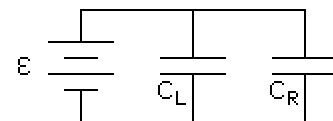


Part I. [21 points] An $\mathcal{E} = 18 \text{ V}$ battery is used to charge two identical capacitors $C_L = C_R = 5.0 \mu\text{F}$, as shown in this diagram.

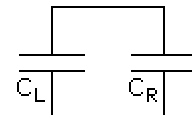


1. [4 points] Which choice best represents the magnitude of charge Q_R on either plate of the right hand capacitor C_R ?

- A. $2.8 \times 10^{-7} \text{ C}$
- B. $2.6 \times 10^{-6} \text{ C}$
- C. $2.3 \times 10^{-5} \text{ C}$
- D. $4.5 \times 10^{-5} \text{ C}$
- E. $9.0 \times 10^{-5} \text{ C}$

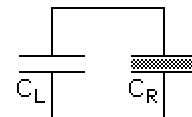
The battery is now removed as indicated in this diagram:

2. [5 points] Calculate the total energy stored in the capacitor network



- A. $3.2 \times 10^{-7} \text{ J}$
- B. $1.8 \times 10^{-4} \text{ J}$
- C. $2.0 \times 10^{-4} \text{ J}$
- D. $8.1 \times 10^{-4} \text{ J}$
- E. $1.6 \times 10^{-3} \text{ J}$

Next a dielectric with $k = 2.0$ is inserted between the plates of C_R , fully filling the available space as shown. (The dielectric carries zero net charge.)



3. [5 points] Recalculate the resulting charge Q_R on either plate of the right capacitor, C_R .

- A. $2.8 \times 10^{-5} \text{ C}$
- B. $6.0 \times 10^{-5} \text{ C}$
- C. $1.2 \times 10^{-4} \text{ C}$
- D. $1.8 \times 10^{-4} \text{ C}$
- E. $3.6 \times 10^{-6} \text{ C}$

4. [3 points] Calculate the voltage across C_R :

- A. 6.0 V
- B. 9.0 V
- C. 12 V
- D. 15 V
- E. 18 V

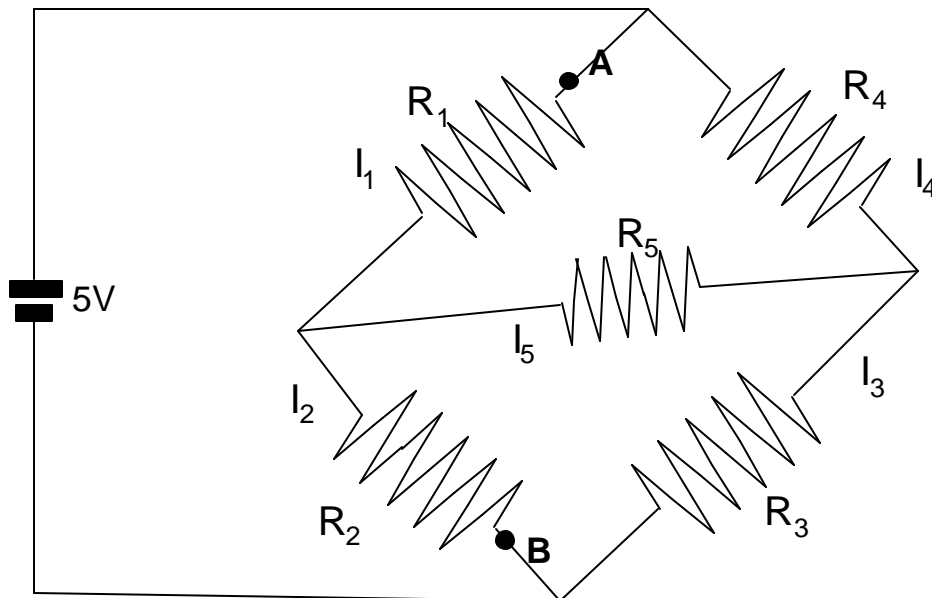
5. [4 points] A 30 V battery is reconnected to the circuit as above (though the dielectric is left in C_R). Calculate the energy now stored in the capacitor network.

- A. $4.5 \times 10^{-4} \text{ J}$
- B. $5.9 \times 10^{-4} \text{ J}$
- C. $1.1 \times 10^{-3} \text{ J}$
- D. $4.5 \times 10^{-3} \text{ J}$
- E. $6.8 \times 10^{-3} \text{ J}$

last

first

Part II. [34 points] Consider the circuit at the left. The ideal battery is rated at 5V. R_1 is $25\ \Omega$, R_2 is $50\ \Omega$, R_3 is $150\ \Omega$, and R_5 is $75\ \Omega$. R_4 is set so that the current I_5 is zero.



6. [3 points] What is the magnitude of potential difference across R_5 ?

- A. 0.0 V
- B. 1.3 V
- C. 2.5 V
- D. 5.0 V
- E. 7.3 V

7. [5 points] What is the value of R_4 ?

- A. $25\ \Omega$
- B. $50\ \Omega$
- C. $75\ \Omega$
- D. $150\ \Omega$
- E. $175\ \Omega$

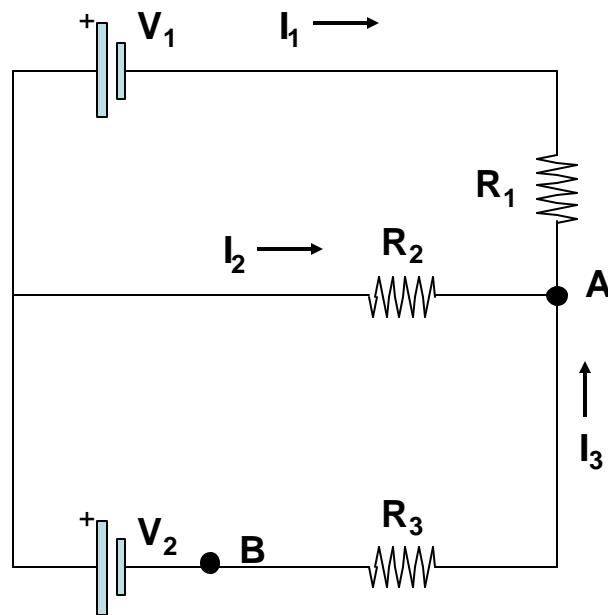
8. [4 points] If the resistor R_5 is doubled, how will R_4 have to change in order to keep I_5 zero?

- A. Increase R_4
- B. Decrease R_4
- C. No Change to R_4
- D. It will not be possible to make I_5 zero.
- E. Not enough information

9. [4 points] What is the magnitude of the potential between points A and B?

- A. 0.0 V
- B. 1.2 V
- C. 4.0 V
- D. 5.0 V
- E. 6.2 V

Consider the circuit at the right for the rest of this problem. V_1 is 5 V and V_2 is 9 V. R_1 , R_2 , and R_3 are $20\ \Omega$, $130\ \Omega$, and $40\ \Omega$, respectively. The voltage between points A and B is measured to be 1.3 V



10. [5 points] What is the current I_1 ?

- A. 13 mA
- B. 63 mA
- C. 73 mA
- D. 85 mA
- E. 140 mA

11. [5 points] What is the current I_2 ?

- A. 10 mA
- B. 28 mA
- C. 38 mA
- D. 59 mA
- E. 69 mA

12. [3 points] What is the current I_3 ?

- A. 21 mA
- B. 33 mA
- C. 37 mA
- D. 43 mA
- E. 48 mA

13. [5 points] Which of the following loop equations is correct, given the directions of the assumed current flow on the diagram?

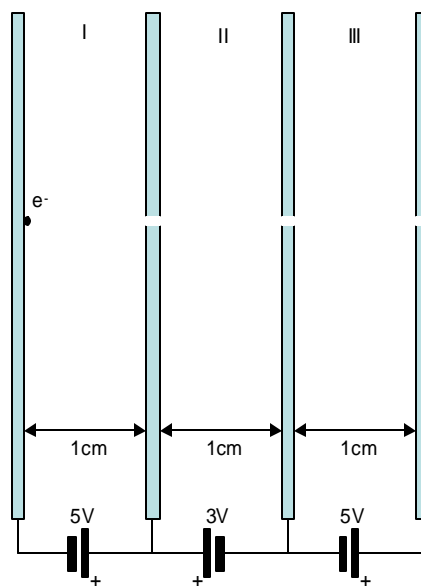
- A. $V_1 - R_1 I_1 + I_2 R_2 = 0$
- B. $I_1 + I_3 = I_2$
- C. $-V_1 + I_1 R_1 - I_3 R_3 - V_2 = 0$
- D. $-V_2 - I_3 R_3 + I_2 R_2 = 0$
- E. $V_2 + I_3 R_3 + I_2 R_2 = 0$

last

first

Part III. [25 points] An electron accelerator element consists of 4 metal plates separated by 1cm with small holes, as shown in the figure (as a cross section). The two outer plates are connected by 5 V batteries, and a reversed biased 3V battery in the middle, as shown. Each plate is very thin compared to the distance between them. $m_e = 9.11 \times 10^{-31}$ kg, charge on an electron is 1.6×10^{-19} C.

14. [10 points] An electron is released from the left-most plate. How fast is it moving when it leaves the small hole in the right most plate?



15. [10 points] Calculate the direction and magnitude of the electric field between the plates, in regions I, II, and III (see labels at the top of the figure).

16. [5 points] How would removing the middle two plates change your answers above? Assume all three batteries remain connected as before. Explain.

