

Constants you may find useful

$$G = 6.67 \times 10^{-11} \text{ Nm}^2/\text{kg}^2$$

$$M_{\text{Earth}} = 5.97 \times 10^{24} \text{ kg}$$

$$M_{\text{Sun}} = 1.99 \times 10^{30} \text{ kg}$$

$$r_{\text{Earth}} = 6.38 \times 10^3 \text{ km}$$

$$r_{\text{Sun}} = 6.96 \times 10^5 \text{ km}$$

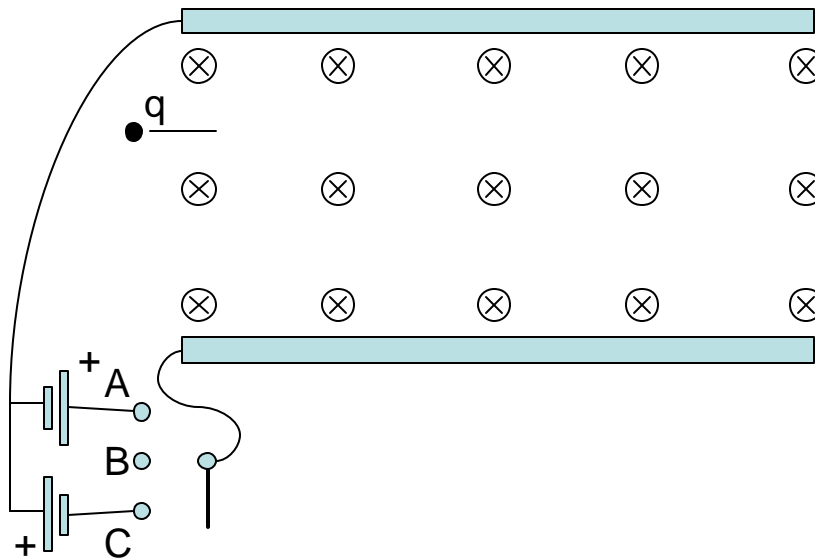
$$d_{\text{Sun-Earth}} = 149.6 \times 10^6 \text{ km}$$

$$g = 9.8 \text{ m/s}^2$$

$$\epsilon_0 = 8.85 \times 10^{-12} \text{ C}^2/(\text{Nm}^2)$$

$$\mu_0 = 4\pi \times 10^{-7} \text{ Tm/A}$$

Part I. [30 points] A particle with a charge q is shot through a velocity selector, shown at right. The device is made up of two plates connected to a battery which create an electric field, and is also immersed in a magnetic field, which points into the page. When a particle enters with the correct velocity it will travel in a straight, horizontal line. Ignore gravity. The magnitude of the magnetic field is 0.2 T , and the device is 1.5 m long.



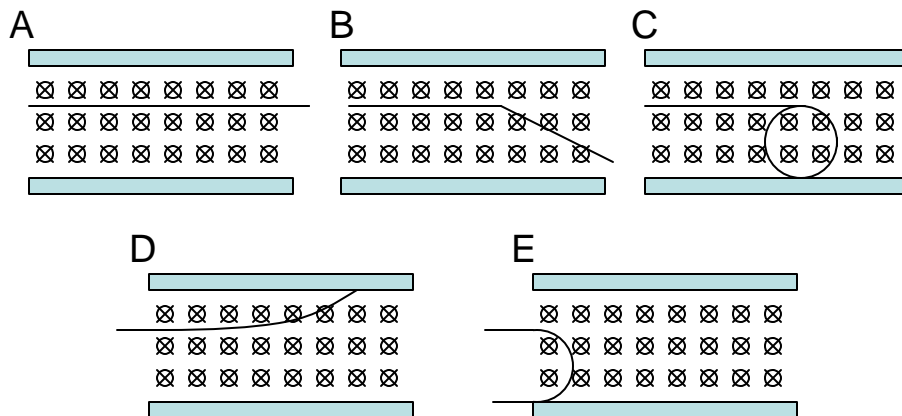
- [4 points] For the velocity selector to work, the particle q must move in a horizontal line. What position must the switch be in to accomplish this?
 - A
 - B (disconnected)
 - C
 - A or C
 - A or B or C
- [5 points] The device is designed to select particles with a velocity of 500 m/s . Determine the magnitude of the electric field, E
 - 0.30 N/C
 - 100 N/C
 - 150 N/C
 - 450 N/C
 - 750 N/C
- [5 points] A particle with mass $1.0 \times 10^{-3}\text{ kg}$ enters at 500 m/s , and travels through in a straight horizontal line. Determine its charge.
 - 0.0 C
 - $5.0 \times 10^{-3}\text{ C}$
 - $8.3 \times 10^{-3}\text{ C}$
 - $1.1 \times 10^{-2}\text{ C}$
 - Not possible to determine
- [3 points] The particle enters with a speed of 400 m/s . Which of the following statements is true?
 - The magnitude of F_B increases and the magnitude of F_E remains constant.
 - The magnitude of F_B decreases and the magnitude of F_E remains constant.
 - The magnitude of F_B remains constant, but the magnitude of F_E increases.
 - The magnitude of F_B remains constant, but the magnitude of F_E decreases.
 - The magnitudes of both F_B and F_E decrease.

The electric field is adjusted to be 230 V/m (and the B field magnitude remains 0.2 T). A particle with charge +0.2 mC enters at 1200 m/s.

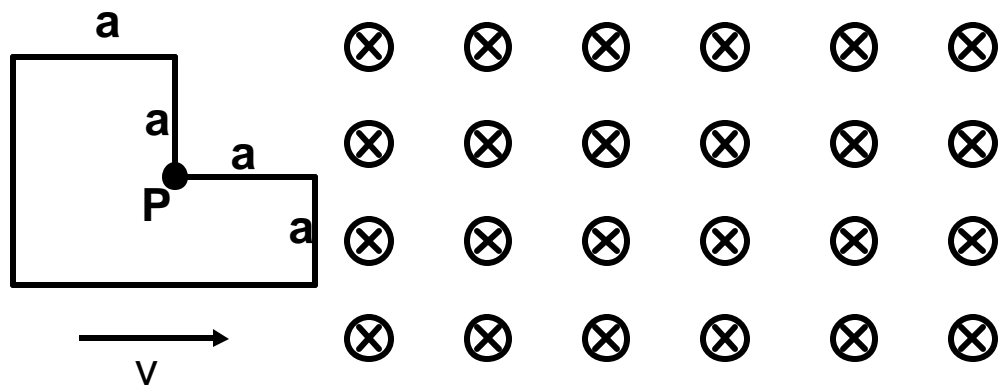
5. [3 points] Which of the following best describes the particles trajectory?
- A. The particle curves towards the top plate.
 - B. The particle curves towards the bottom plate.
 - C. The particle travels in a horizontal line through the velocity selector
 - D. Not enough information given to determine.
6. [3 points] As the particle starts to travel through the velocity selector,
- A. Its net velocity will increase.
 - B. Its net velocity will decrease.
 - C. Its net velocity will decrease exponentially.
 - D. Its net velocity will remain the same

The electric field is now shut off, leaving only the magnetic field. A negatively charged particle is shot into the magnetic field directly between the two plates (which are separated by 5 cm). The particle's initial velocity is 600 m/s, its charge is 0.2 mC, and its mass is 1.0×10^{-9} kg.

7. [3 points] Which trajectory best represents the possible path of the particle?

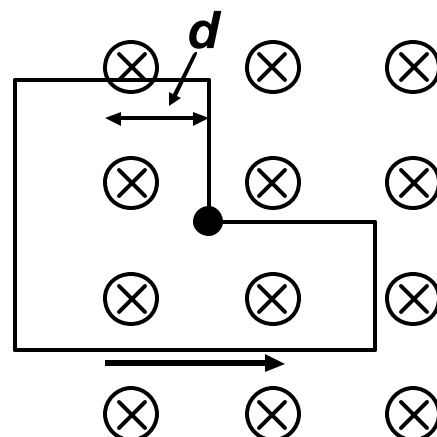


8. [4 points] What is the radius of curvature of the particle?
- A. 1.0×10^{-2} m
 - B. 1.5×10^{-2} m
 - C. 2.5 m
 - D. 9.0 m
 - E. It moves in a straight line, so there is no radius of curvature!



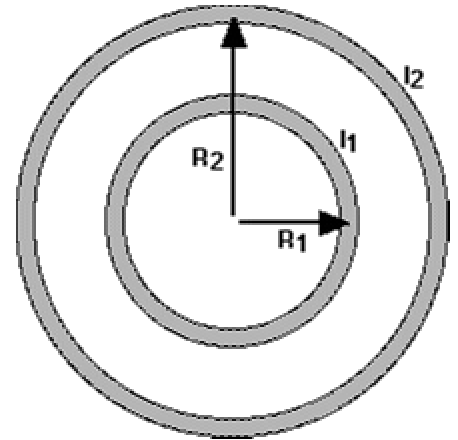
Part II. [25 points] Consider the wire loop next to the magnetic field area at left. The length a is 5 cm. The point P is fixed to the loop at the position shown. The loop is moving to the right with a speed of $v = 3$ m/second. The magnetic field is 2.5 T.

9. [4 points] Just before point P enters the magnetic field, which of the following statements is true?
- A. The induced magnetic field is in the opposite direction field already present, and is only present in the interior of the loop already in the field.
 - B. The current flow in the loop is counter clockwise.
 - C. The induced magnetic field points into the page, and the current flows counter clockwise.
 - D. The induced magnetic field is present throughout the interior of the loop, and points into the page.
 - E. None of the above.
10. [6 points] At the same point – just before the point P enters the magnetic field - calculate the induced EMF in the loop.
- A. 6.3×10^{-3} V
 - B. 1.9×10^{-2} V
 - C. 1.3×10^{-1} V
 - D. 3.8×10^{-1} V
 - E. 1.2 V
11. [5 points] Calculate the induced EMF as the second half of the loop enters the magnetic field. l is the distance the second part of the loop is in the magnetic field.
- A. $1.3 \times 10^{-2} d + 6.3 \times 10^{-3}$ V
 - B. $3.8 \times 10^{-2} d$ V
 - C. 3.8×10^{-2} V
 - D. 7.5×10^{-1} V
 - E. $7.5 \times 10^{-1} d$ V



12. [6 points] While the loop is completely inside the field, the magnetic field is uniformly reduced down from 2.5 T to 1.0 T over a period of 2 seconds. The induced EMF in the loop is
- A. 1.9×10^{-3} V
 - B. 3.8×10^{-3} V
 - C. 5.6×10^{-3} V
 - D. 7.5×10^{-3} V
 - E. 1.1×10^{-2} V
13. [4 points] The wire loop is cut, and a resistor with resistance R is used to rejoin the cut bits of the loop. The resistor, R, is much greater than the intrinsic resistance of the wire loop. Which of the following would be true:
- A. It would require less force to pull the wire into the magnetic field, but not out of.
 - B. It would require more force to put the loop both into and out of the magnetic field.
 - C. It would less force to both pull the loop into and out of the magnetic field.
 - D. It would require more force to pull the loop out of, but not into the magnetic field.
 - E. There would be no change.

Part III. [25 points] A thin, infinitely long cylindrical conducting **shell** of radius $R_1 = 3 \text{ cm}$ carries a current $I_1 = 21 \text{ mA}$ in the $+z$ -direction (out of the page). This current is uniformly distributed in the azimuthal direction about the z -axis. A second thin, infinite cylindrical shell of radius $R_2 = 8 \text{ cm}$ carries a current $I_2 = 26 \text{ mA}$, also in the $+z$ -direction, also uniformly distributed in the azimuthal direction. The two conducting shells are very thin.



14. [5 points] What is the magnitude of the net magnetic field at a distance $r = 1.5 \text{ cm}$ from the axis of symmetry? Explain.
15. [4 points] What is the magnitude of the magnetic field at a distance $r = 16 \text{ cm}$ from the axis of symmetry?
16. [5 points] What is the magnitude of the magnetic field due to the current I_1 alone at $r = R_2$?
17. [7 points] Calculate the magnitude of the magnetic force *per unit area* on the outer shell due to current I_1 .
18. [4 points] Calculate the magnitude of the net magnetic force *per unit length* in the z -direction on the outer shell due to current I_1 . Explain.