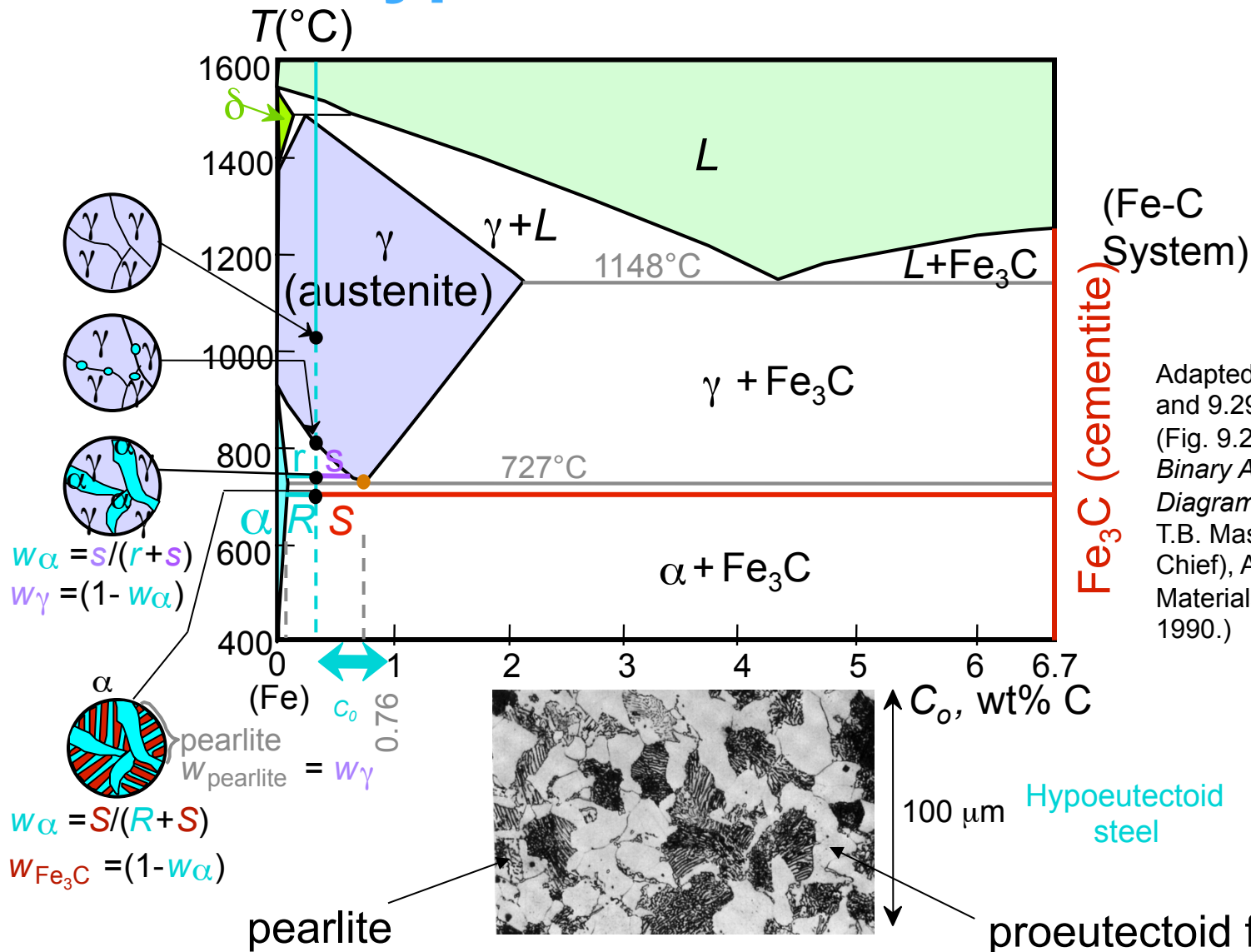


(b)

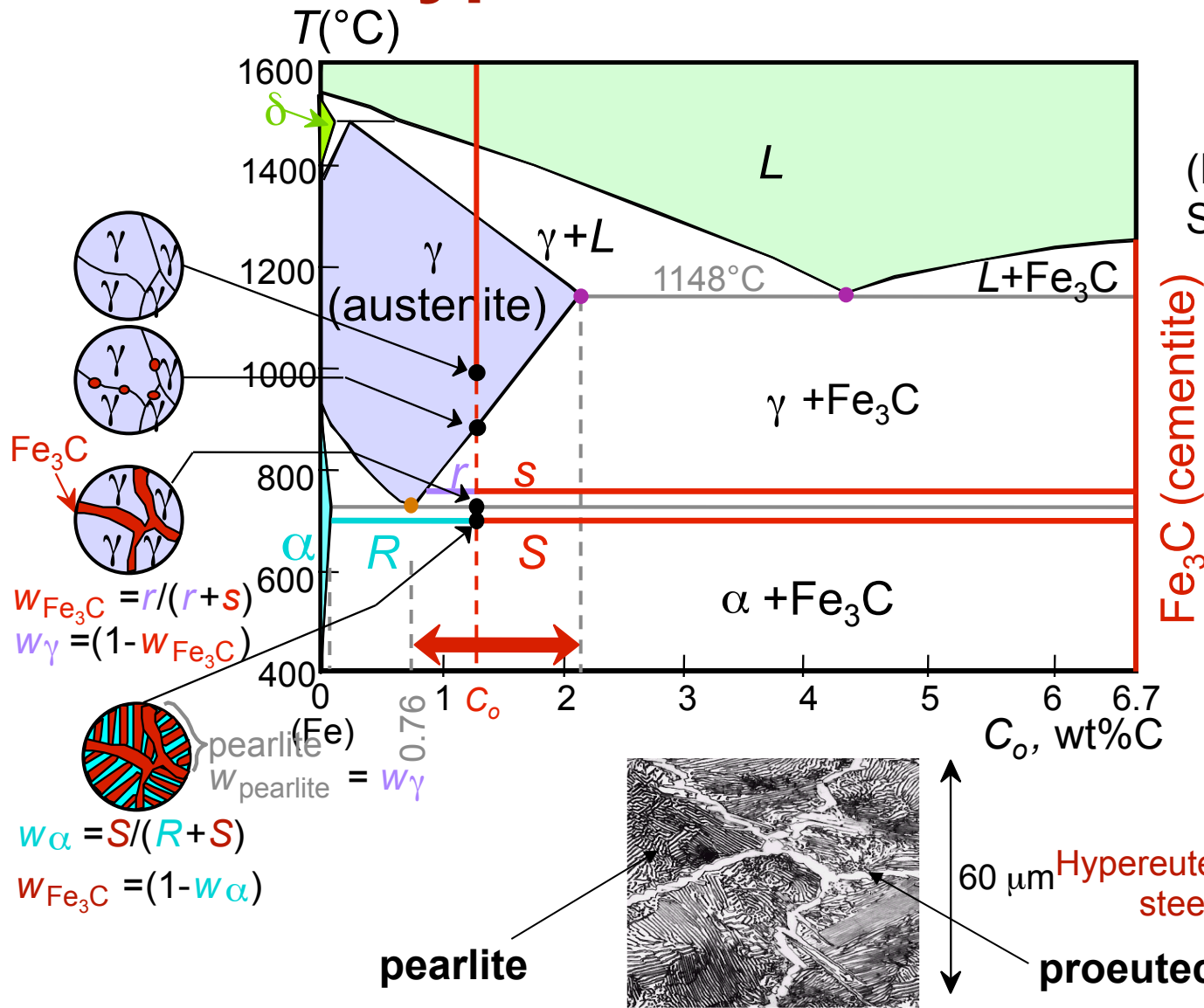
austenite



Hypoeutectoid Steel



Hypereutectoid Steel



Adapted from Fig. 9.33, *Callister 7e*.



Example: Phase Equilibria

For a 99.6 wt% Fe-0.40 wt% C at a temperature just below the eutectoid, determine the following

- a) composition of Fe_3C and ferrite (α)
- b) the amount of carbide (cementite) in grams that forms per 100 g of steel
- c) the amount of pearlite and proeutectoid ferrite (α)

Chapter 9 – Phase Equilibria

Solution: a) composition of Fe_3C and ferrite (α)

b) the amount of carbide (cementite) in grams that forms per 100 g of steel

$$C_o = 0.40 \text{ wt\% C}$$

$$C_\alpha = 0.022 \text{ wt\% C}$$

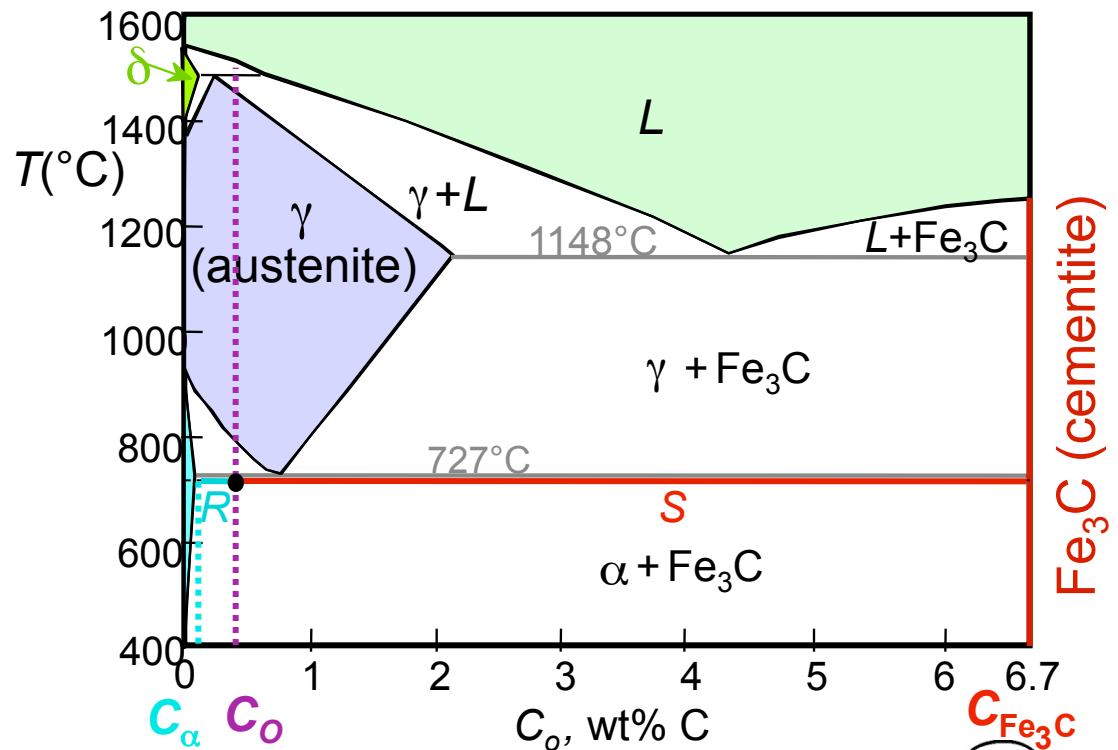
$$C_{\text{Fe}_3\text{C}} = 6.70 \text{ wt\% C}$$

$$\frac{\text{Fe}_3\text{C}}{\text{Fe}_3\text{C} + \alpha} = \frac{C_o - C_\alpha}{C_{\text{Fe}_3\text{C}} - C_\alpha} \times 100$$

$$= \frac{0.4 - 0.022}{6.7 - 0.022} \times 100 = 5.7\text{g}$$

$$\text{Fe}_3\text{C} = 5.7 \text{ g}$$

$$\alpha = 94.3 \text{ g}$$



Chapter 9 – Phase Equilibria

- c. the amount of pearlite and proeutectoid ferrite (α)
 note: amount of pearlite = amount of γ just above T_E

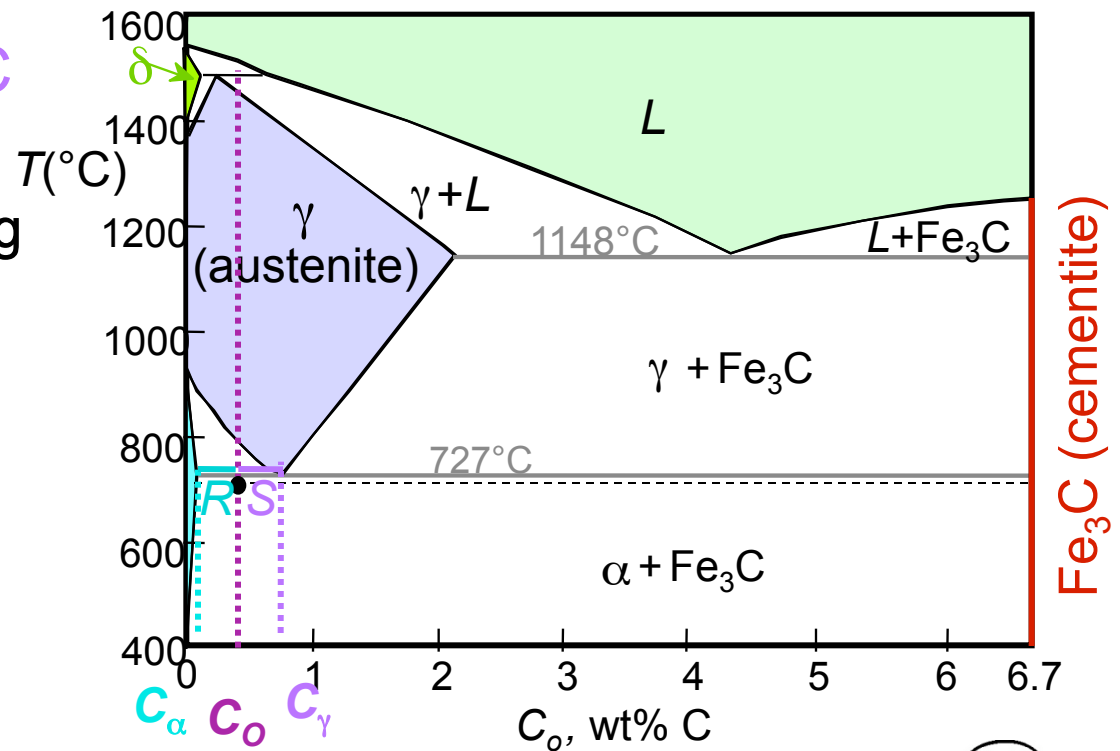
$$C_o = 0.40 \text{ wt\% C}$$

$$C_\alpha = 0.022 \text{ wt\% C}$$

$$C_{\text{pearlite}} = C_\gamma = 0.76 \text{ wt\% C}$$

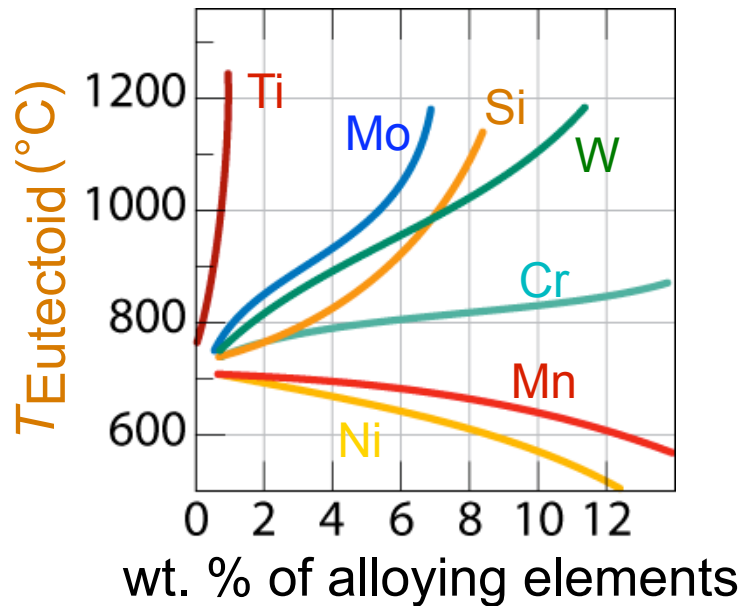
$$\frac{\gamma}{\gamma + \alpha} = \frac{C_o - C_\alpha}{C_\gamma - C_\alpha} \times 100 = 51.2 \text{ g}$$

pearlite = 51.2 g
 proeutectoid α = 48.8 g



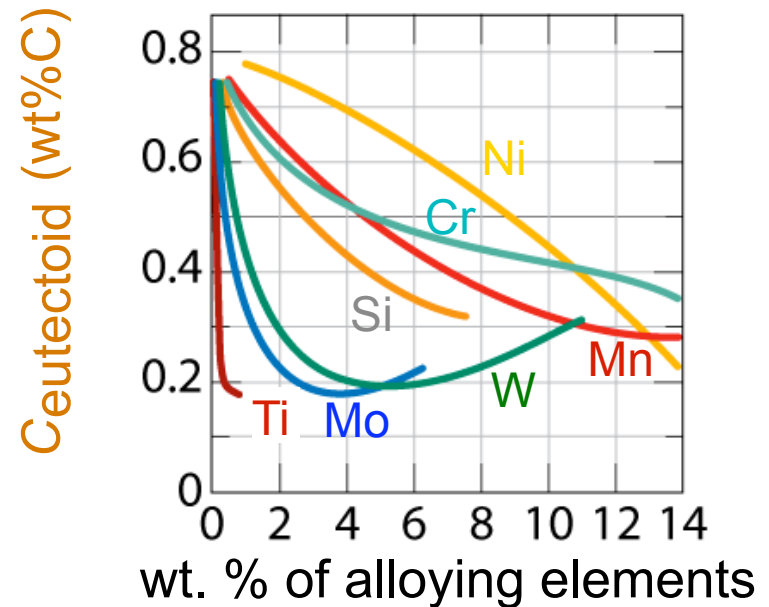
Alloying Steel with More Elements

- $T_{\text{eutectoid}}$ changes:



Adapted from Fig. 9.34, Callister 7e. (Fig. 9.34 from Edgar C. Bain, *Functions of the Alloying Elements in Steel*, American Society for Metals, 1939, p. 127.)

- $C_{\text{eutectoid}}$ changes:



Adapted from Fig. 9.35, Callister 7e. (Fig. 9.35 from Edgar C. Bain, *Functions of the Alloying Elements in Steel*, American Society for Metals, 1939, p. 127.)



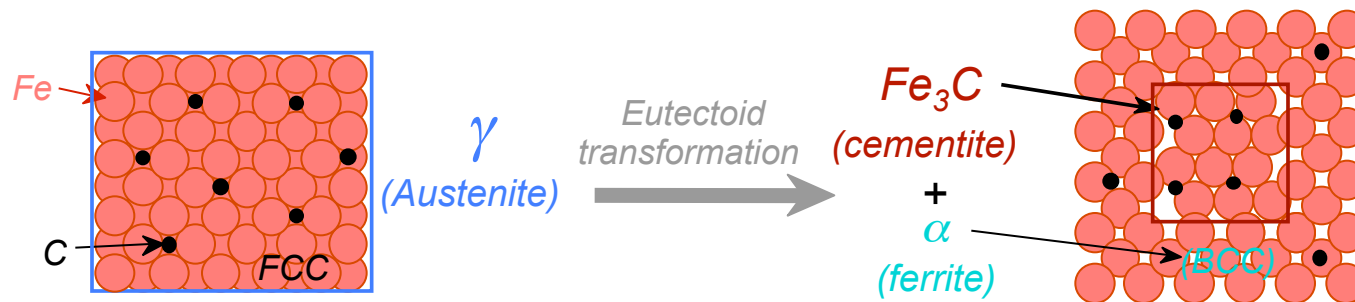
Summary

- **Phase diagrams** are useful tools to determine:
 - the number and types of phases,
 - the wt% of each phase,
 - and the **composition** of each phasefor a given T and composition of the system.
- Alloying to produce a solid solution usually
 - increases the tensile strength (TS)
 - decreases the ductility.
- Binary **eutectics** and binary **eutectoids** allow for a range of microstructures.



Chapter 10: Phase Transformations

- *Transforming one phase into another takes time.*



- *How does the rate of transformation depend on time and T ?*
- *How can we slow down the transformation so that we can engineer non-equilibrium structures?*
- *Are the mechanical properties of non-equilibrium structures better?*

t=time!

T=temperature!

ΔT = temperature difference from phase
transition temperature

Phase Transformations

Nucleation

- nuclei (seeds) act as template to grow crystals

Driving force to nucleate increases as we increase ΔT

In ΔT range close to T_m , rate of nucleation higher with higher ΔT

- *supercooling* (eutectic, eutectoid)

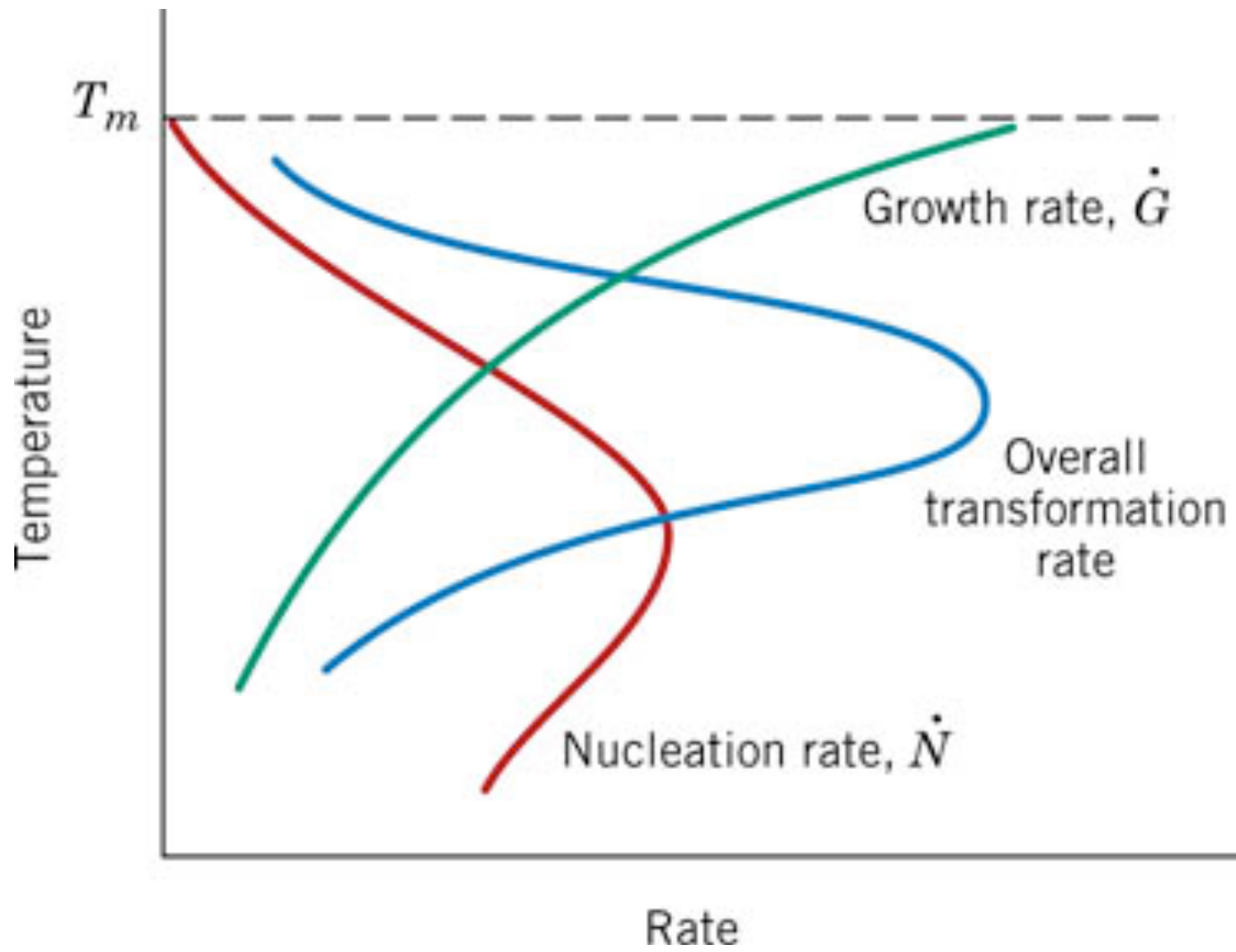
Growth

Growth rate increases with T (thermally activated)

$$dG/dt = C \exp(-Q/kT)$$

Small supercooling \rightarrow few nuclei - large crystals

*Large supercooling \rightarrow rapid nucleation - many nuclei,
small crystals*



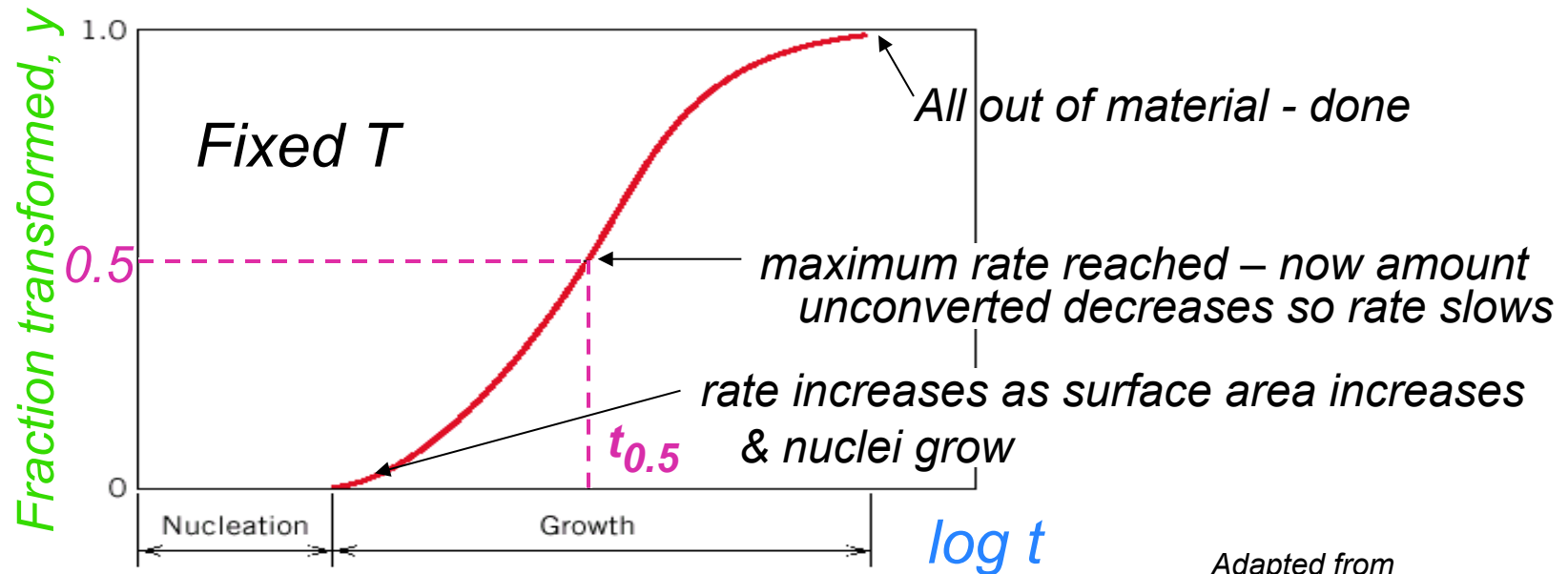
Rate of Phase Transformations

Kinetics - measure approach to equilibrium vs. time

- *Hold temperature constant & measure conversion vs. time*
 - *How is conversion measured?*
 - *X-ray diffraction – have to do many samples*
 - *electrical conductivity – follow one sample*
 - *sound waves – one sample*



Rate of Phase Transformation



Adapted from
Fig. 10.10,
Callister 7e.

Avrami rate equation $\Rightarrow y = 1 - \exp(-kt^n)$

fraction transformed *time*

– k & n fit for specific sample

By convention

$$r = 1 / t_{0.5}$$

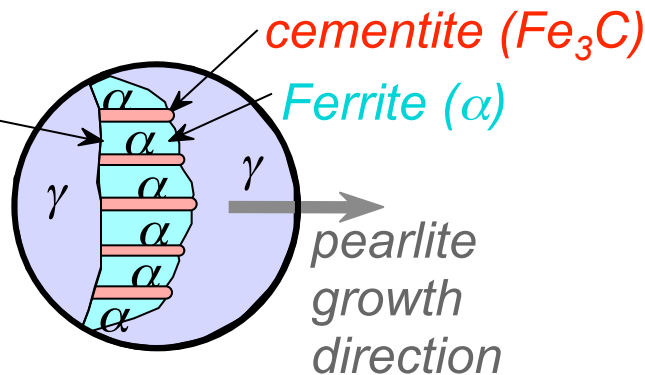


Eutectoid Transformation Rate

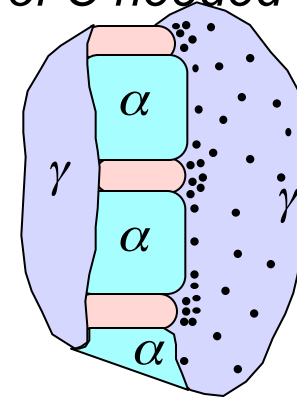
- Growth of pearlite from austenite:

Austenite (γ)
grain
boundary

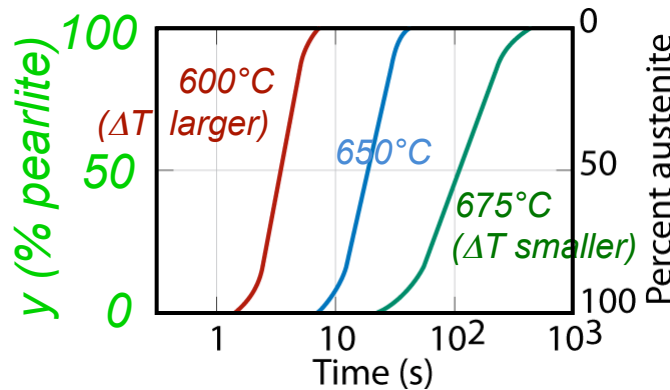
Adapted from
Fig. 9.15,
Callister 7e.



Diffusive flow
of C needed



- Recrystallization rate increases with ΔT .



Adapted from
Fig. 10.12,
Callister 7e.

Course pearlite → formed at higher T - softer
Fine pearlite → formed at low T - harder

