

Constants: $k_e = 8.99 \times 10^9 \text{ Nm}^2 / \text{C}^2$ $\epsilon_o = \frac{1}{4\pi k_e} = 8.85 \times 10^{-12} \text{ F / m}$ $e = 1.602 \times 10^{-19} \text{ C}$

$m_e = 9.11 \times 10^{-31} \text{ kg}$ $m_p = 1.67 \times 10^{-27} \text{ kg}$ $N_A = 6.02 \times 10^{23} \text{ items / mole}$ $G = 6.67 \times 10^{-11} \text{ Nm}^2 / \text{kg}^2$

Dielectric strength of air = 30,000 V/cm = 3 MV/m

Electric Field:

$$\vec{F}_{q_o} = q_o \vec{E}(\vec{r}_{q_o}) \quad \vec{E}(\vec{r}_o) = k_e \sum_i \frac{Q_i}{r_{io}^2} \hat{r}_{io} \quad \vec{E}(\vec{r}_o) = k_e \int_{\text{charge distribution}} \frac{dq}{r_{qo}^2} \hat{r}_{qo} \quad \vec{E}_{\text{point}}(\vec{r}) = \frac{k_e q}{r^2} \hat{r} \quad E_{\text{line}} = \frac{2k_e q}{r} \hat{r} \quad \vec{E}_{\text{plane}}(\vec{r}) = \frac{\sigma}{2\epsilon_o} (\text{out})$$

Electric Potential & Potential Energy

$$\Delta U = q\Delta V = -W_{\text{by field}} \quad \Delta U = U_b - U_a = -\int_a^b \vec{F} \cdot d\vec{\ell}$$

$$U_{\text{2 point charges}} = \frac{q_1 q_2}{r_{12}} \quad \Delta V = V_b - V_a = -\int_a^b \vec{E} \cdot d\vec{\ell} \quad E_x = -\frac{\partial V}{\partial x} \quad V_{\text{point}}(r) = \frac{k_e q}{r} - \frac{k_e q}{R_{\text{ref}}} \quad V_{\text{line}}(R) = 2k_e \lambda \ln \frac{R_{\text{ref}}}{R} \quad V(r) = k_e \int_{\text{charge distribution}} \frac{dq}{r}$$

Conductor at Equilibrium

$E = 0$ inside; $E = \frac{\sigma_{\text{surface}}}{\epsilon_o}$ just outside; $V = \text{constant}..$

Gauss' Law and Coulomb's Law

$$\vec{F}_{12} = k_e \frac{q_1 q_2}{r_{12}^2} \hat{r}_{12}; \quad \vec{r}_{12} = \vec{r}_1 - \vec{r}_2 \quad \Phi_e = \iint \vec{E} \cdot d\vec{A} = \iint (\vec{E} \cdot \hat{n}) dA \quad \Phi_{\text{net}} = \iint_{\text{closed surface}} \vec{E} \cdot d\vec{A} = \frac{q_{\text{enclosed}}}{\epsilon_o} = \frac{1}{\epsilon_o} \iiint_{\text{enclosed volume}} \rho dV$$

Circuits: Capacitance, Current and Resistance

$$Q = CV; \quad U = \frac{1}{2} QV = \frac{1}{2} CV^2 = \frac{1}{2} \frac{Q^2}{C} \quad C_{\text{parallel}} = C_1 + C_2 \quad C_{\text{series}} = \left(\frac{1}{C_1} + \frac{1}{C_2} \right)^{-1}$$

parallel plate: $C_{pp} = \frac{\kappa \epsilon_o A}{d}$; coaxial cable: $C_{\text{coax}} = \frac{2\pi \kappa \epsilon_o L}{\ln(R_2/R_1)}$; isolated sphere: $C_{\text{sphere}} = 4\pi \kappa \epsilon_o R$

$$I = GV = \frac{V}{R}; \quad \text{Power} = I^2 R = IV = \frac{V^2}{R}; \quad G = \frac{\sigma A}{L}; \quad R = \frac{1}{G} = \rho \frac{L}{A} \quad R_{\text{parallel}} = \left(\frac{1}{R_1} + \frac{1}{R_2} \right)^{-1} \quad R_{\text{series}} = R_1 + R_2$$

$$\sum_{\text{closed loop}} \Delta V = 0 \quad \sum_{\text{point}} I = 0 \quad I \text{ same in series; } \Delta V \text{ same in parallel} \quad \vec{J} = nq\vec{v}_{\text{drift}} \quad I = \iint \vec{J} \cdot d\vec{A}$$

Geometry and Definitions: Surface Area: $A_{\text{sphere}} = 4\pi R^2$ $A_{\text{cyl}} = 2\pi RH + 2\pi R^2$ $A_{\text{cube}} = 6a^2$

Volume: $V_{\text{sphere}} = \frac{4}{3}\pi R^3$ $V_{\text{cyl}} = \pi R^2 H$ $V_{\text{cube}} = a^3$

Linear Charge Density: $\lambda = \frac{Q}{\text{length}}$; Areal Charge Density: $\sigma = \frac{Q}{\text{Area}}$;

Volume Charge Density $\rho = \frac{Q}{\text{volume}}$ $\cos 30^\circ = \frac{\sqrt{3}}{2}; \sin 30^\circ = \frac{1}{2}; \cos 45^\circ = \sin 45^\circ = \frac{\sqrt{2}}{2}$

Kinematics

$$\vec{a} = \frac{\vec{F}}{m} = \frac{q}{m} \vec{E} \quad x = x_o + v_o t + \frac{1}{2} a t^2 \quad v = v_o + a t$$